



Solar-like oscillators

Information in the frequency power spectrum

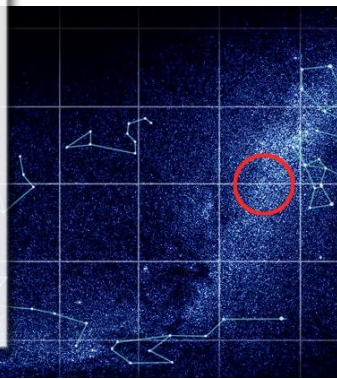
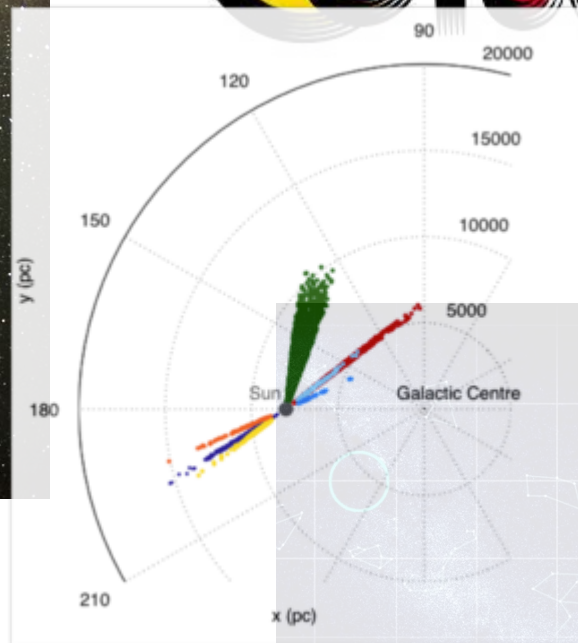
Kepler



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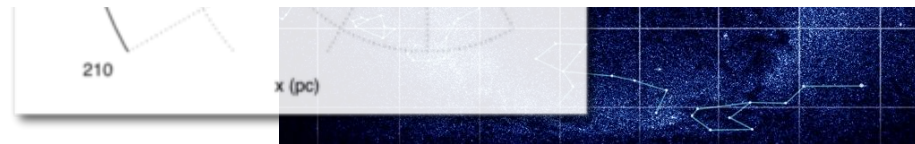
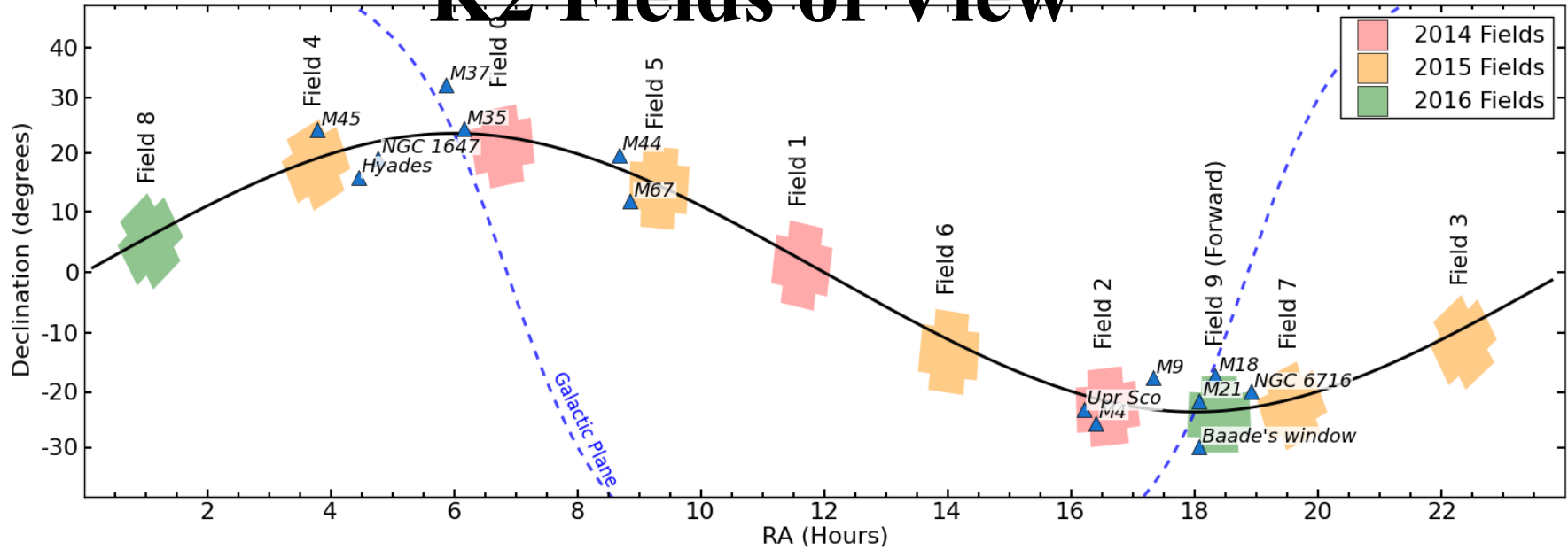


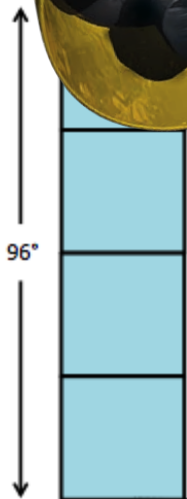
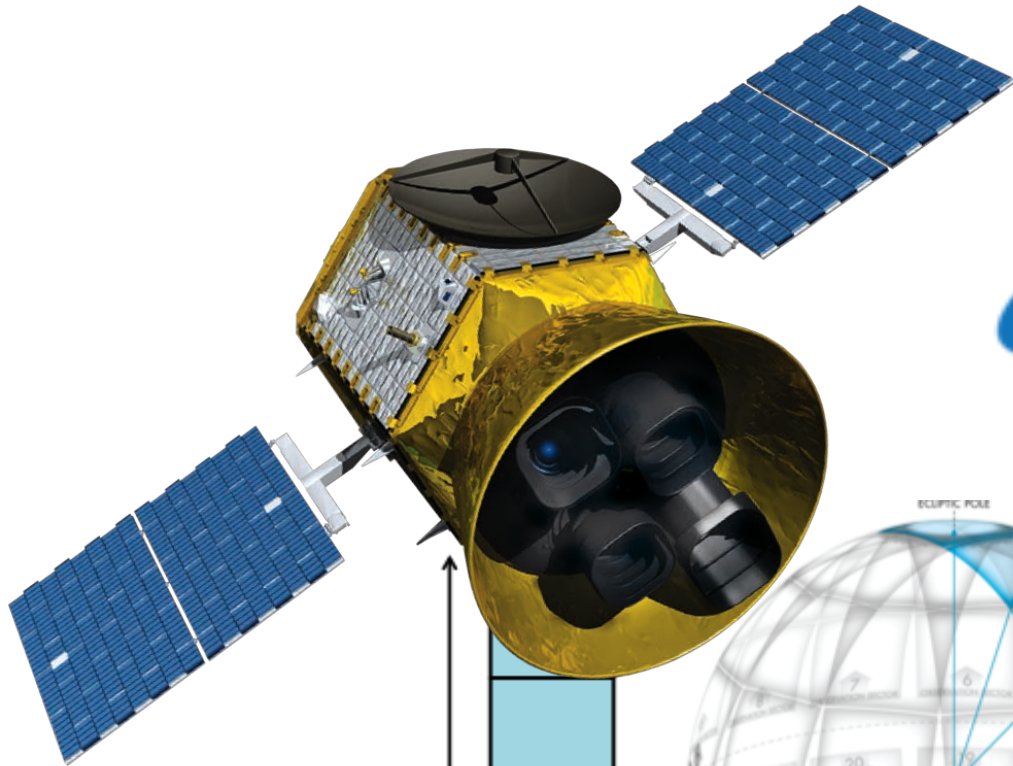
Kepler





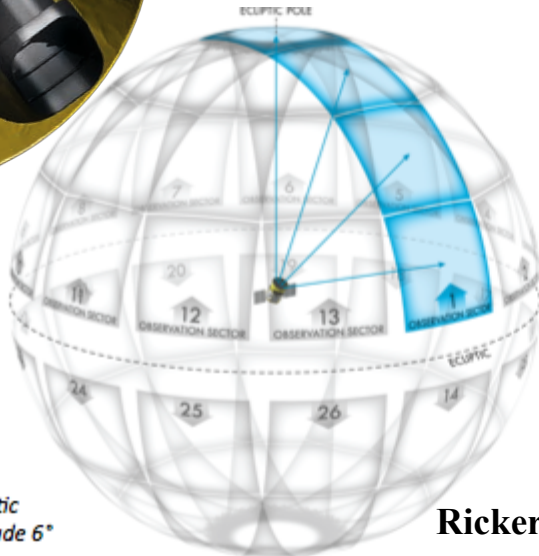
K2 Fields of View



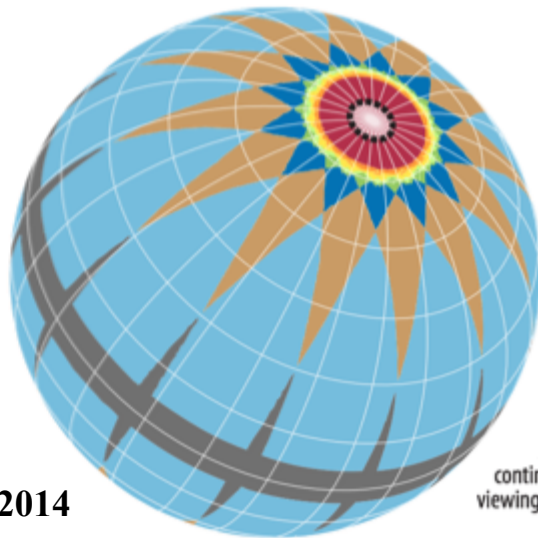


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ecliptic latitude 6°

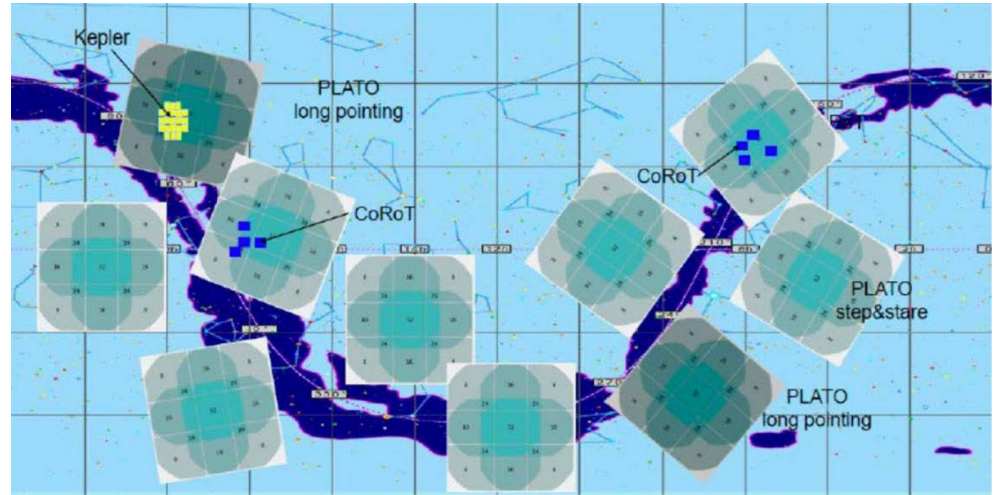
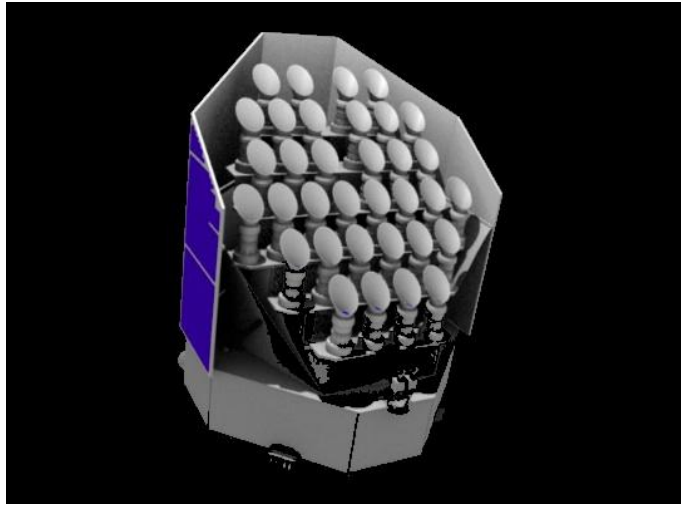


Ricker 2014

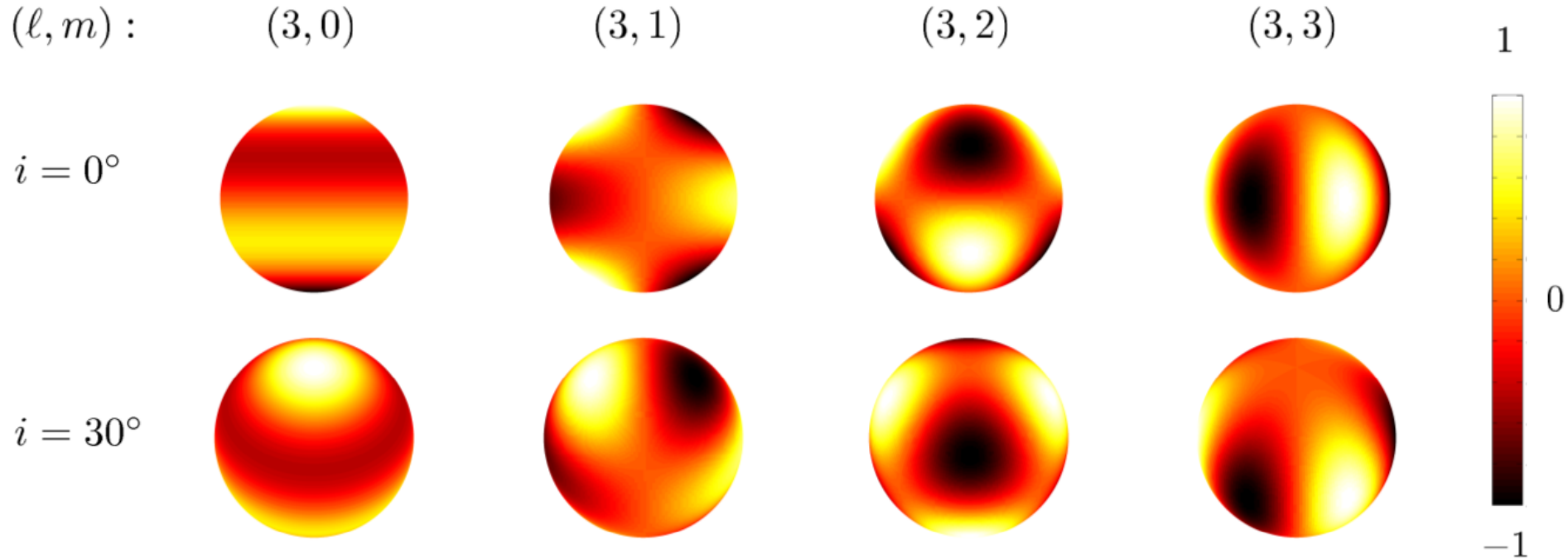


- 27 days
- 54 days
- 81 days
- 108 days
- 189 days
- 351 days

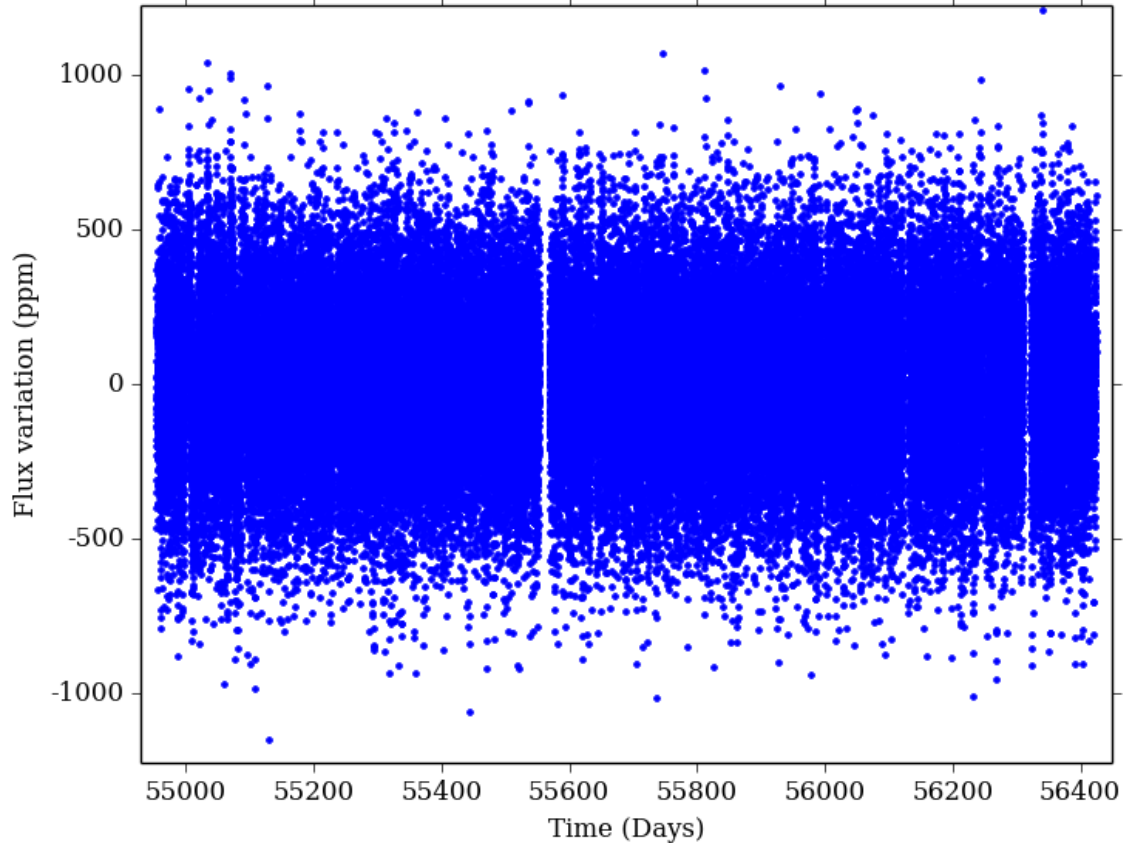
JWST continuous viewing zone



Oscillations produce variations in intensity

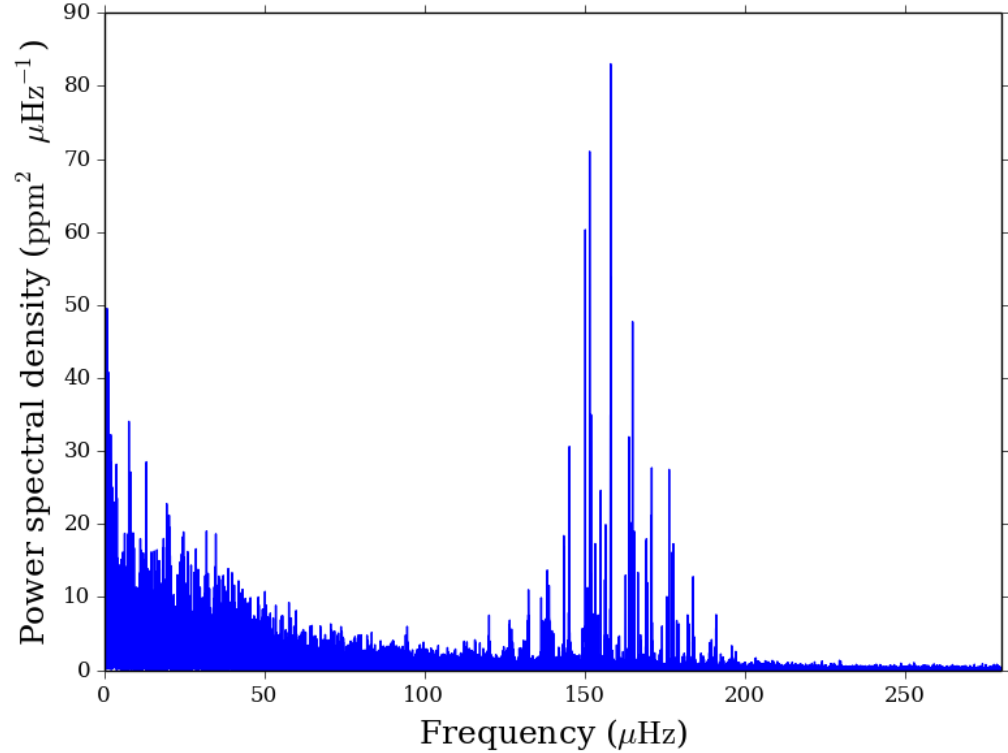
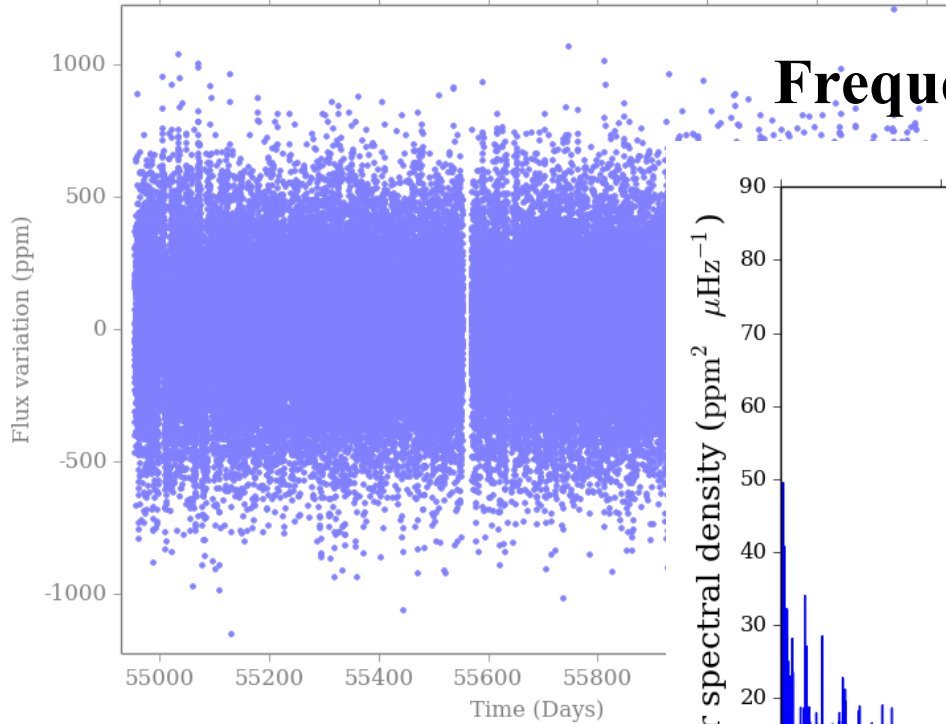


Time domain astronomy





Frequency domain astronomy!



Sun-like stars



Solar type	Solar analog	Solar twin
K2 through to F8	5200 to 6300 K	5720 to 5830 K
Main sequence	Main sequence and no close companion	MS, 3.5 to 5.6 Gyr, and no stellar companion
Any metallicity	Solar +/- 0.3 dex	Solar +/- 0.05 dex
A lot of stars	>30 within 50 ly e.g., Alpha Cen A (& B)	A handful e.g., 18 Sco

Solar-like oscillators

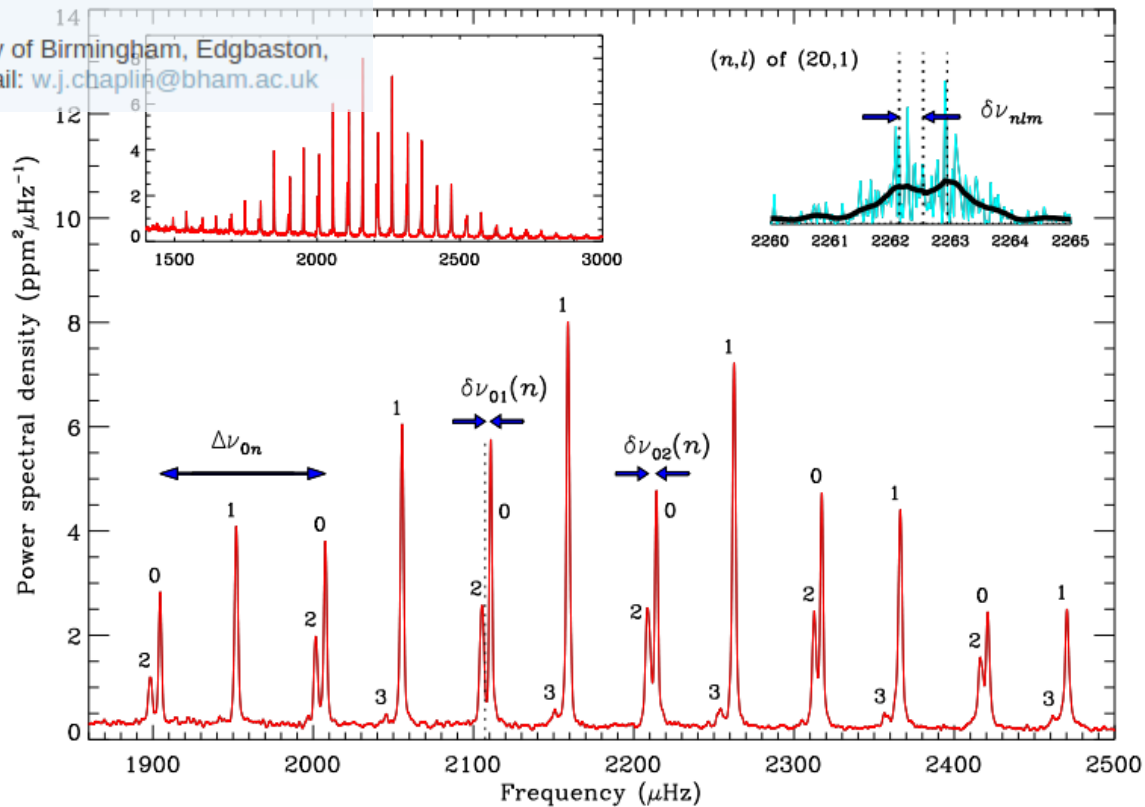


Evolved Sun-like stars	Solar type	Solar analog	Solar twin	The Sun
Cooler	K2 through to F8	5200 to 6300 K	5720 to 5830 K	5777 K
Sub giant Red giant	Main sequence	Main sequence	MS, 3.5 to 5.6 Gyr	4.5 Gyr
Any	Any metallicity	Solar +/- 0.3 dex	Solar +/- 0.05 dex	Solar
Many many detectable	A lot	>30 within 50 ly e.g., Alpha Cen A (& B)	A handful e.g., 18 Sco	Just the one!

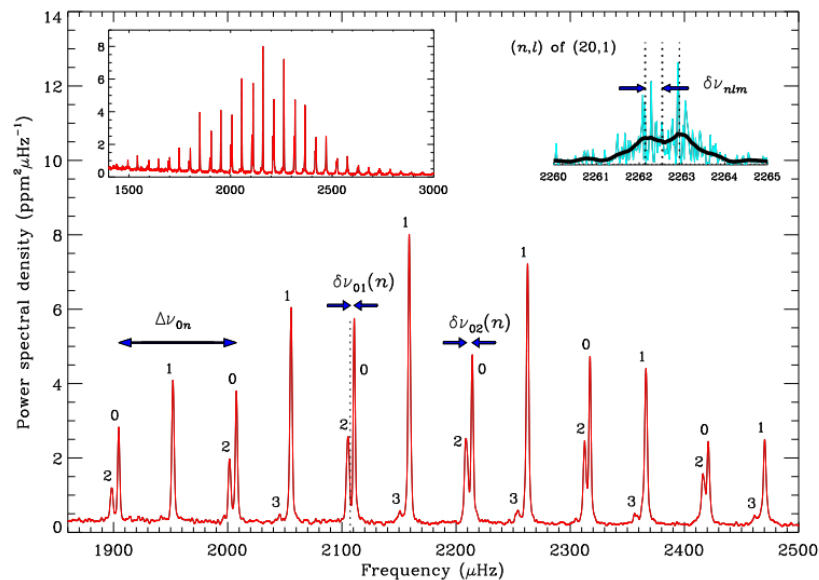
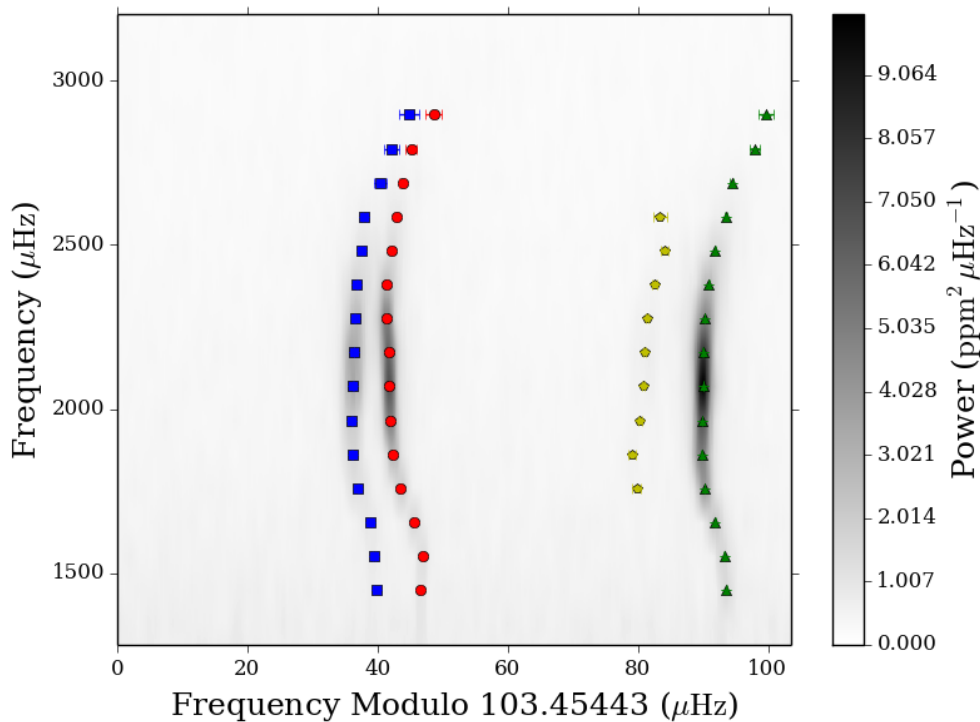


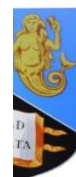
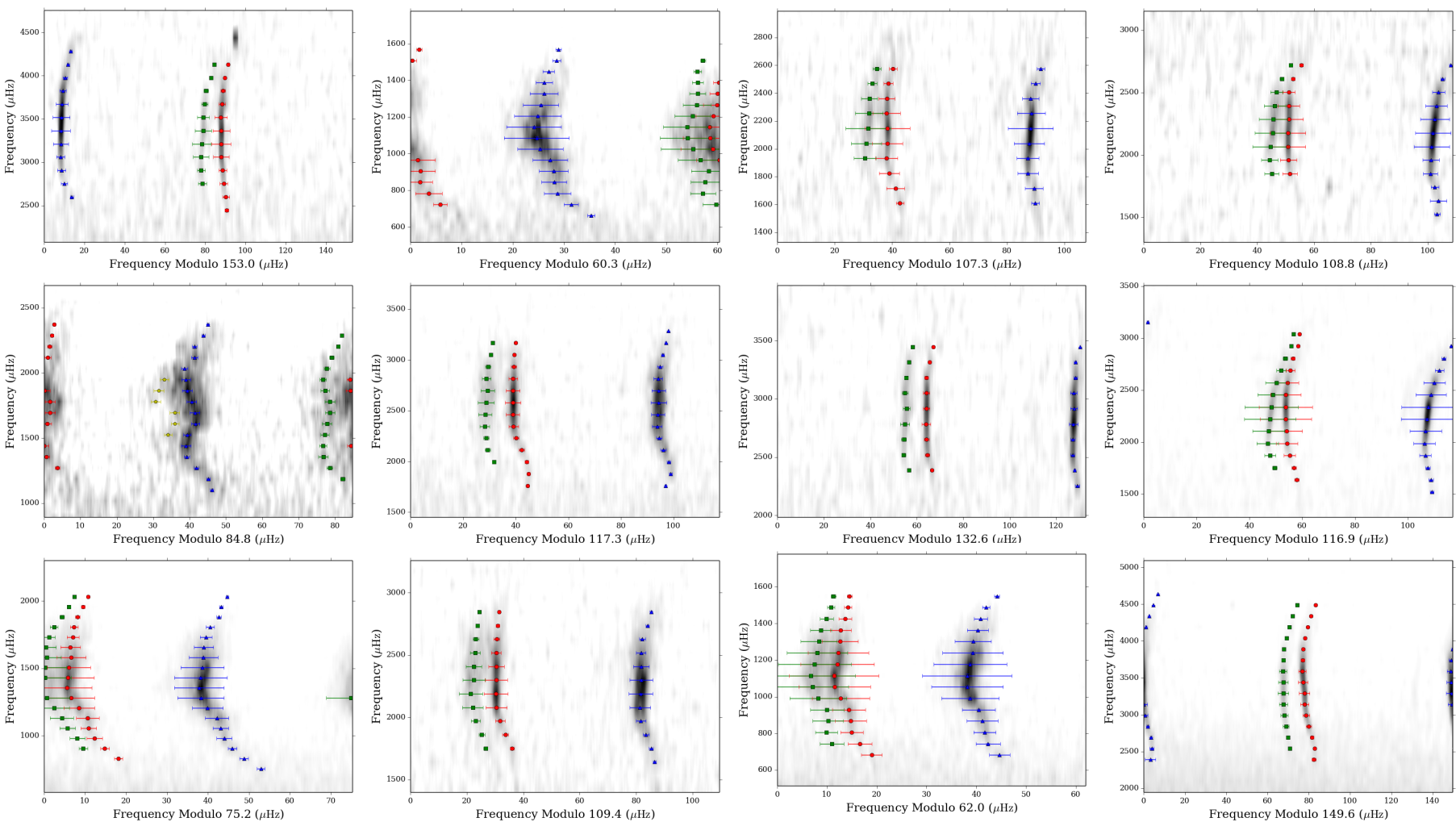
William J. Chaplin and Andrea Miglio

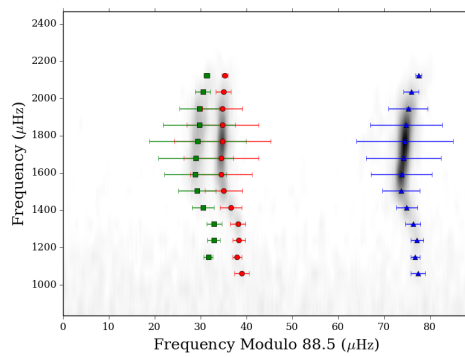
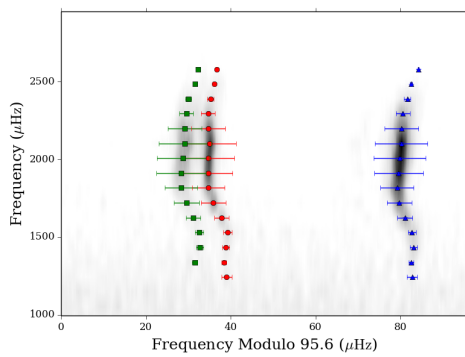
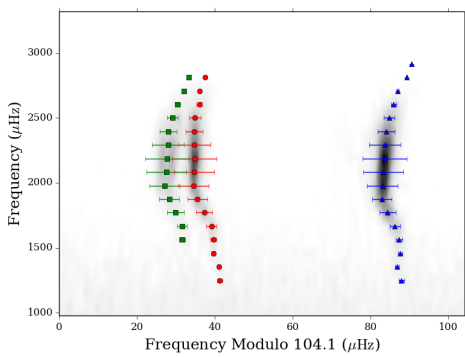
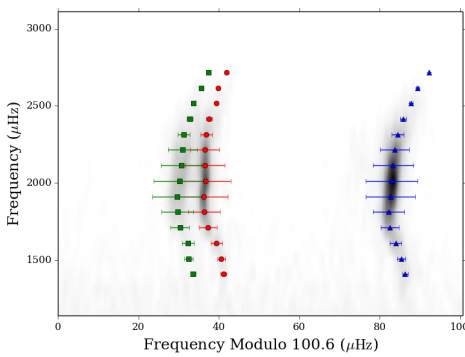
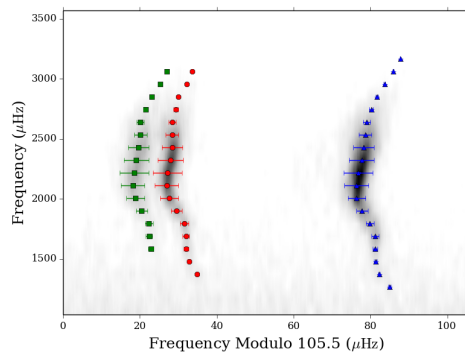
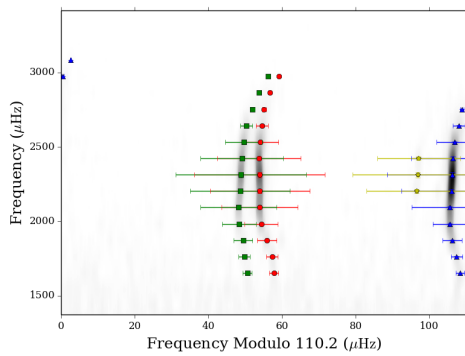
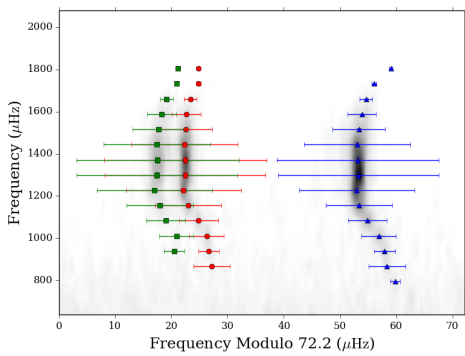
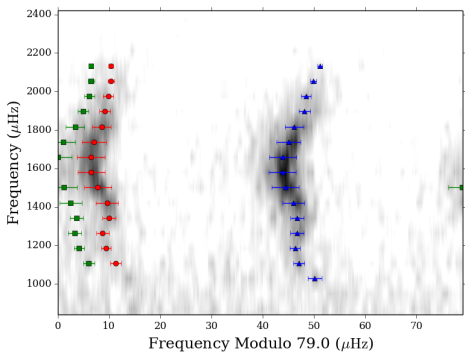
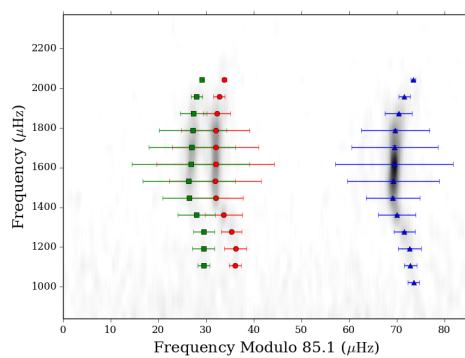
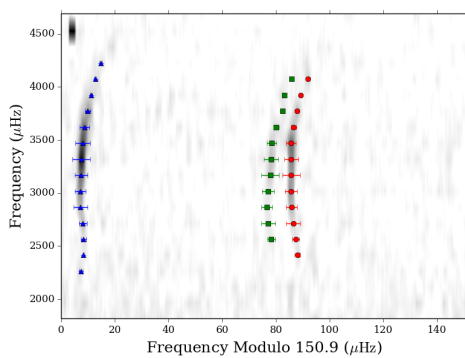
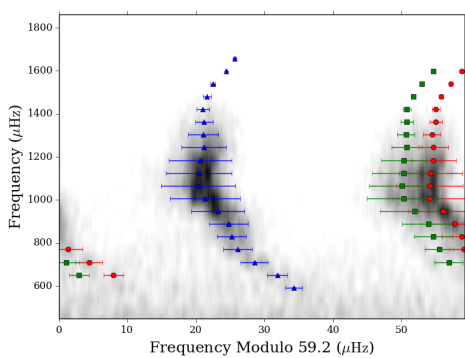
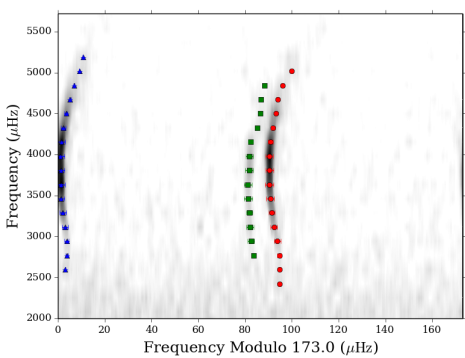
School of Physics and Astronomy, University of Birmingham, Edgbaston,
Birmingham, B15 2TT, United Kingdom; email: w.j.chaplin@bham.ac.uk

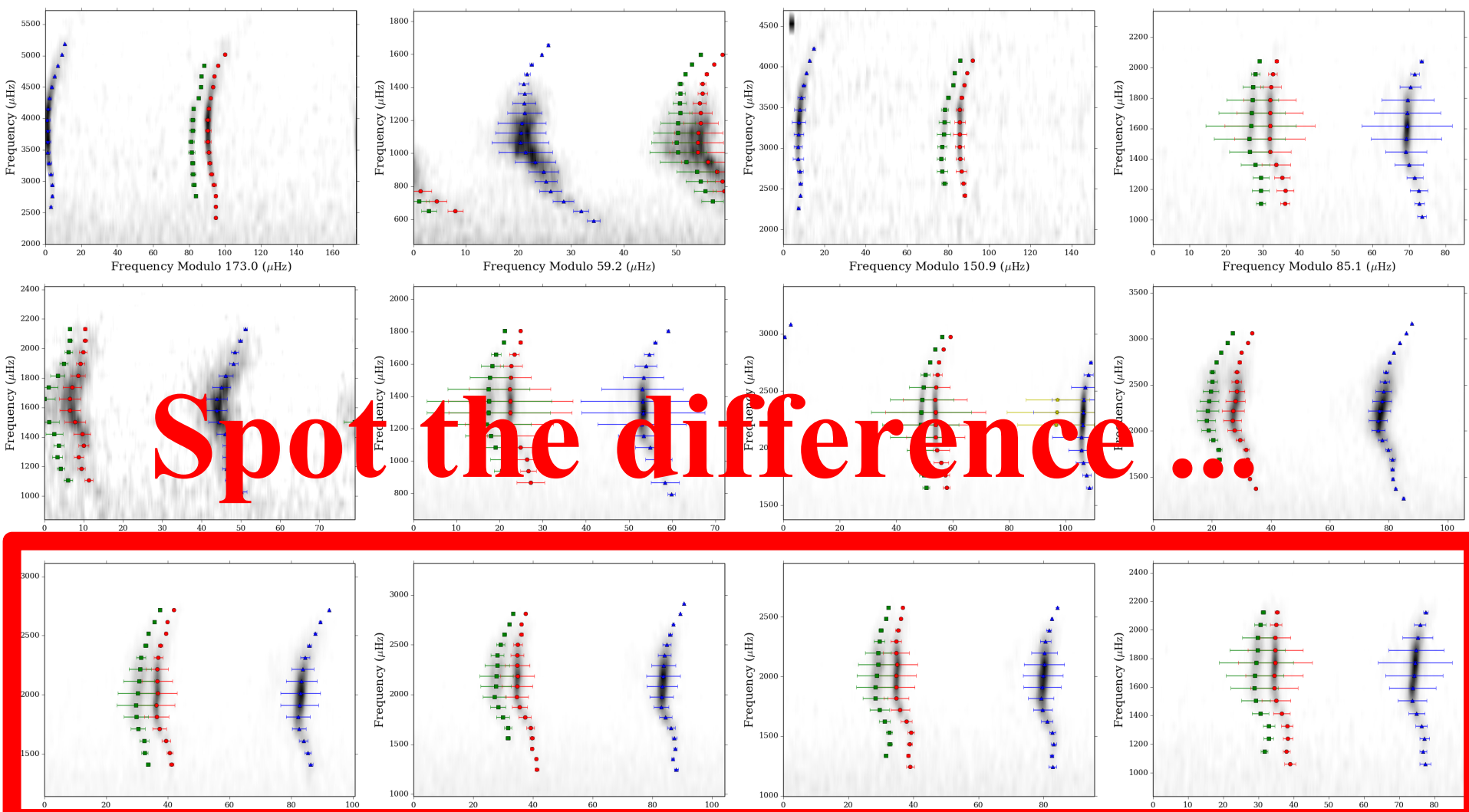


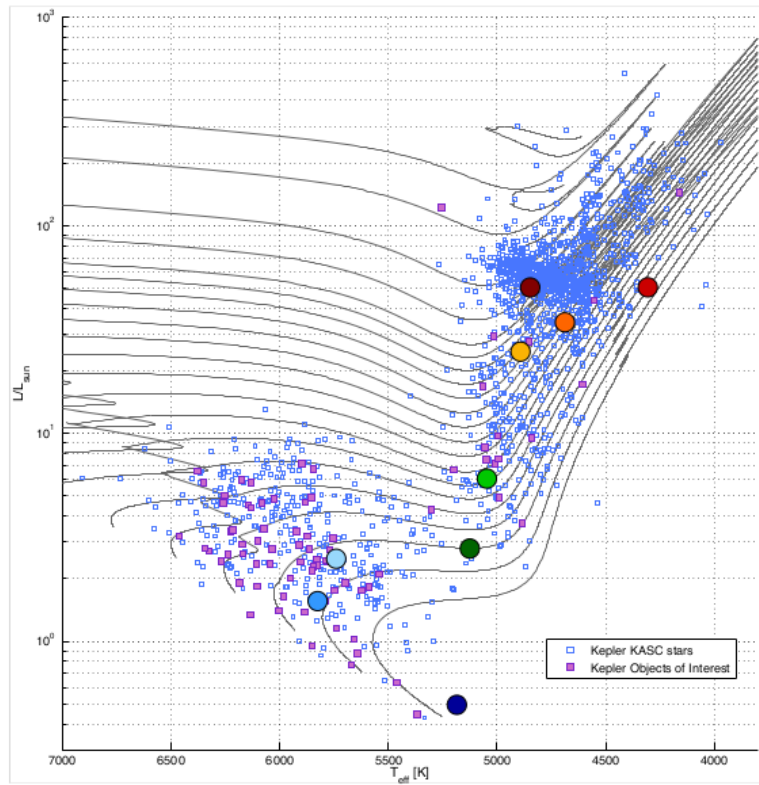
Sun-like MS stars - echelle diagram





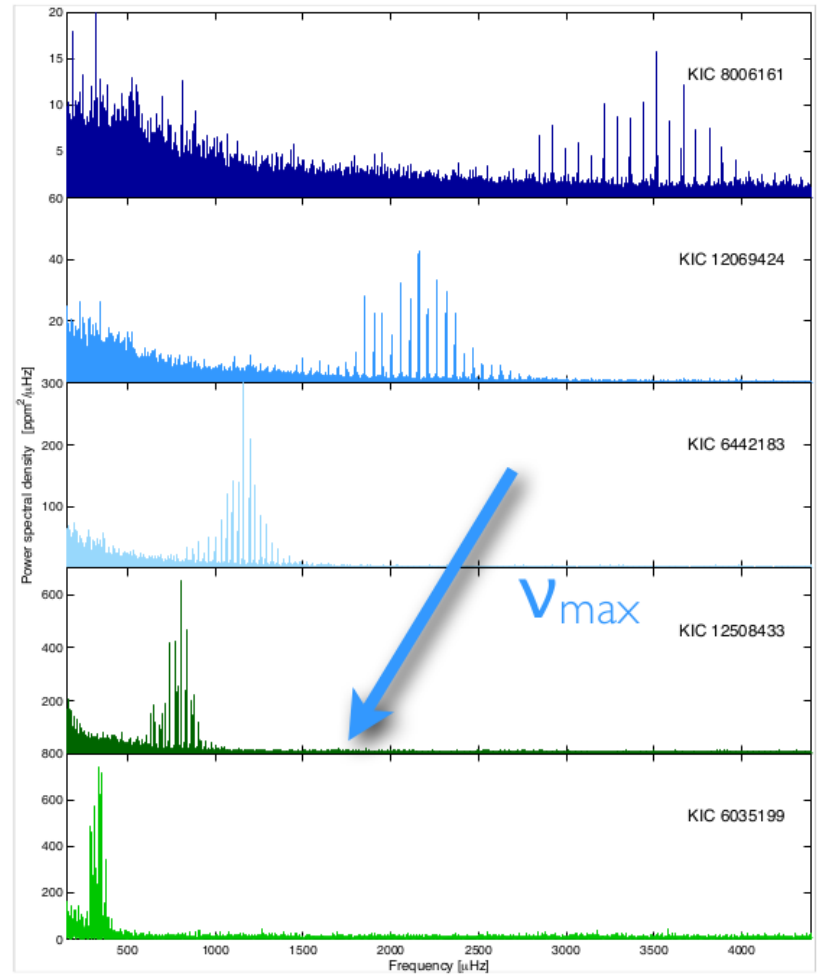
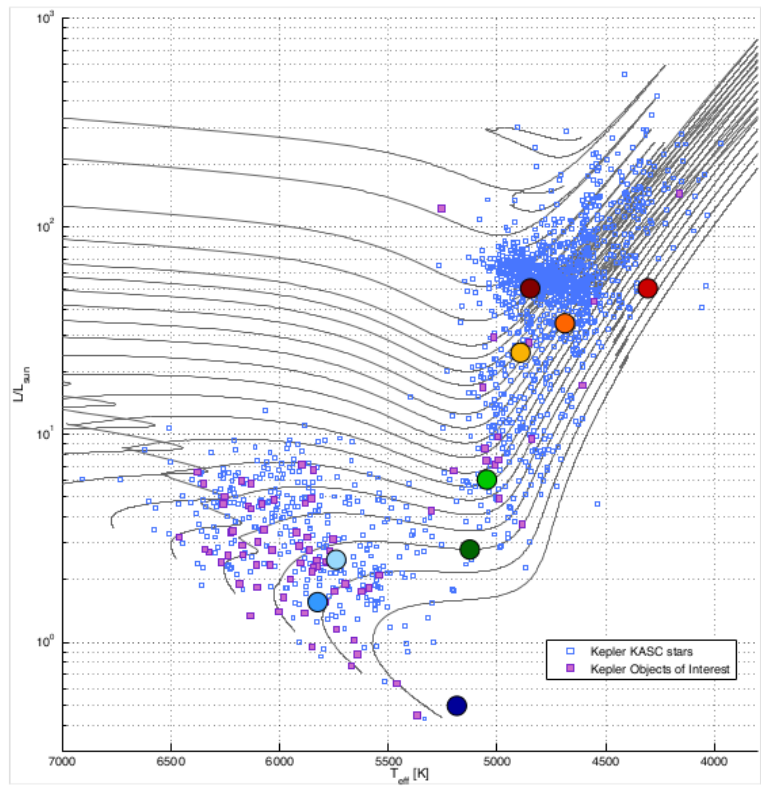




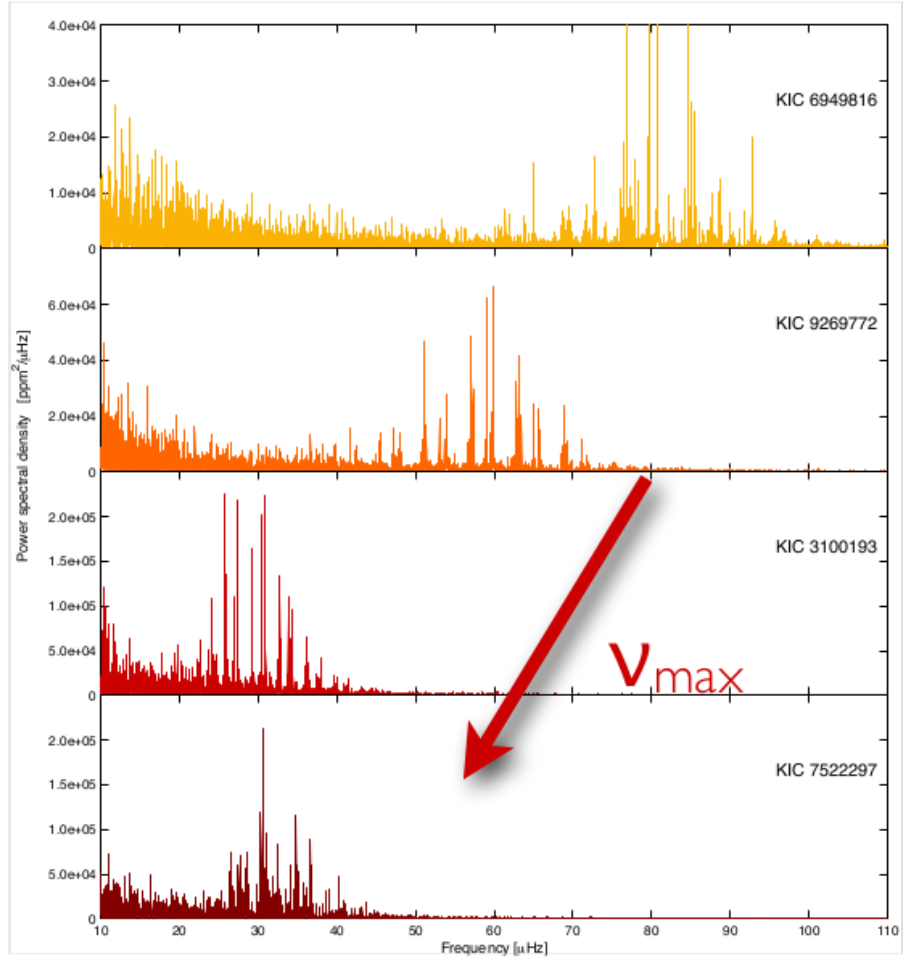
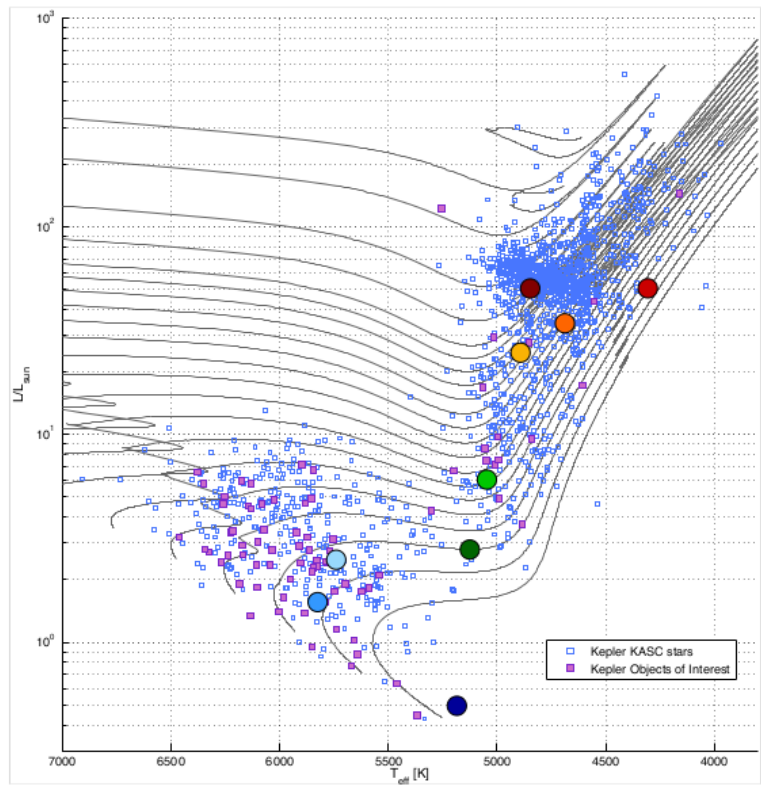


Chaplin & Miglio, ARAA, 2013

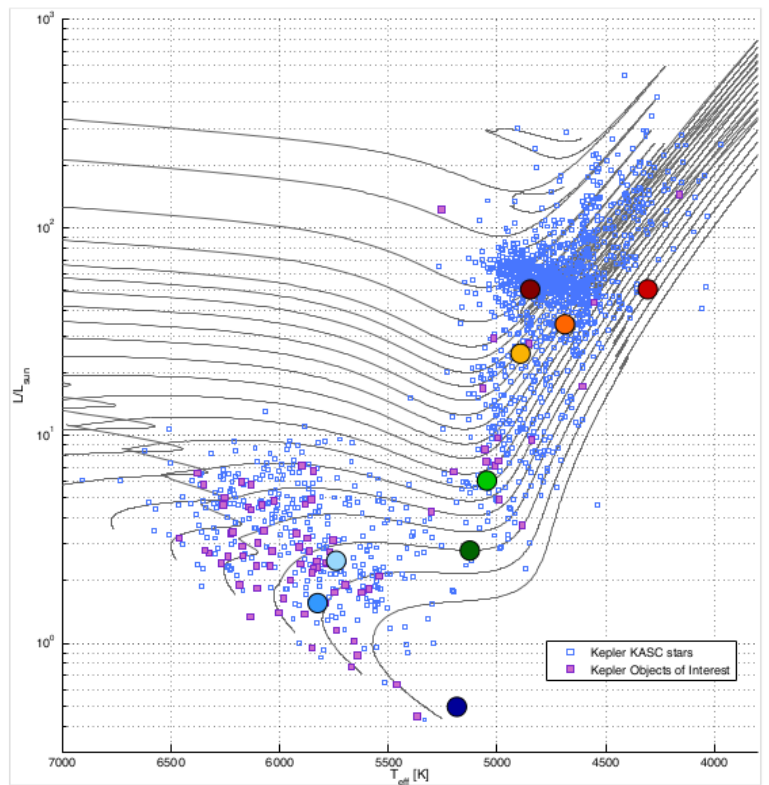
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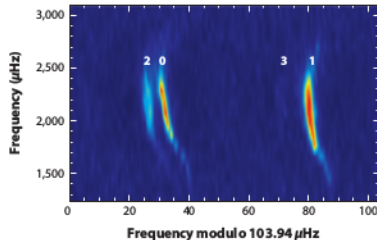
Chaplin & Miglio, ARAA, 2013



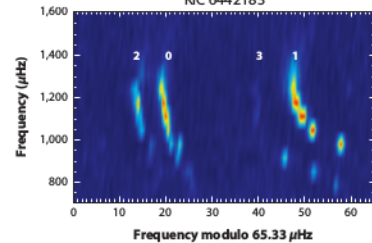
Chaplin & Miglio, ARAA, 2013



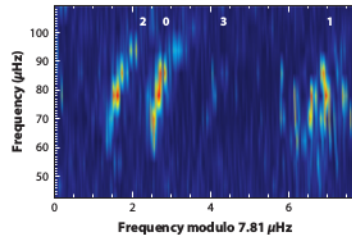
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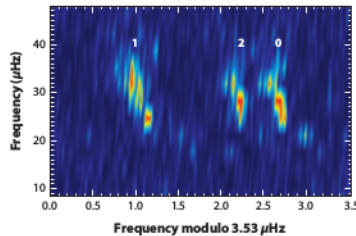
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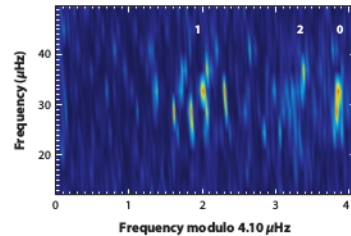
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Chaplin & Miglio, ARAA, 2013

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Observations and constraint







Evolved Sun-like stars	Solar type	Solar analog	Solar twin	The Sun
Cooler	K2 through to F8	5200 to 6300 K	5720 to 5830 K	5777 K
Sub giant Red giant	Main sequence	Main sequence	MS, 3.5 to 5.6 Gyr	4.5 Gyr
Any	Any metallicity	Solar +/- 0.3 dex	Solar +/- 0.1 dex	Solar
Many many detectable	A lot	>30 within 50 ly e.g., Alpha Cen A (& B)	A handful e.g., 18 Sco	Just the one!

Progress

Observations and constraint



Observable	Solar type red giant	Solar type subgiant	Solar type main sequence	The Sun
Average frequency spacings + numax				
Period spacing				
Rotation				
Individual frequencies				

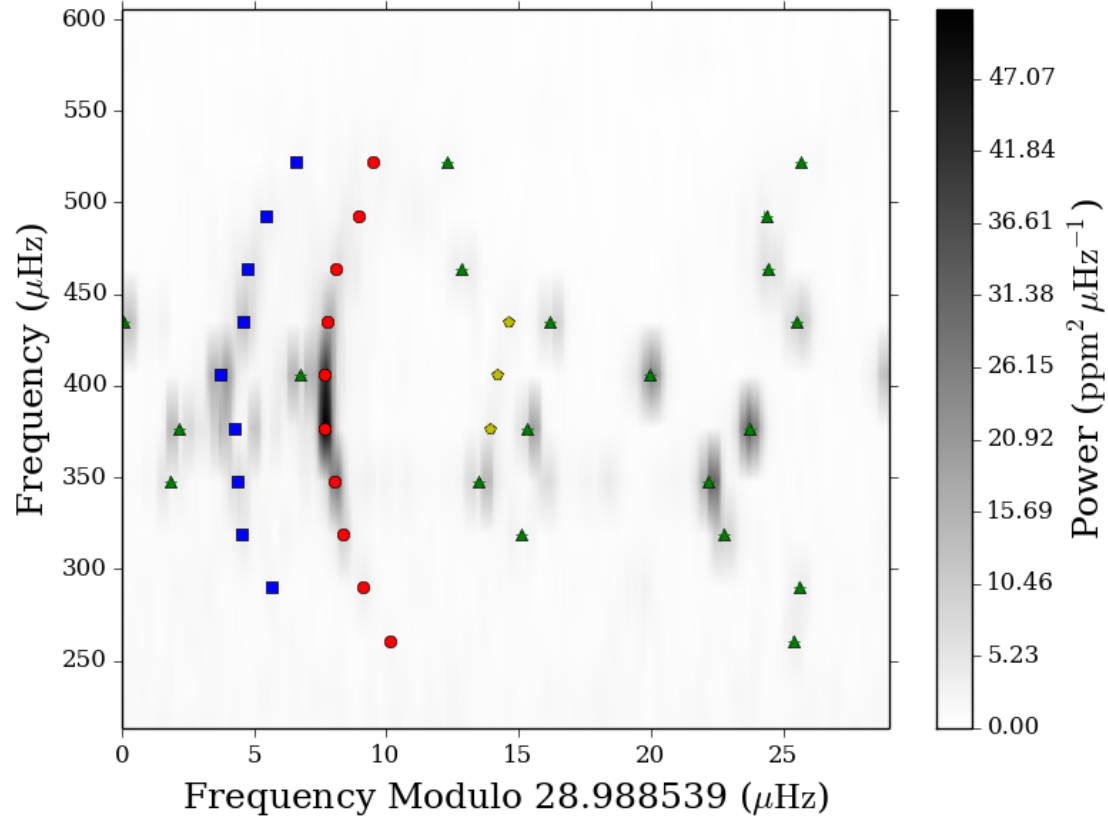
Sun-like evolved stars



**KIC 7341231 -
“Otto”**

**Mixed modes of
oscillation**

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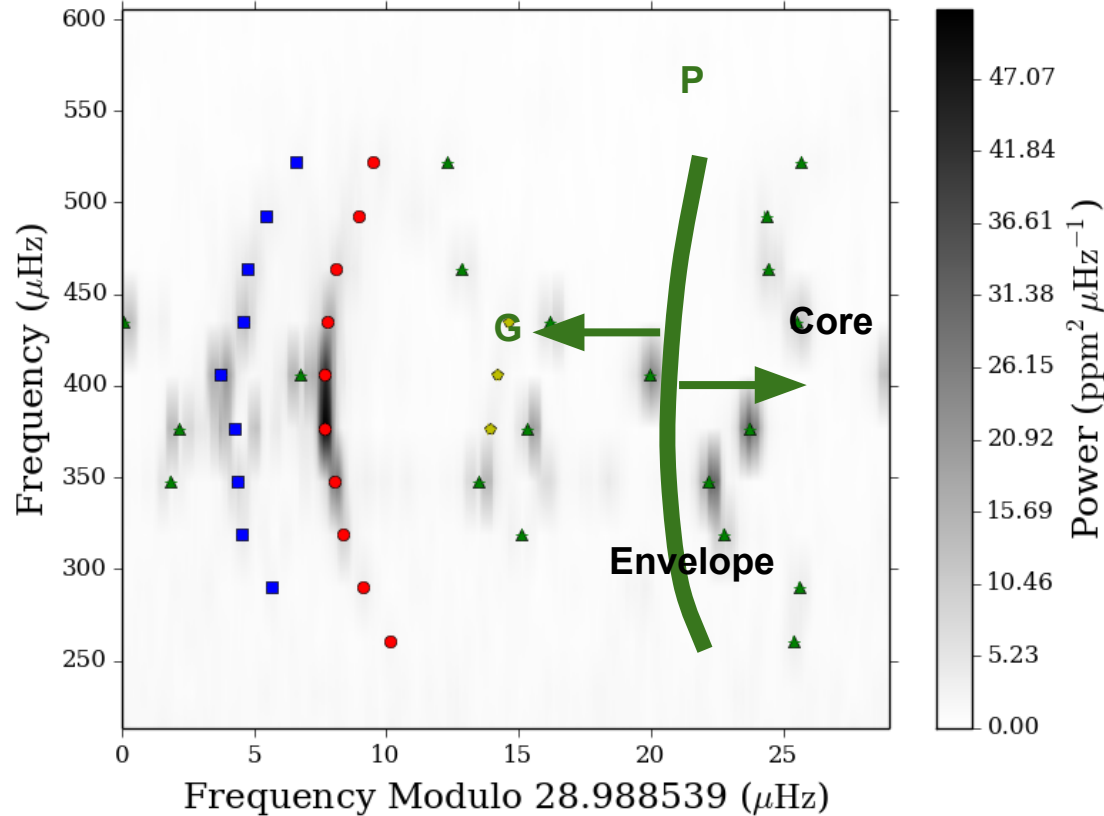
Sun-like evolved stars



**KIC 7341231 -
“Otto”**

**Mixed modes of
oscillation**

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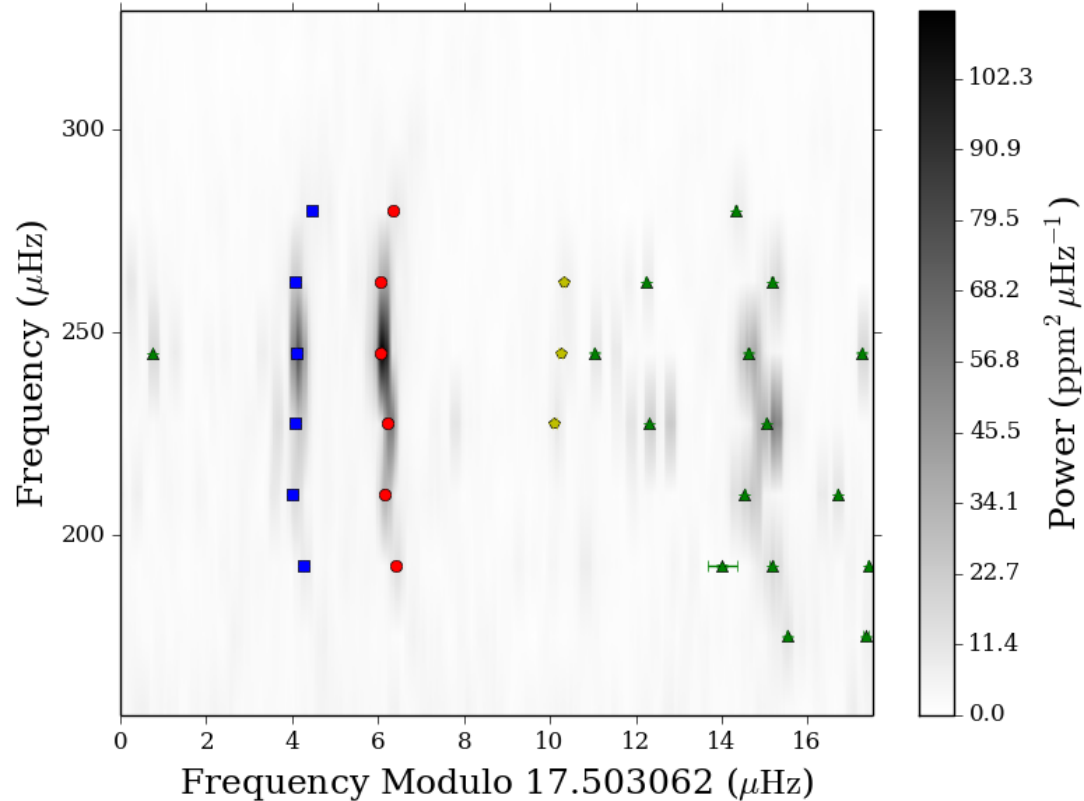


Sun-like red giant branch

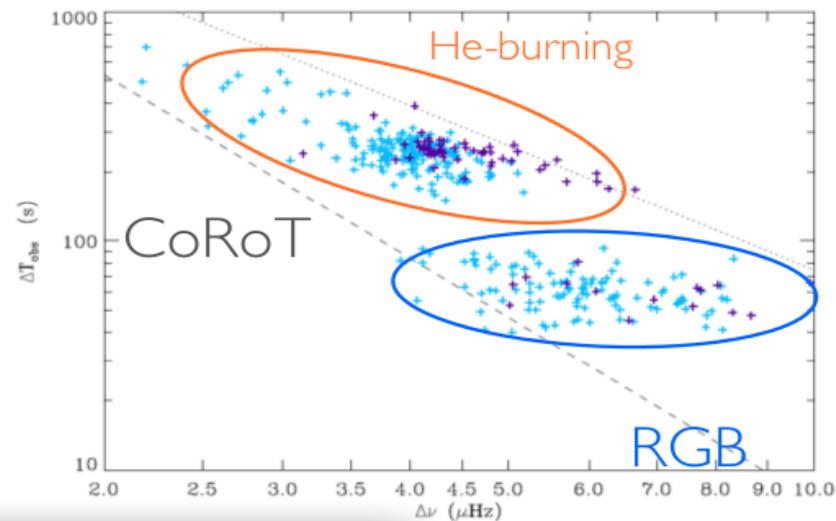
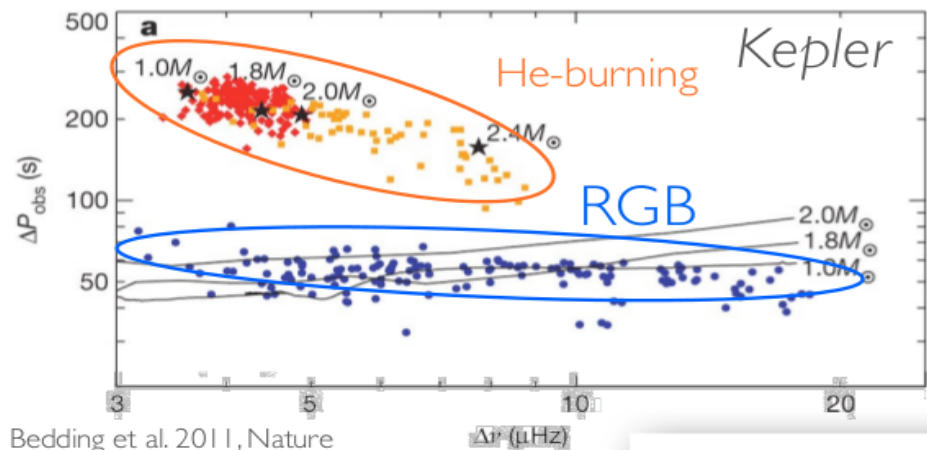


Kepler-56

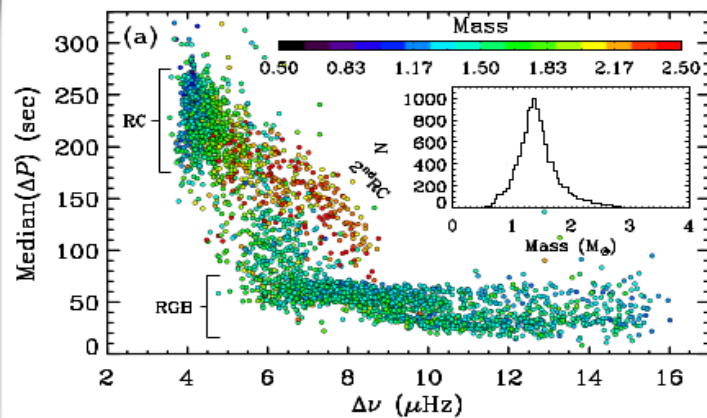
**RGB star with
mixed modes**



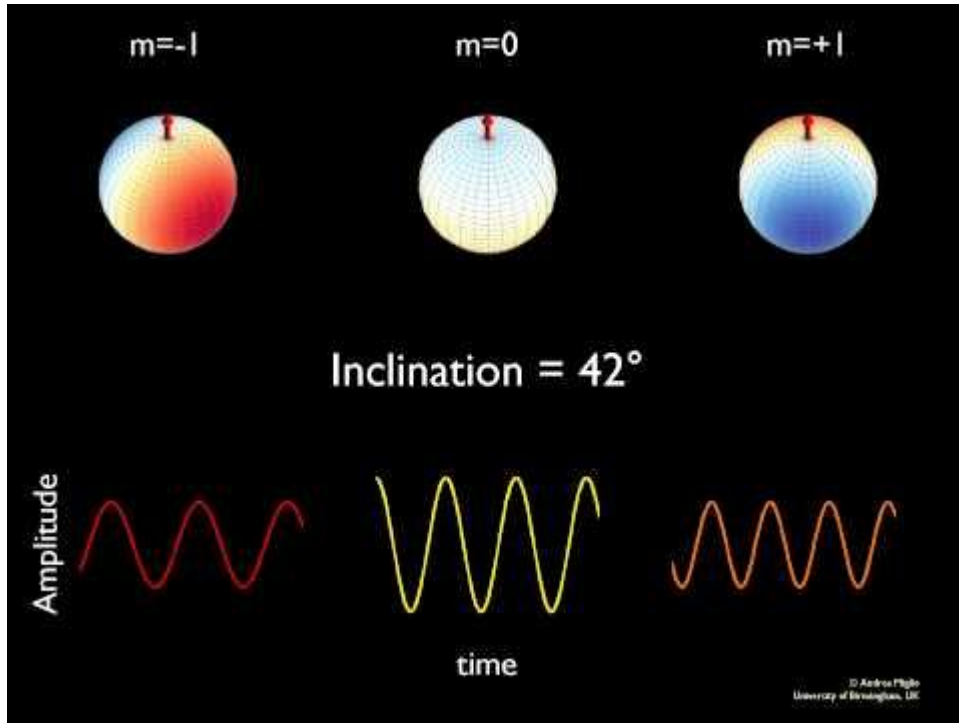
Observations with Kepler and CoRoT:



Mosser et al. 2011, A&A



Rotation



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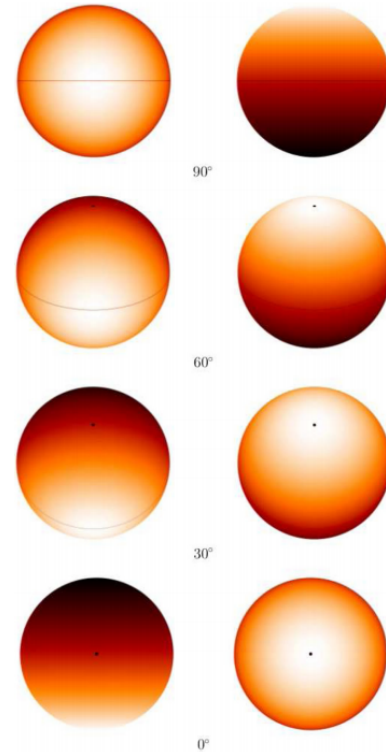


Figure 6. Intensity perturbations for $l = 1$ mode components, at a phase corresponding to extreme displacement of the oscillations. Plotted are patterns for $m = 1$ (left-hand column) and $m = 0$ (right-hand column) modes viewed at different angles, $i_s = 90^\circ$ (top row), 60° (second row), 30° (third row), and 0° (bottom row). The filled circles mark the pole of the rotation axis and the lines the stellar equator.

Internal rotation



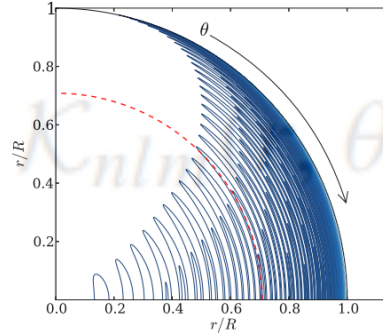
$$\delta v_{nlm} = \int_0^\pi \int_0^R \mathcal{K}_{nlm}(r, \theta) \mathcal{N}(r, \theta) r dr d\theta.$$

Internal rotation

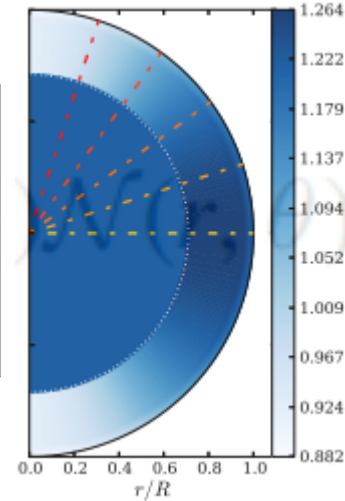


$$\delta v_{nlm} = \int_0^\pi \int_0^R$$

Frequency splitting



Kernel



Rotation profile

$$r dr d\theta.$$

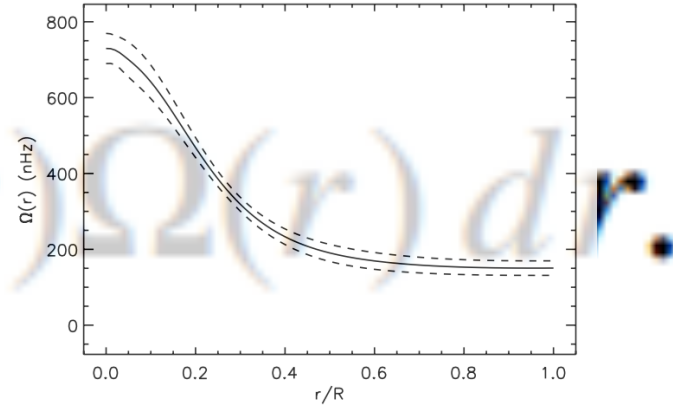
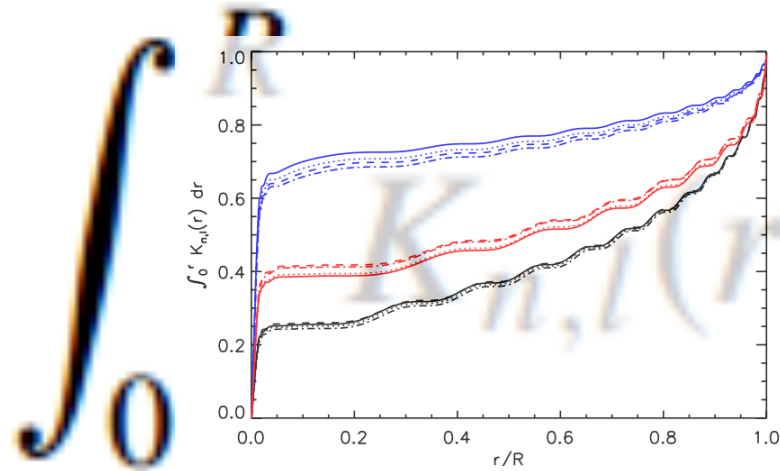
Lund+ 2014

Internal rotation - 1D

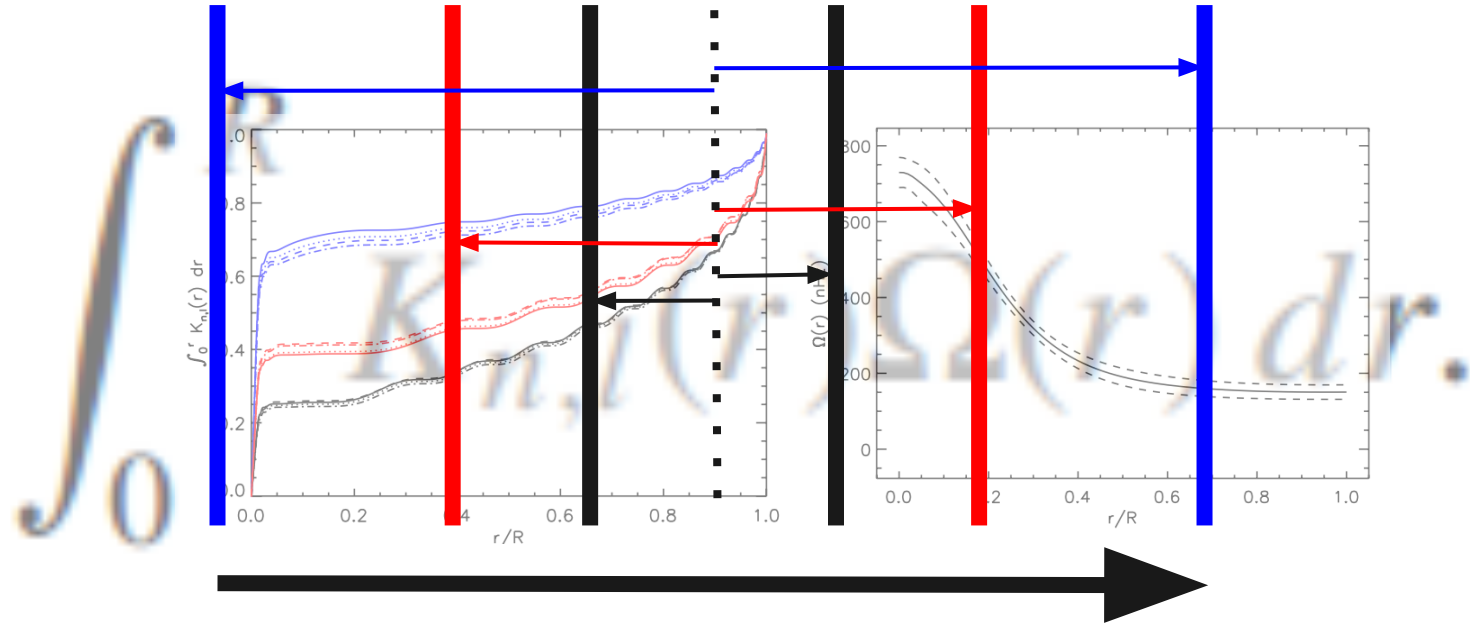


$$\delta v_{n,l} = (2\pi)^{-1} \int_0^R K_{n,l}(r) \Omega(r) dr.$$

Internal rotation - 1D



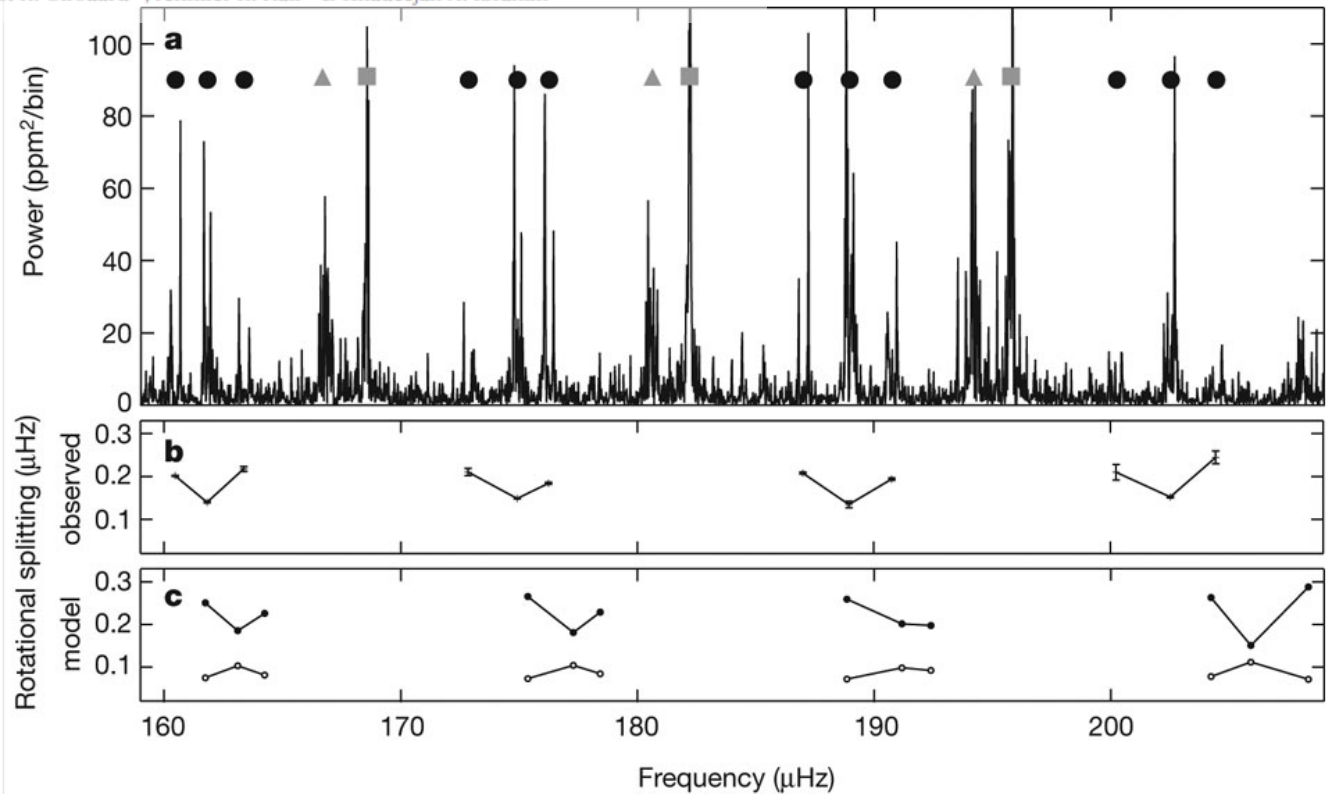
Rotation - 1D



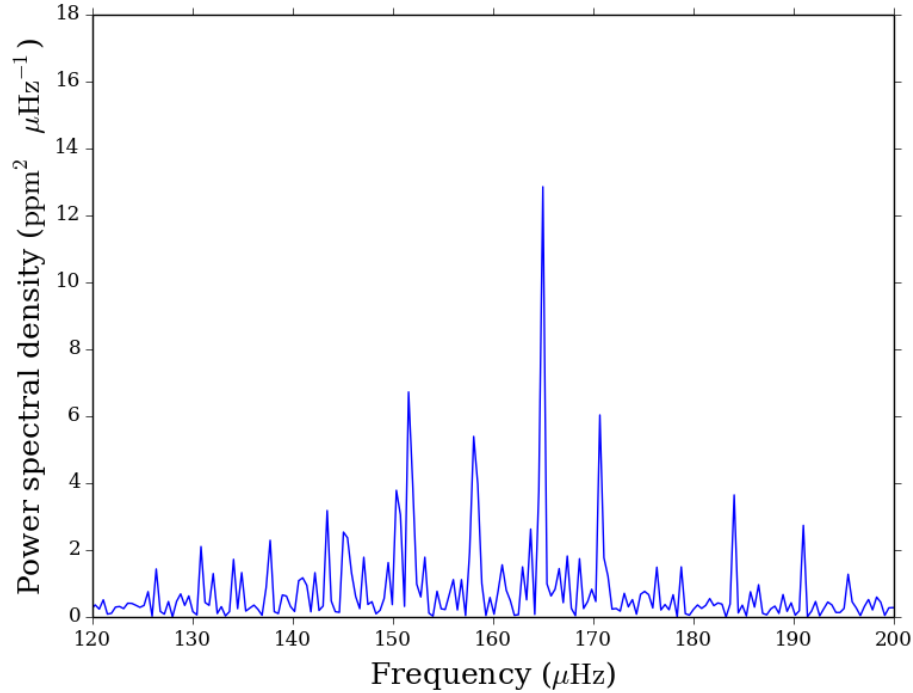


Fast core rotation in red-giant stars as revealed by gravity-dominated mixed modes

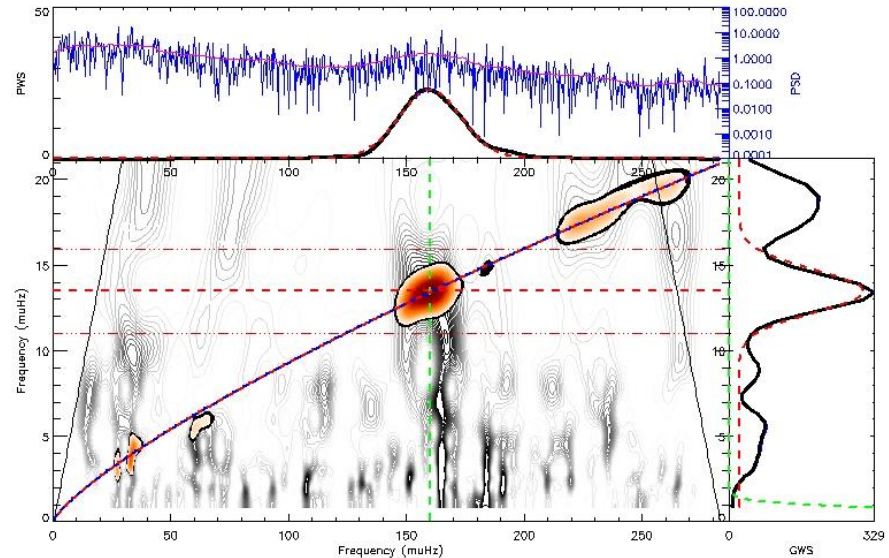
Paul G. Beck¹, Josefina Montalbán², Thomas Kallinger^{1,3}, Joris De Ridder¹, Conny Aerts^{1,4}, Rafael A. García⁵, Saskia Hekker^{6,7}, Marc-Antoine Dupret², Benoit Mosser⁸, Patrick Eggenberger⁹, Dennis Stello¹⁰, Yvonne Elsworth⁷, Søren Frandsen¹¹, Fabien Carrier¹, Michel Hillen¹, Michael Gruberbauer¹², Jørgen Christensen-Dalsgaard¹¹, Andrea Miglio⁷, Marica Valentini², Timothy R. Bedding¹⁰, Hans Kjeldsen¹¹, Forrest R. Girouard^{1,3}, Jennifer R. Hall^{1,3} & Khadeejah A. Ibrahim^{1,3}



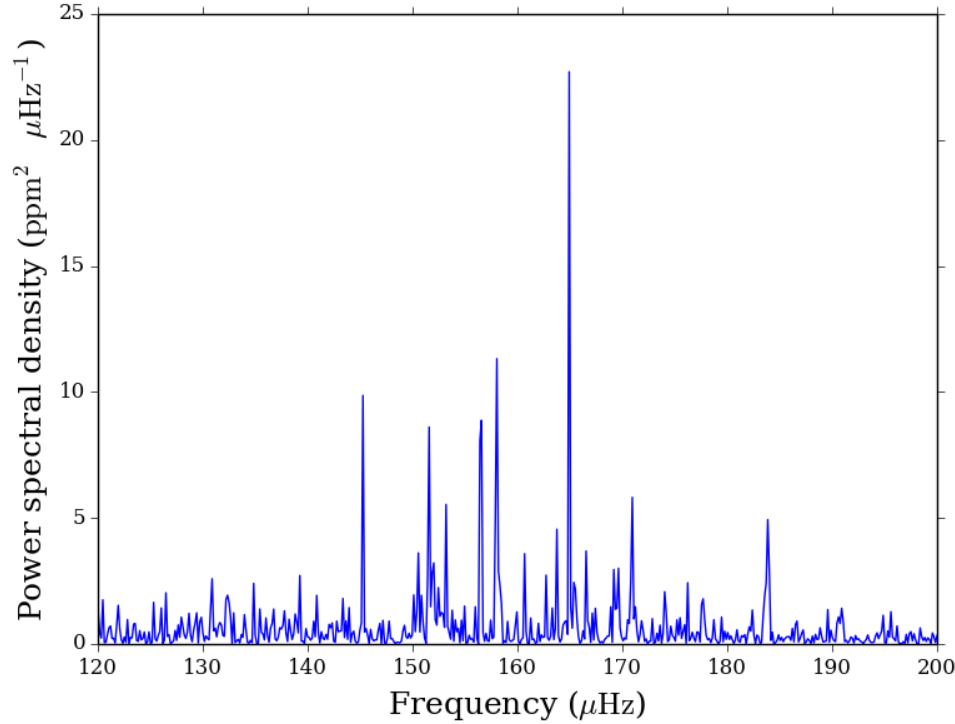
What happens when you only have 27 days of data? (e.g. TESS)



$d\nu = 13 \pm 1 \mu\text{Hz}$
 $\nu_{\text{max}} = 160 \mu\text{Hz}$
period spacing = ?
rotation = ?
Individual frequencies - for $l=0$



What happens when you only have 70 days of data? (e.g. K2)



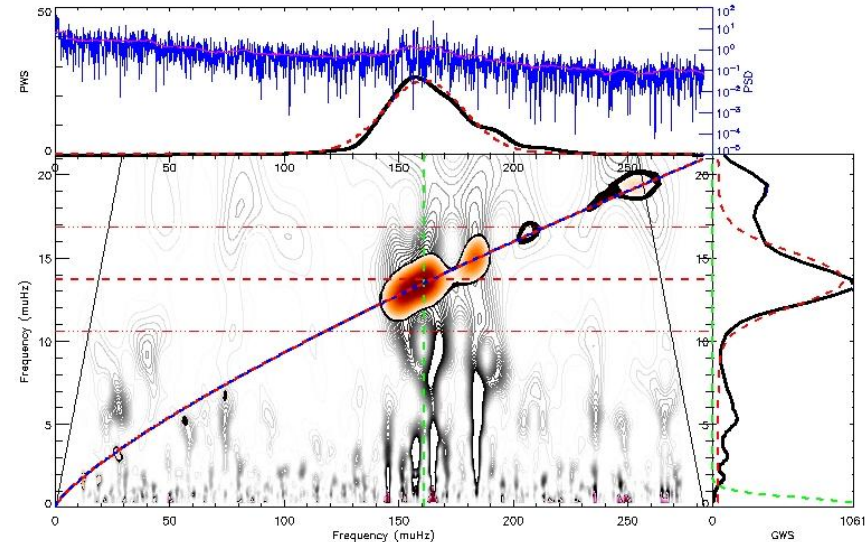
$d\nu = 13.3 \pm 0.7 \mu\text{Hz}$

$\nu_{\text{max}} = 161.2 \mu\text{Hz}$

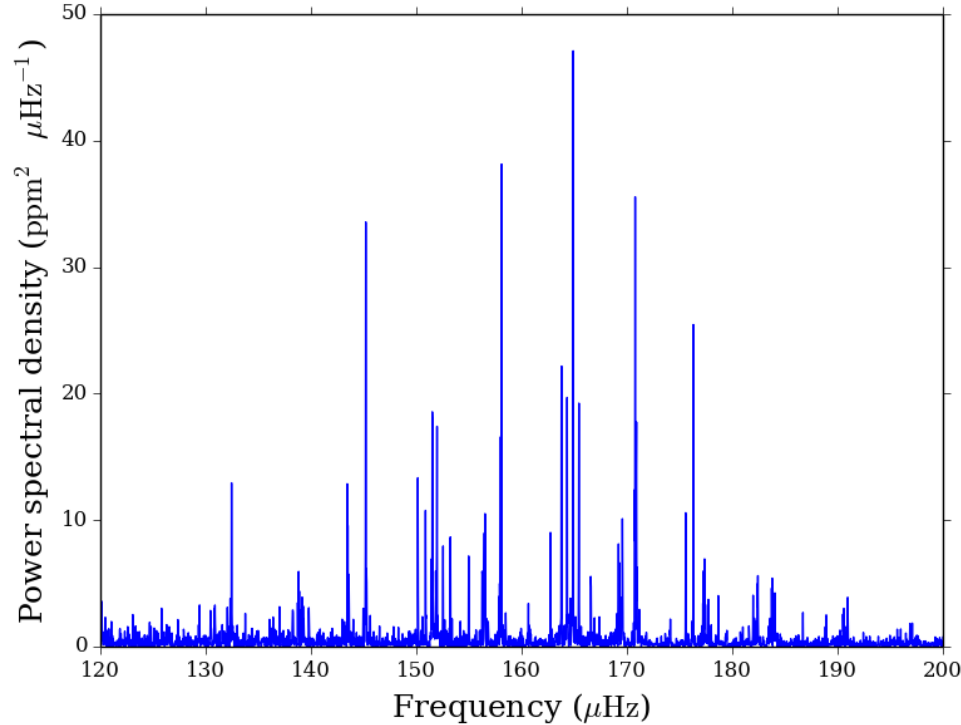
period spacing = ?

rotation = ?

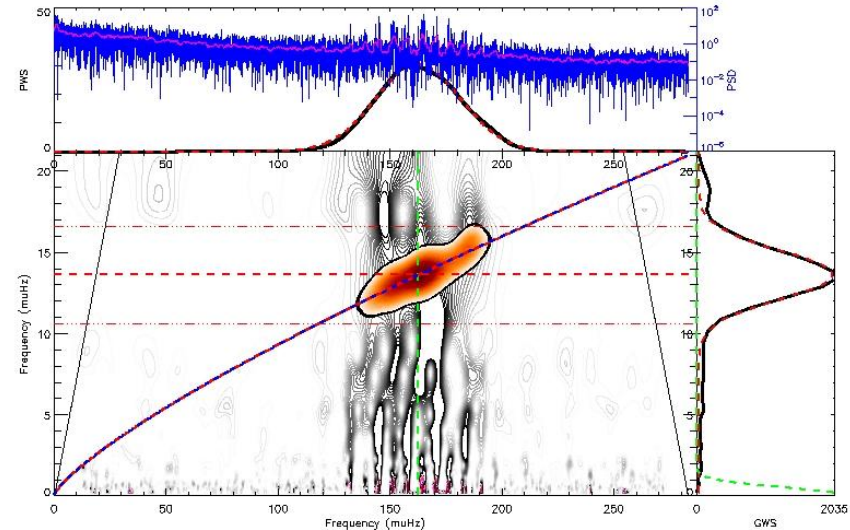
Individual frequencies - for $l=0,2$



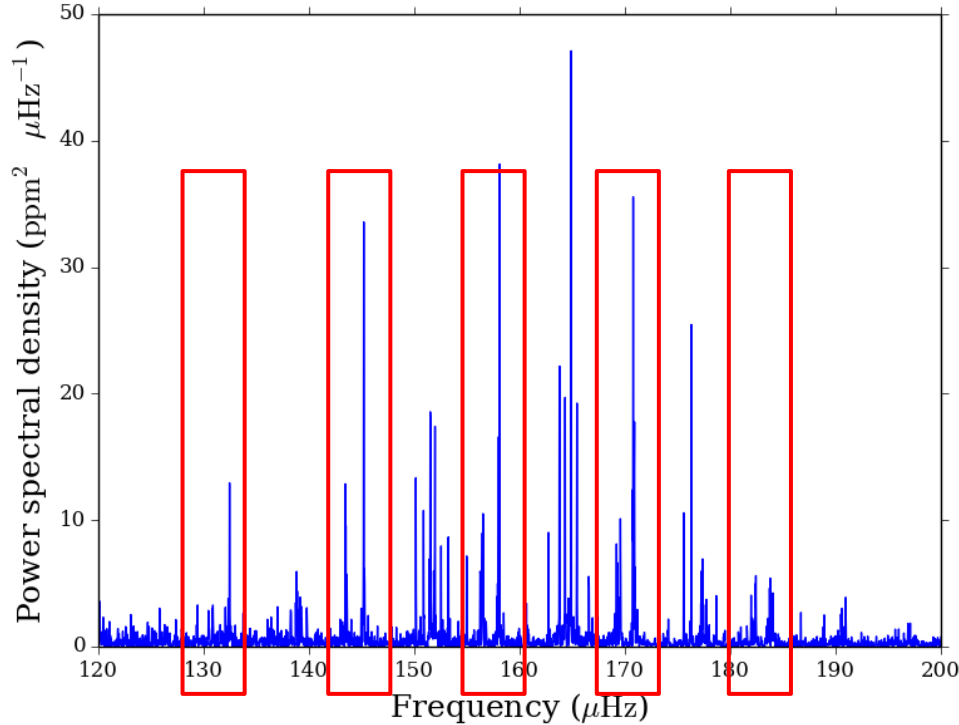
What happens when you only have 351 days of data? (e.g. Best TESS)



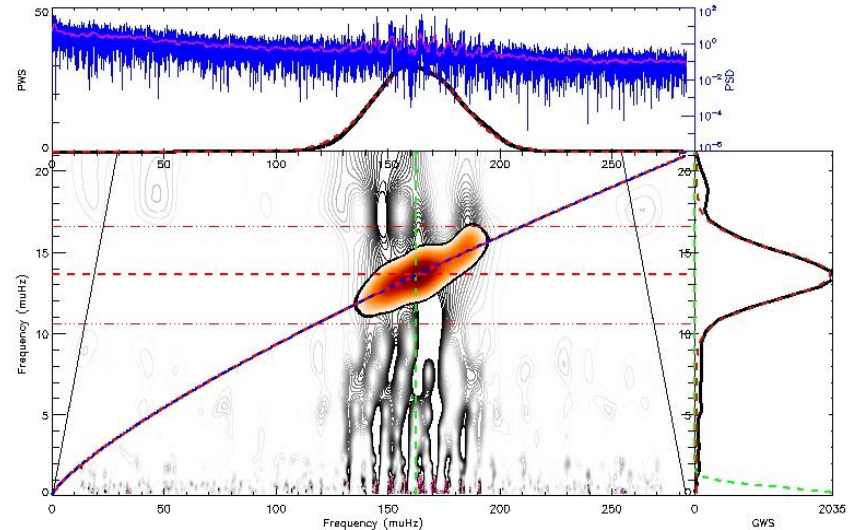
$d\nu = 12.9 \pm 0.2 \mu\text{Hz}$
 $\nu_{\text{max}} = 162.6 \mu\text{Hz}$
period spacing = $80.45 \pm 0.04 \text{ s}$
rotation $\langle \Omega_{\text{Core}} \rangle = 0.43 \pm 0.03 \mu\text{Hz}$
Individual frequencies - for $l=0,2,1,(3)$



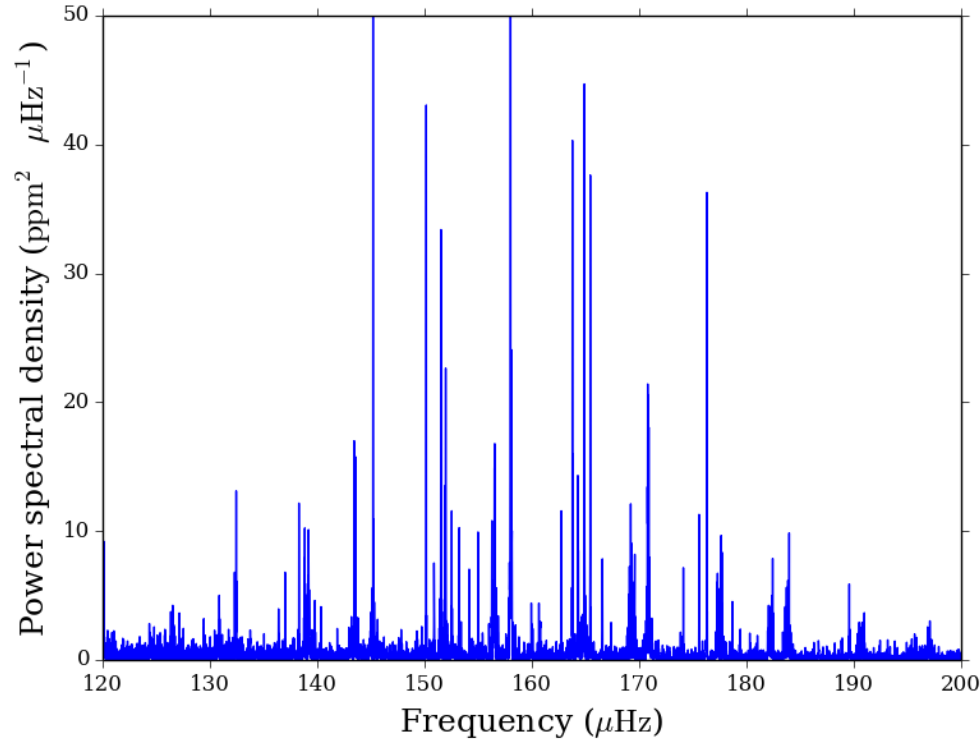
What happens when you only have 351 days of data? (e.g. Best TESS)



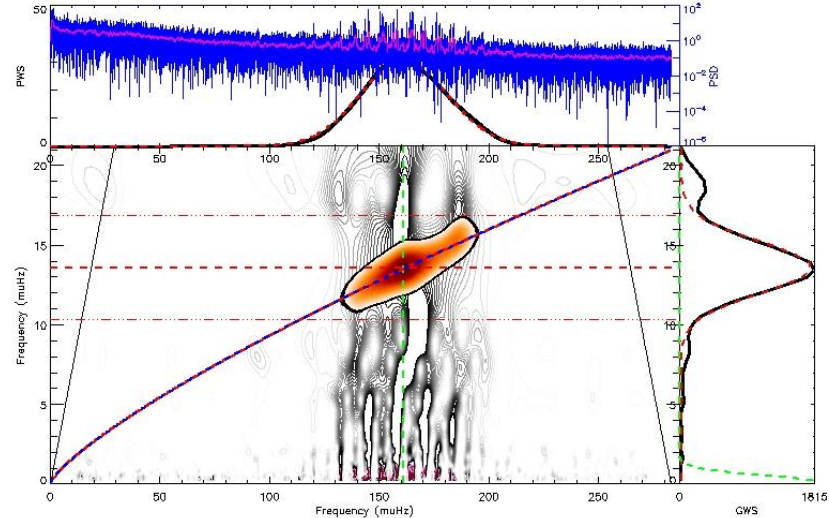
$d\nu = 12.9 \pm 0.2 \mu\text{Hz}$
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Individual frequencies - for $l=0,2,1,(3)$



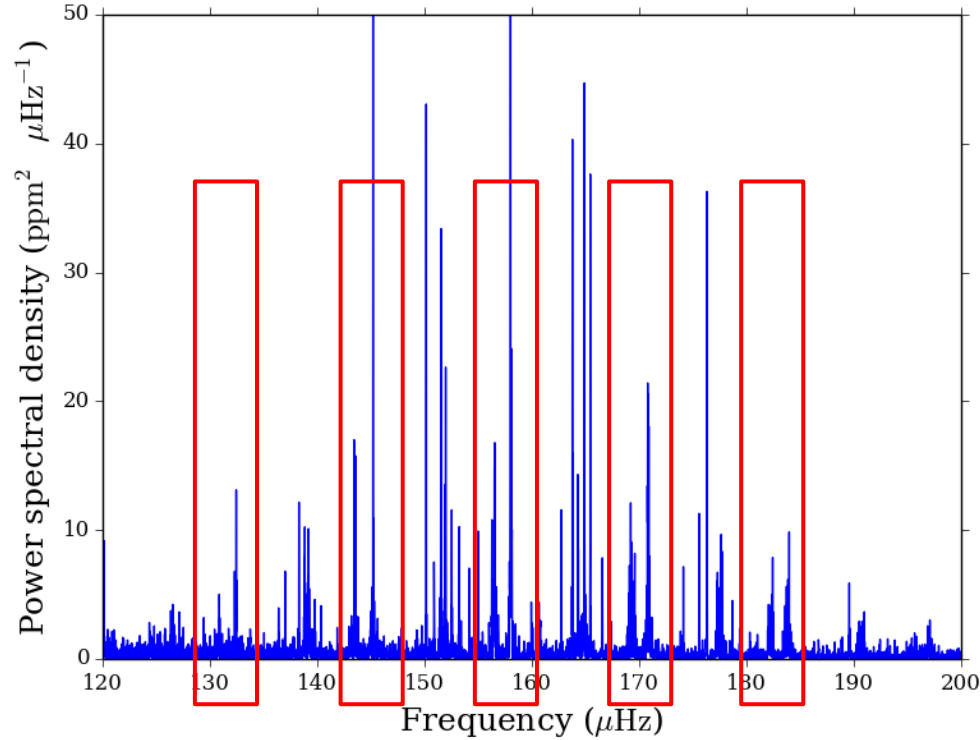
What happens when you only have 730 days of data? (e.g. PLATO long)



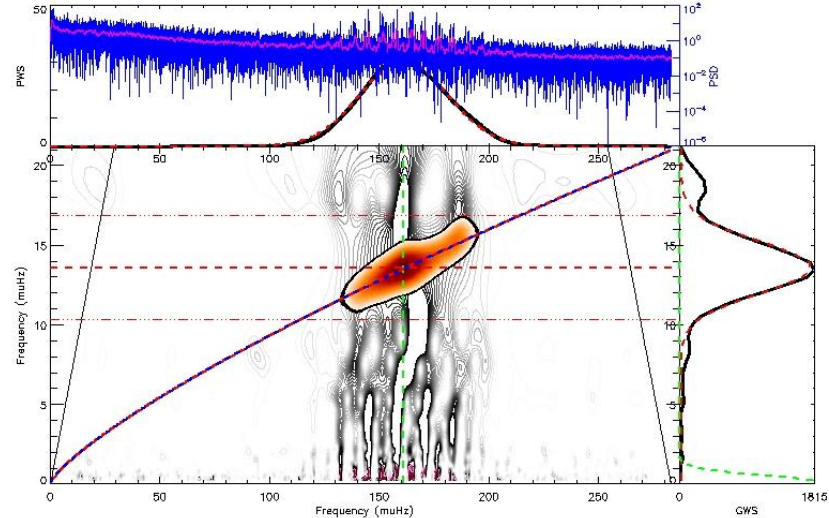
$d\nu = 12.97 \pm 0.17 \mu\text{Hz}$
 $\nu_{\text{max}} = 161.3 \mu\text{Hz}$
period spacing = $80.45 \pm 0.02 \text{ s}$
rotation $\langle \Omega_{\text{Core}} \rangle = 0.44 \pm 0.04 \mu\text{Hz}$
Individual frequencies - for $l=0,2,1,3$



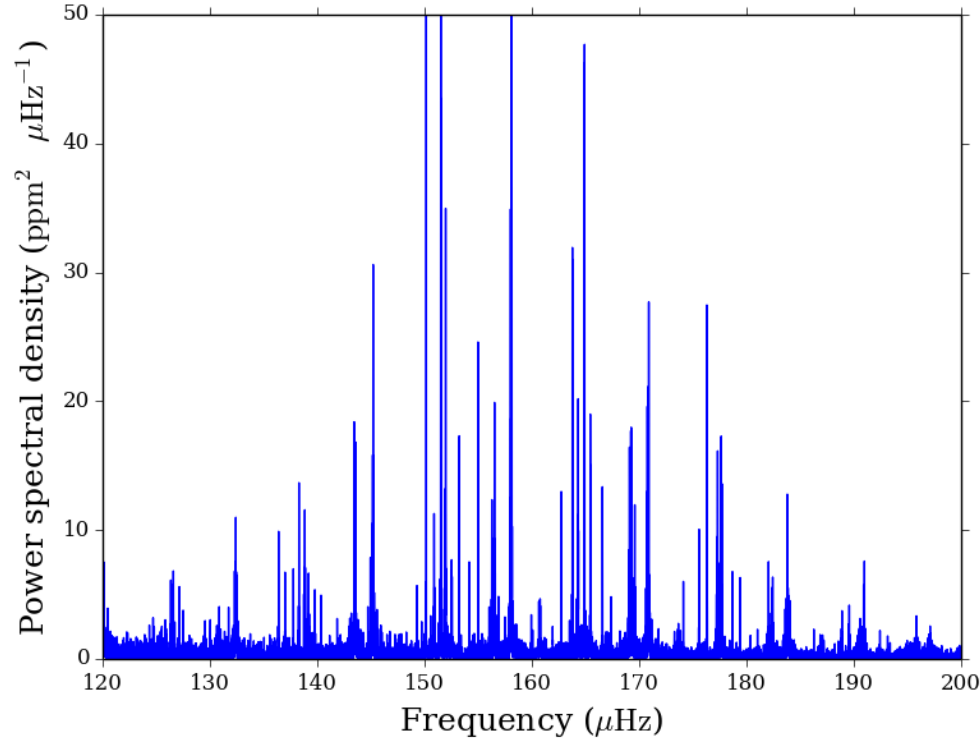
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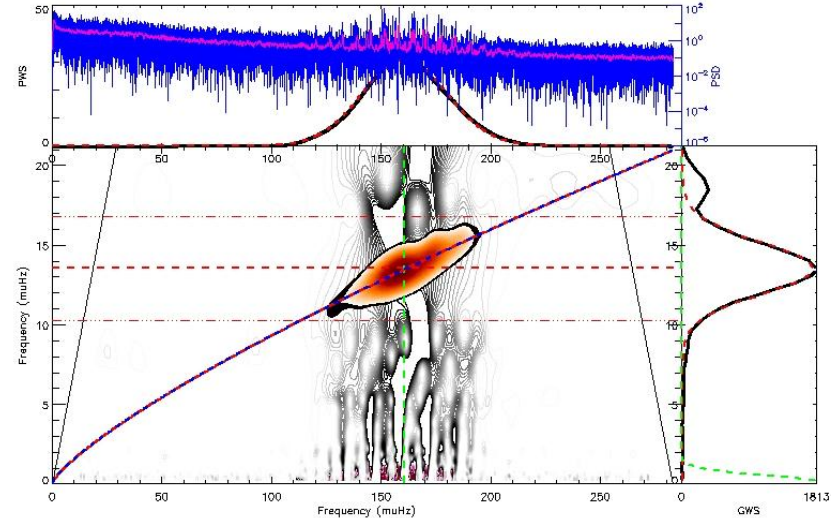
$dnu = 12.97 \pm 0.17 \mu\text{Hz}$
 $numax = 161.3 \mu\text{Hz}$
period spacing = $80.45 \pm 0.02 \text{ s}$
rotation $\langle \Omega_{\text{Core}} \rangle = 0.44 \pm 0.04 \mu\text{Hz}$
Individual frequencies - for $l=0,2,1,3$



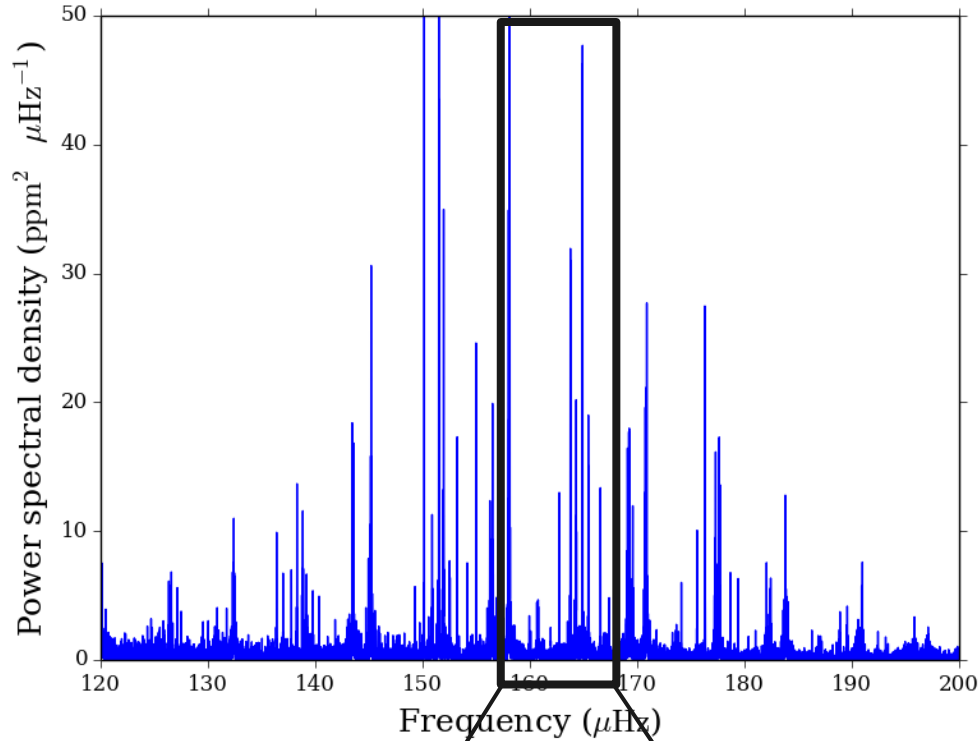
What happens when you *only* have 1335 days of data? (e.g. Best PLATO/Kepler)



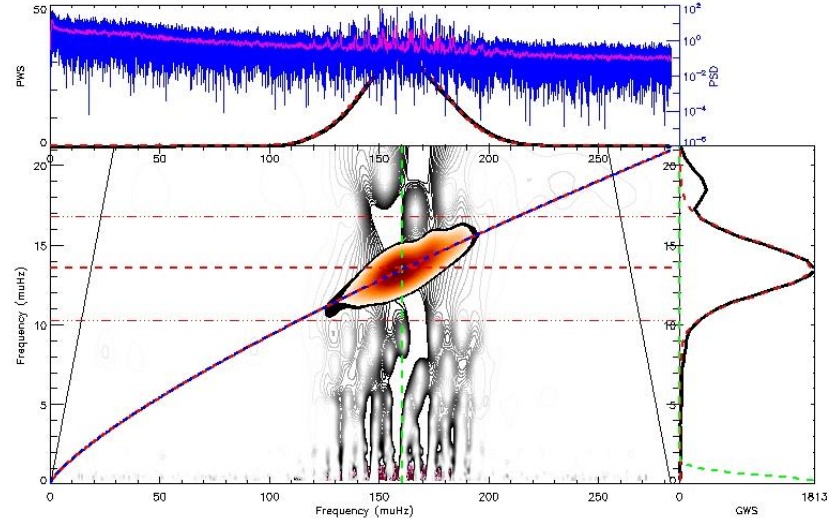
$d\nu = 12.97 \pm 0.27 \text{ } \mu\text{Hz}$
 $\nu_{\text{max}} = 160.8 \text{ } \mu\text{Hz}$
period spacing = $80.446 \pm 0.004 \text{ s}$
rotation $\langle \Omega_{\text{Core}} \rangle = 0.43 \pm 0.01 \text{ } \mu\text{Hz}$
Individual frequencies - for $l=0,2,1,3$

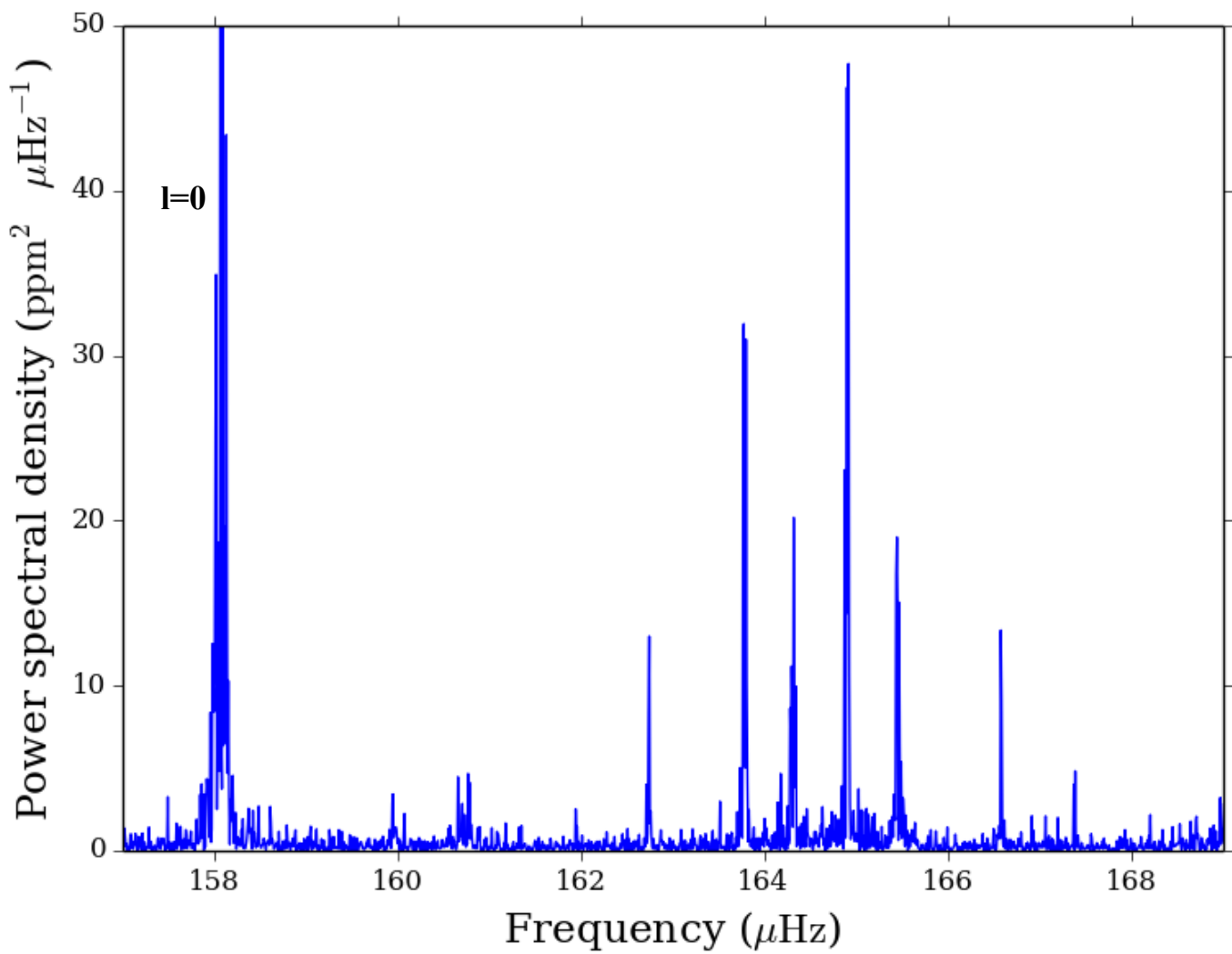


What happens when you *only* have 1335 days of data? (e.g. Best PLATO/Kepler)

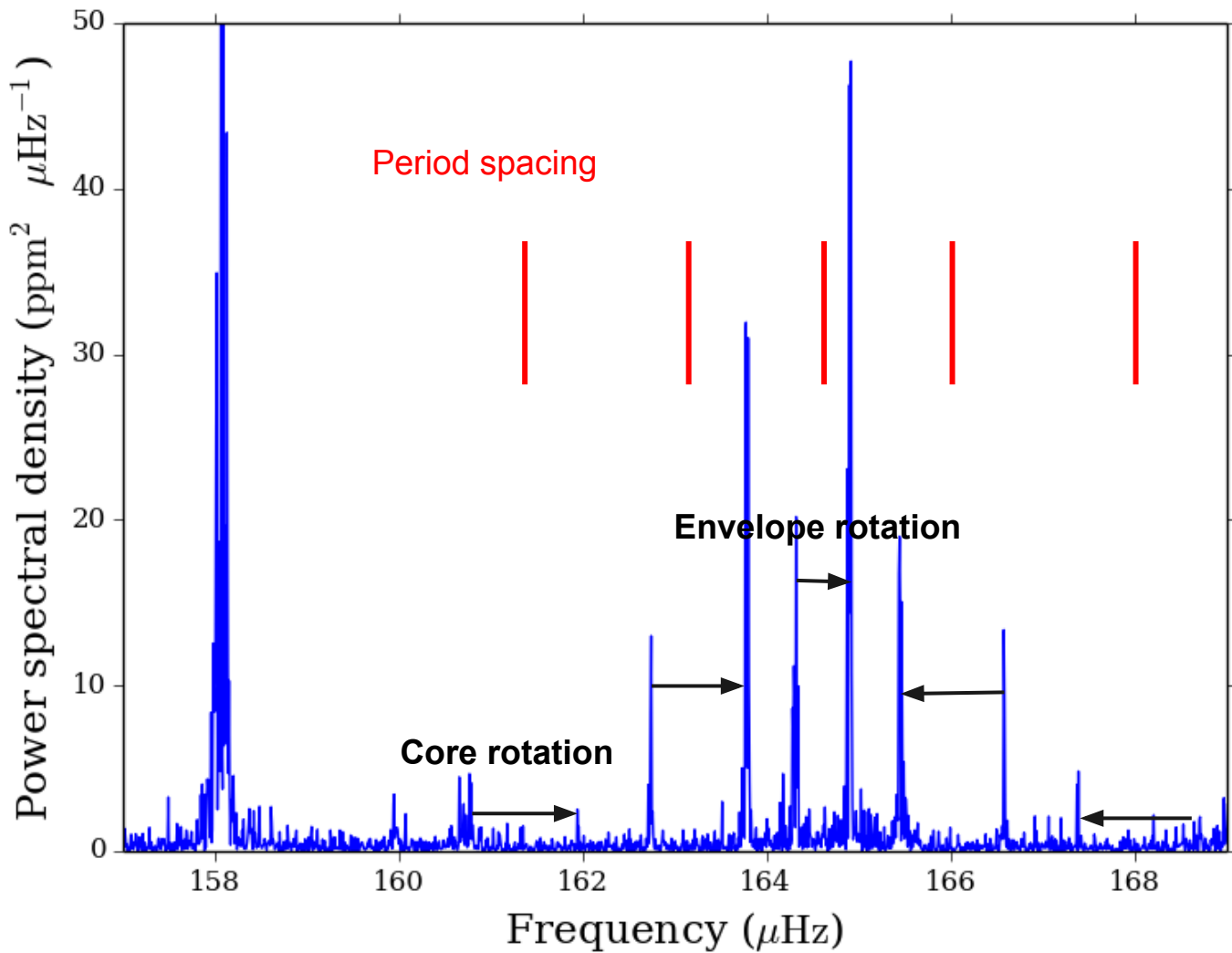


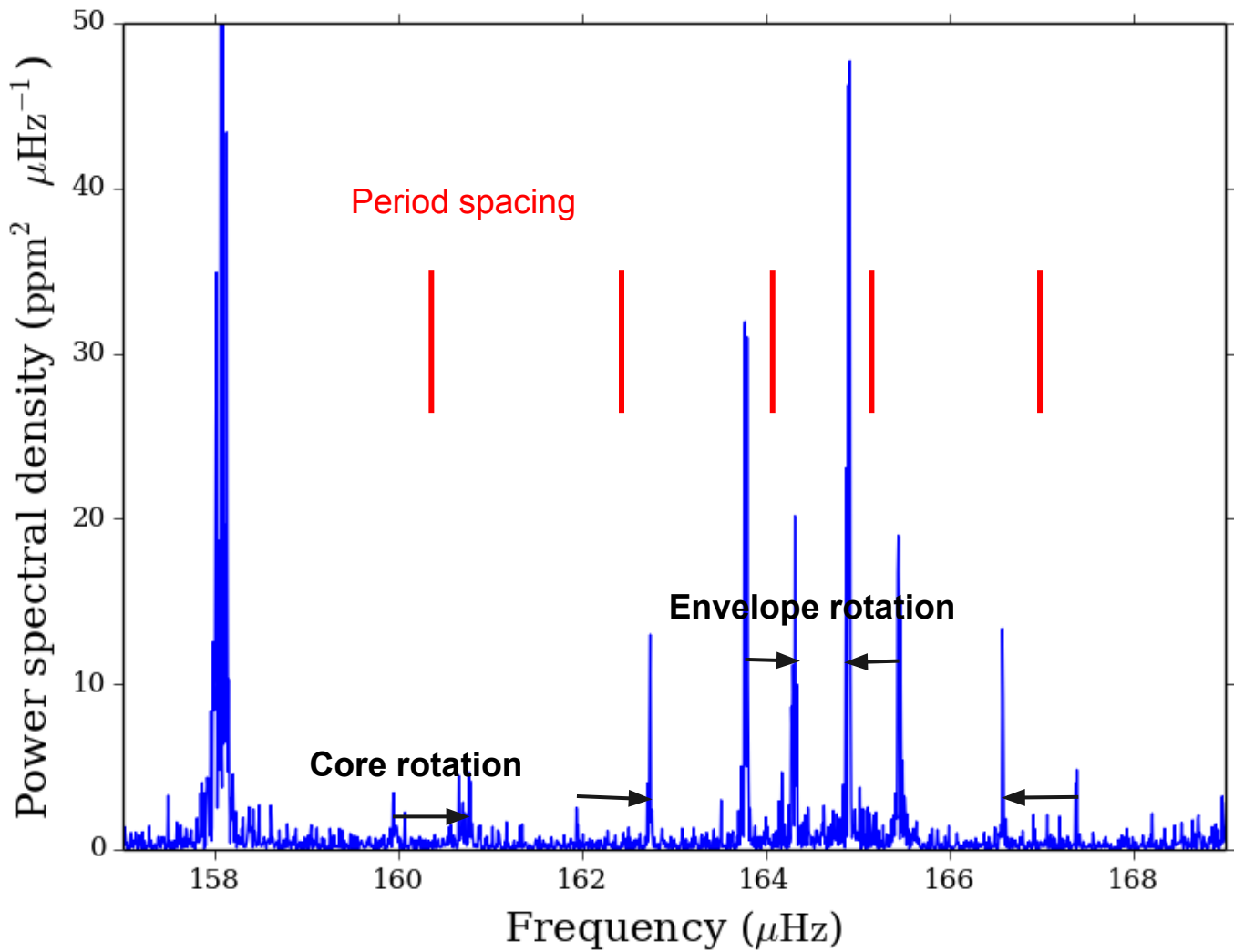
$dnu = 12.97 \pm 0.27 \mu\text{Hz}$
 $numax = 160.8 \mu\text{Hz}$
period spacing = $80.446 \pm 0.004 \text{ s}$
rotation $\langle\Omega_{\text{Core}}\rangle = 0.43 \pm 0.01 \mu\text{Hz}$
Individual frequencies - for $l=0,2,1,3$

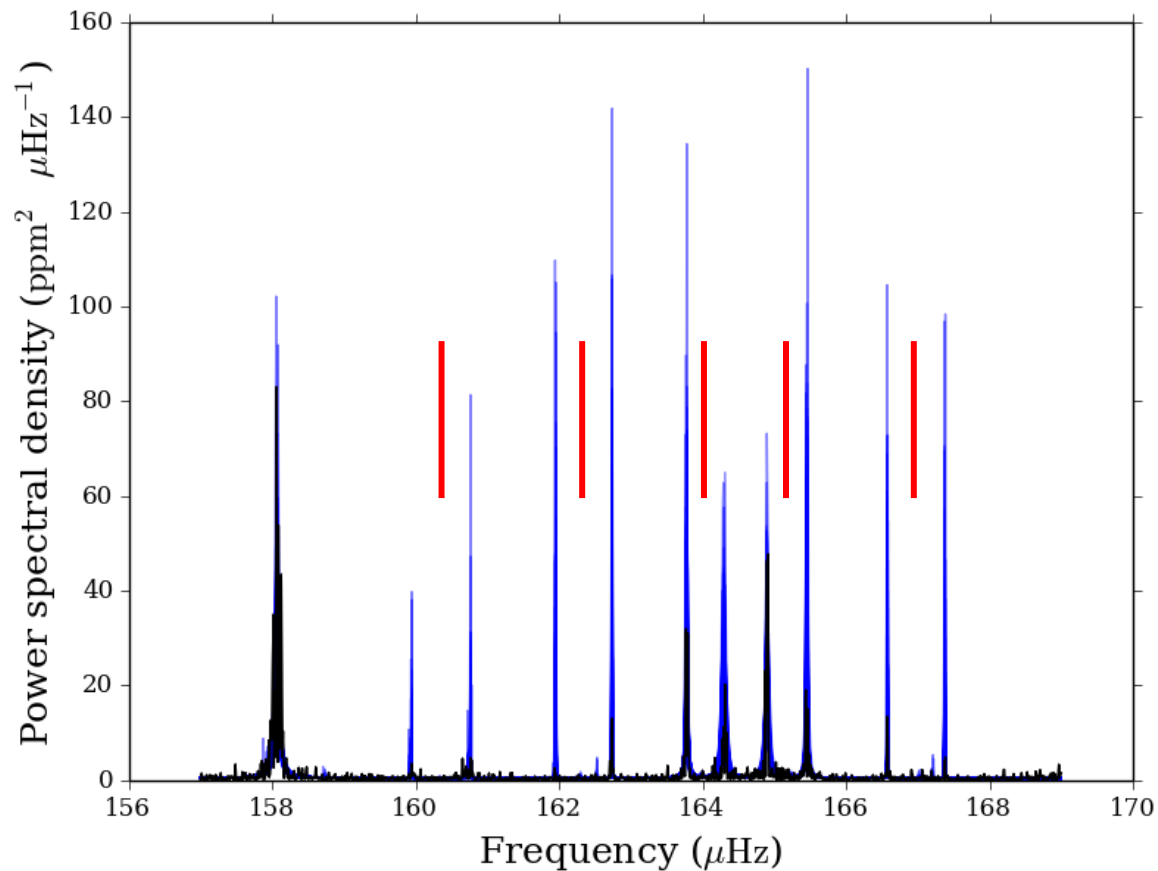
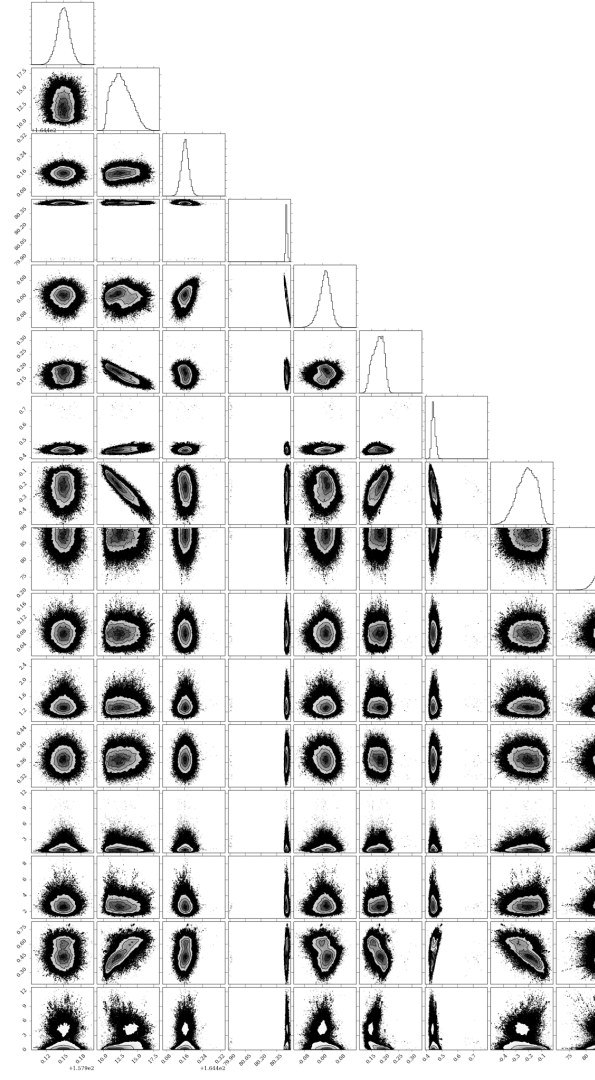




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See the next talk for more on period spacing.

Observations and constraint



Observable	Red giant	Solar type subgiant	Solar type main sequence	The Sun
Average frequency spacings + numax				
Period spacing	Probably (not all)	Possibly	Difficult	Very difficult
Rotation	Probably (even less than above)	Radial differential rotation - some	Average splitting	Helioseismology - map of interior
Individual frequencies	Yes - Mode ID is/was a problem ... Benoit ...	Yes	Yes	Yes



Getting from observables to intrinsic properties you lot care about ...



Why should we correct reported pulsation frequencies for stellar line-of-sight Doppler velocity shifts?

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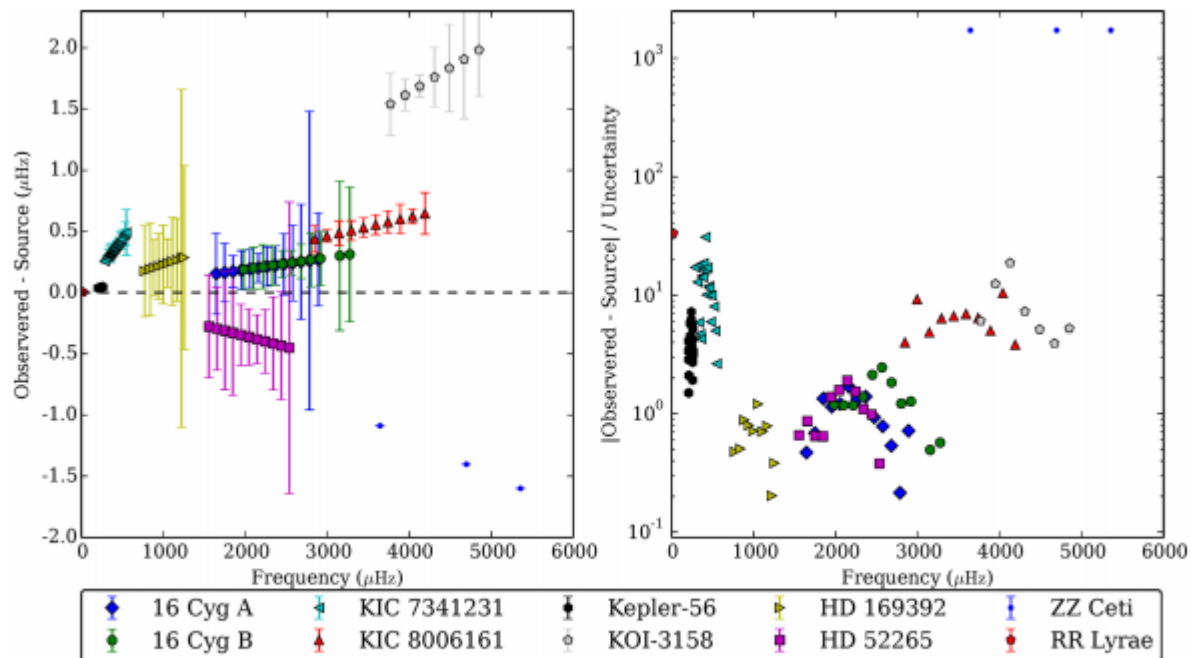


Figure 2. Differences in published (e.g. Solar system barycentric frame of reference) and Doppler shift corrected (source frame of reference) pulsation frequencies for a selection of stars and modes of oscillation. The left-hand panel gives the differences as a function of frequency while the right-hand panel displays the difference divided by the uncertainty.