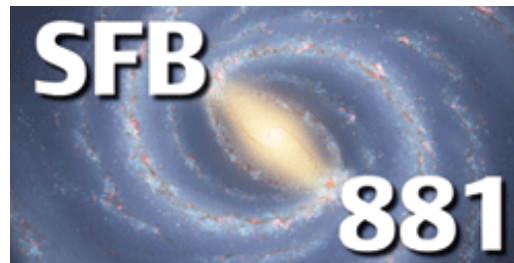


Hydrodynamical model atmospheres: Their impact on stellar spectroscopy and asteroseismology

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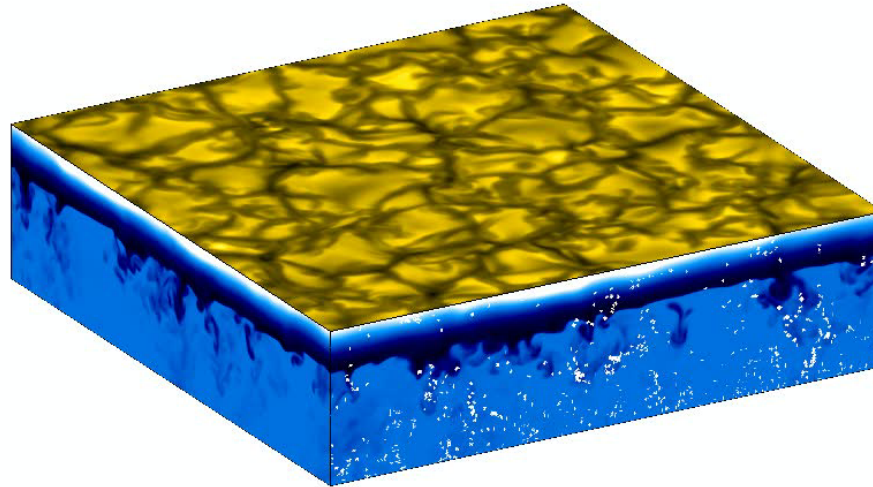
Overview

- 3D model atmospheres in a nutshell
 - contrasting 3D with situation in standard 1D models
- CO⁵BOLD 3D model grid
- Applications in asteroseismology and spectroscopy?
Not exhaustive list but trying to be illustrative
 - work on the percentage level
- Examples from work *in progress* ...
 - diagnostic potential of the so-called granulation background → [Ludwig et al.](#) ↓
 - microturbulence and collisional cross-sections of neutral hydrogen with oxygen
→ [Steffen et al.](#) ↓
 - corrections to theoretical oscillation frequency due to surface effects
→ [Sonoji et al.](#) ↑
- Leaving out 3D abundance corrections, in particular of molecular species

1D and 3D model atmospheres of late-type stars

Solar Granulation: d3g157g44n94
Intensity & specific entropy
Time= 331.8 min

dirms: 15.2 %



1D model atmospheres

plane-parallel or spherical symmetry

time-independent

CT with mixing-length theory

RT with 10^5 frequencies

radiative-convective equilibrium

CPU time \approx 1 min

3D model atmospheres

no assumptions on symmetry

small representative patch of surface layers

time-dependent

solution of M(HD) equations

up-to 25 **frequency bands** (or bins)

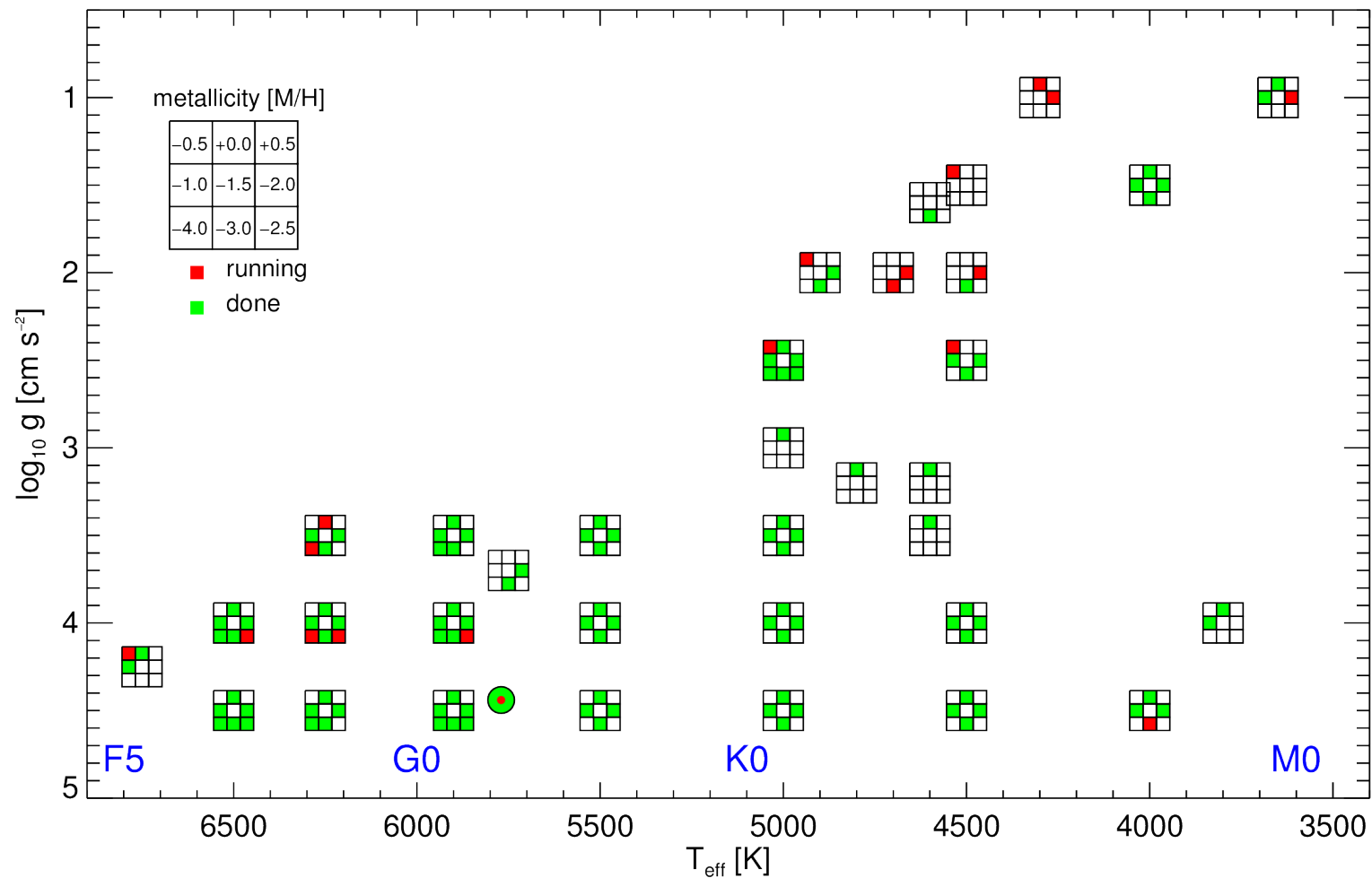
follows flow evolution

quasi-stationary, **fluctuations**

$10^5 \dots 10^6$ min \rightarrow grids?

\dots and **many more technical details**

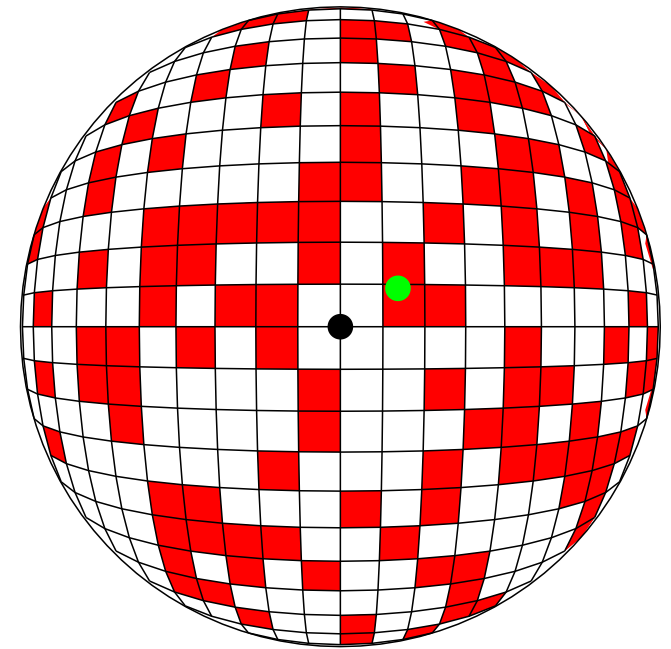
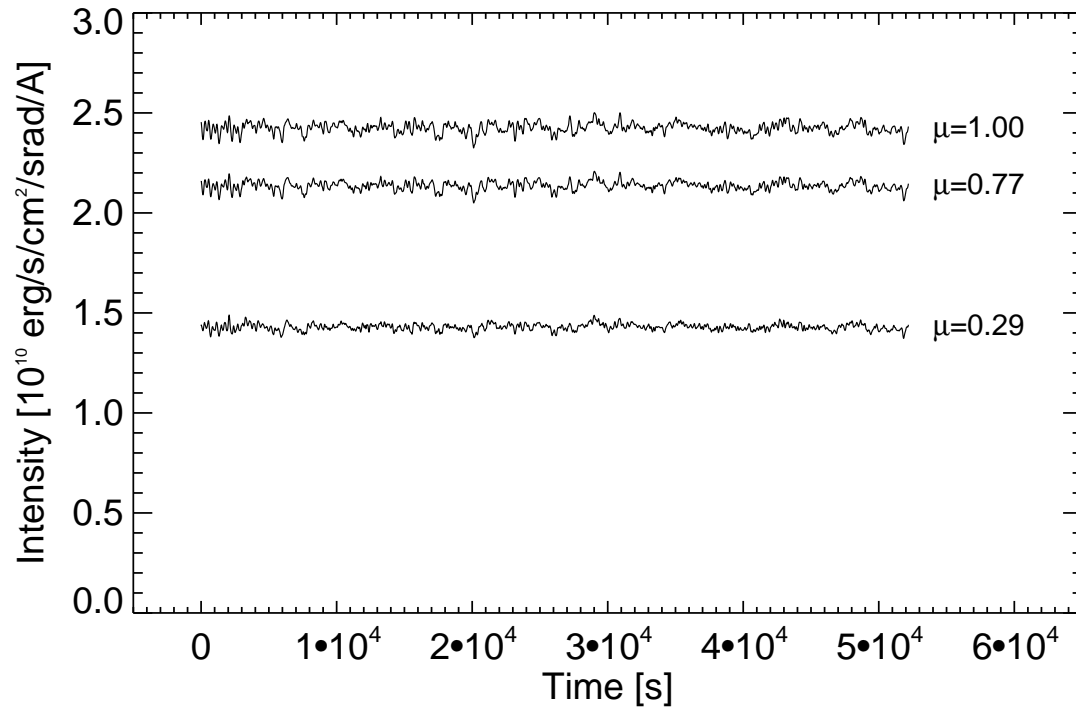
CO⁵BOLD 3D model atmosphere grid of non-degenerate objects



(Ludwig, Caffau, Steffen, Freytag, Bonifacio, Kučinskas)

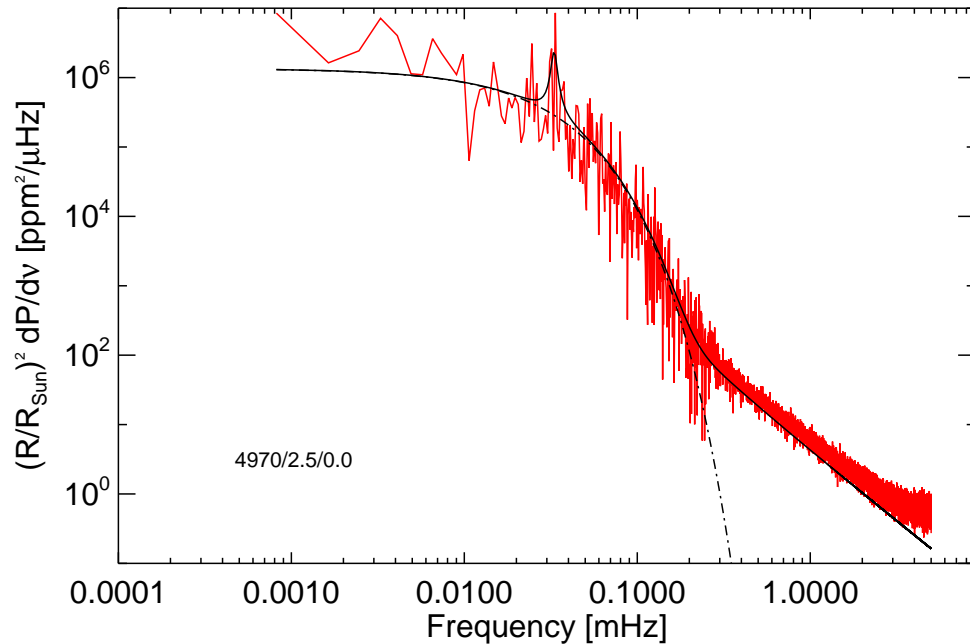
- Filling of parameter space mostly project driven
- In addition: M-dwarfs, AGB giants, brown dwarfs, white dwarfs ...

Granulation background across the Hertzsprung-Russell diagram

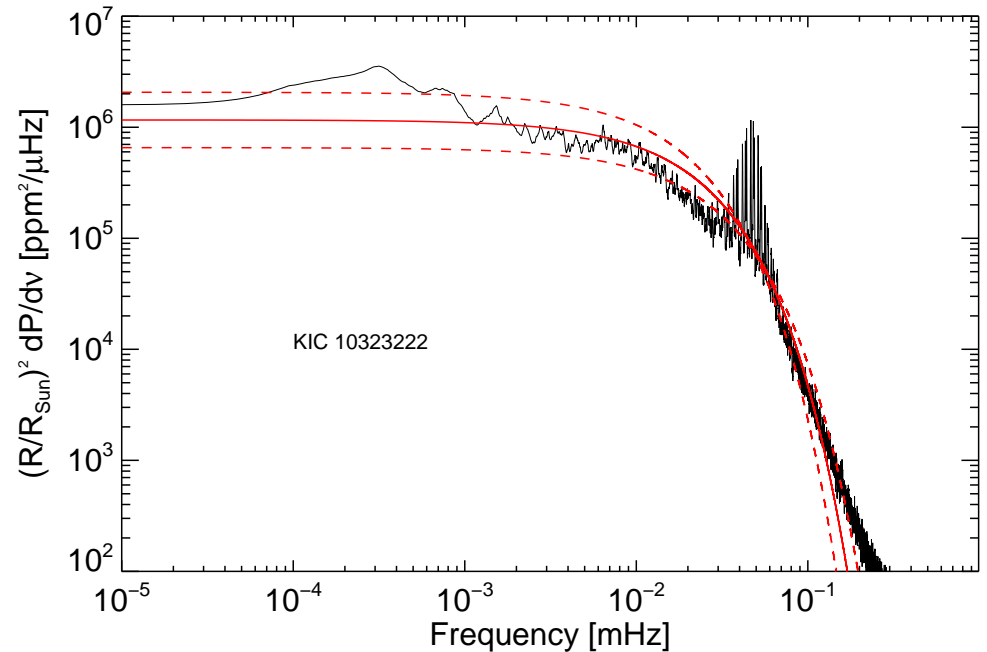


- 3D model provides realization of radiative output of “patch” on the stellar surface
 - only horizontal average considered, dependence on limb-angle included: $I_{\text{bol}}(t, \mu)$
- Assuming *incoherent action* of (perhaps many) patches \rightarrow stellar radius
 - ok for random granulation pattern, inadequate for oscillatory modes
- Outcome: estimate of **power spectrum of observable, global brightness fluctuations**

Simulated and observed power spectra



simulation & fitted model



comparison with observation (Kepler)



Exponential background model

$$\frac{dP}{d\nu}(\nu) = b \exp(-\nu/\nu_{\text{gran}}) + \text{sum of Lorentzian box modes}$$

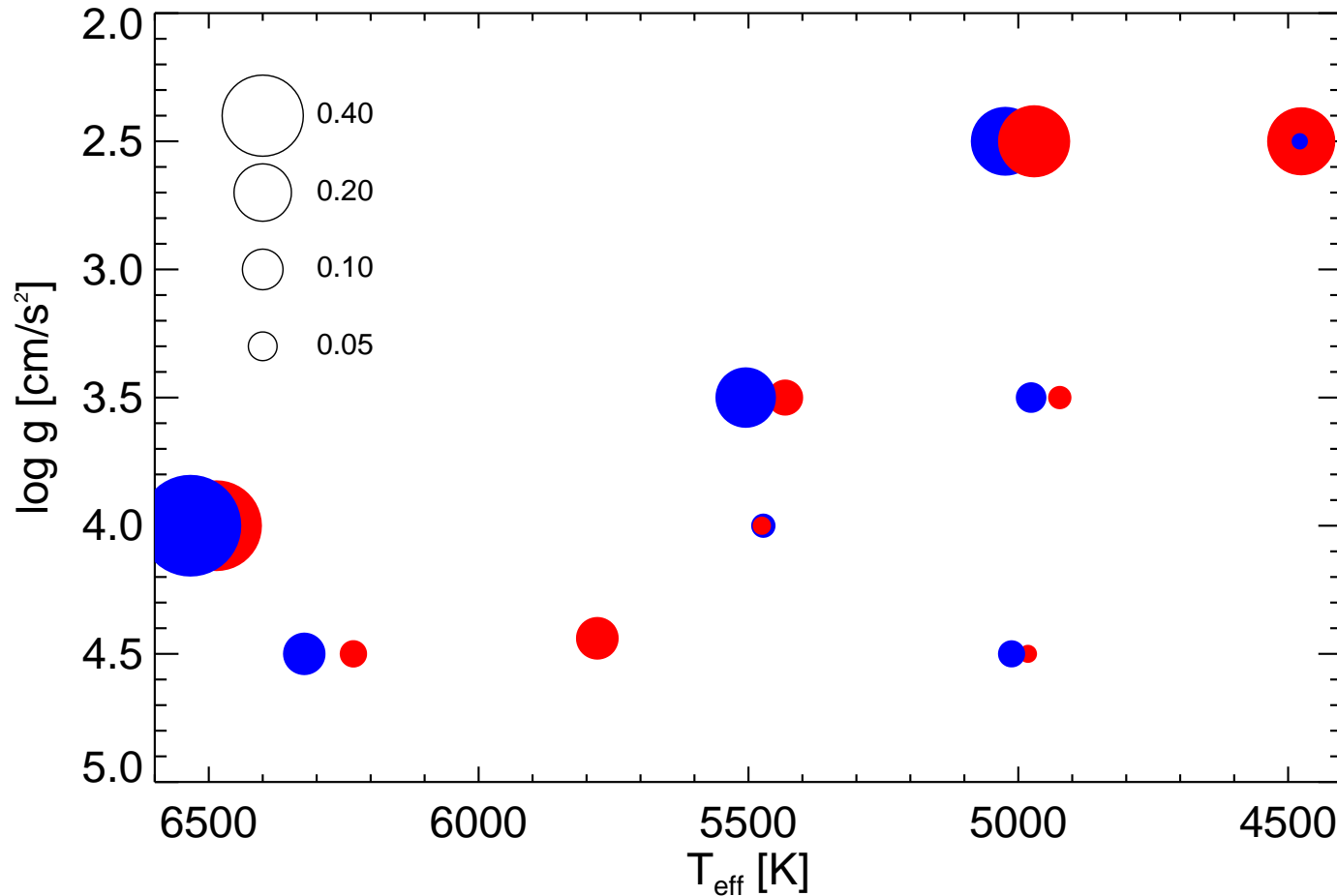
- characteristic granular frequency ν_{gran} , frequency-integrated fluctuation σ_{gran}



Rather: scaled frequency-integrated fluctuation $\tilde{\sigma}_{\text{gran}} \equiv \frac{R}{R_{\odot}} \sigma_{\text{gran}}$

- stellar radius R not control parameter of the 3D model atmospheres
- external piece of information, e.g. $R(T_{\text{eff}}, \log g, [\text{M}/\text{H}])$ from evolutionary models

The (small) sample of 3D model atmospheres

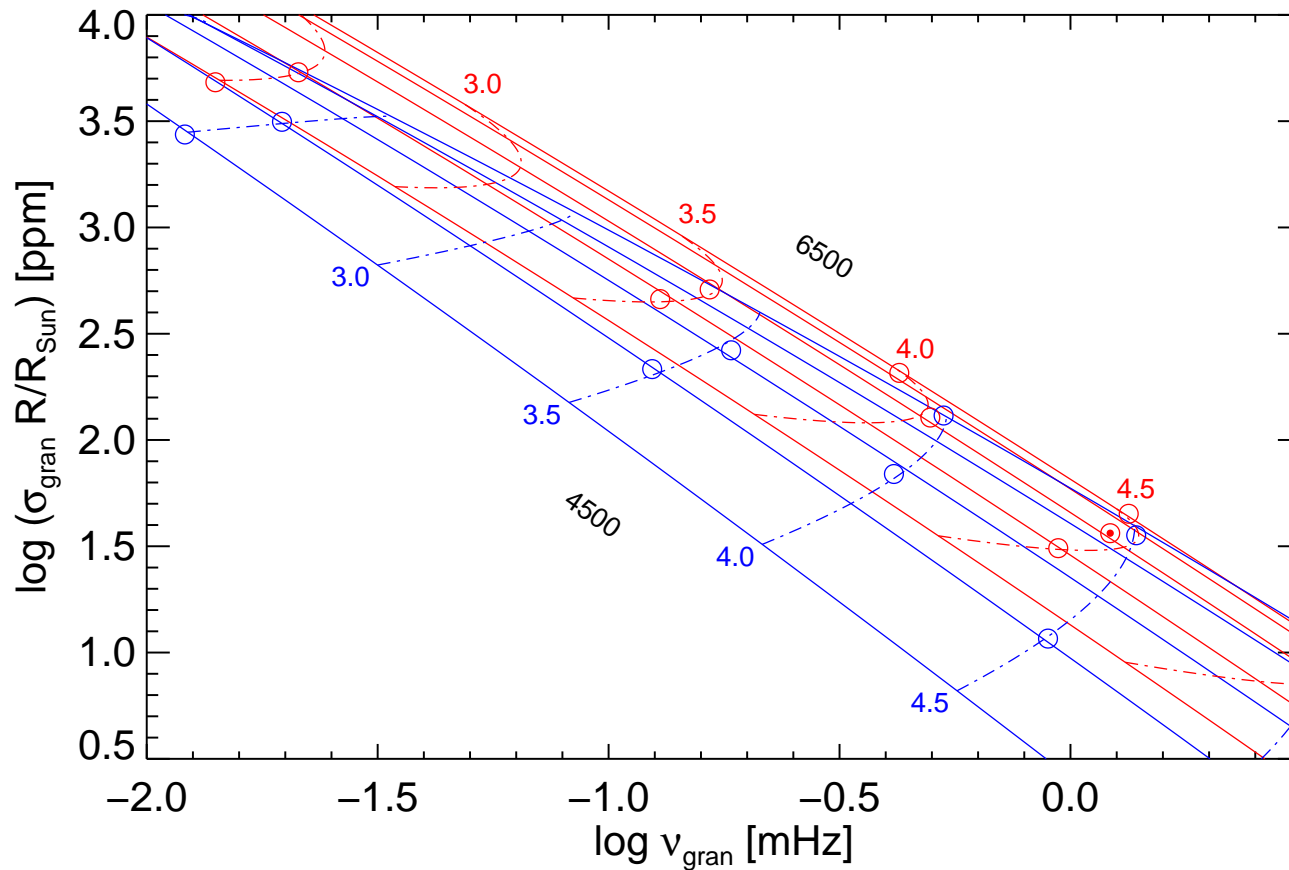


● 17 3D models: (ignore size of symbols)

● 9 solar metallicity **red circles**

● 8 sub-solar metallicity **blue circles** ($[M/H] = -2$)

“Inverse” Hertzsprung-Russell diagram of convective properties



- 17 3D models: solar metallicity red circles, sub-solar metallicity blue circles ($[M/H] = -2$)
- *Bi-quadratic power law* fit in $\log(T_{\text{eff}})$ and $\log g$ separately for both metallicities

- Dependence of brightness fluctuations on gravity well known \rightarrow *8-hour flicker*
- Theoretical quantification of T-sensitivity: significant difference with metallicity
- Fine structure in the shown fit not significant (yet) \rightarrow curvature at $[M/H] = 0$

An abundance analysis of the Hyades giant γ Tauri: an exercise in caution

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3.1.2. Microturbulence

This seemingly innocent but potent parameter deserves more respect than it usually gets, as its abuse can produce drastic effects on abundance results.

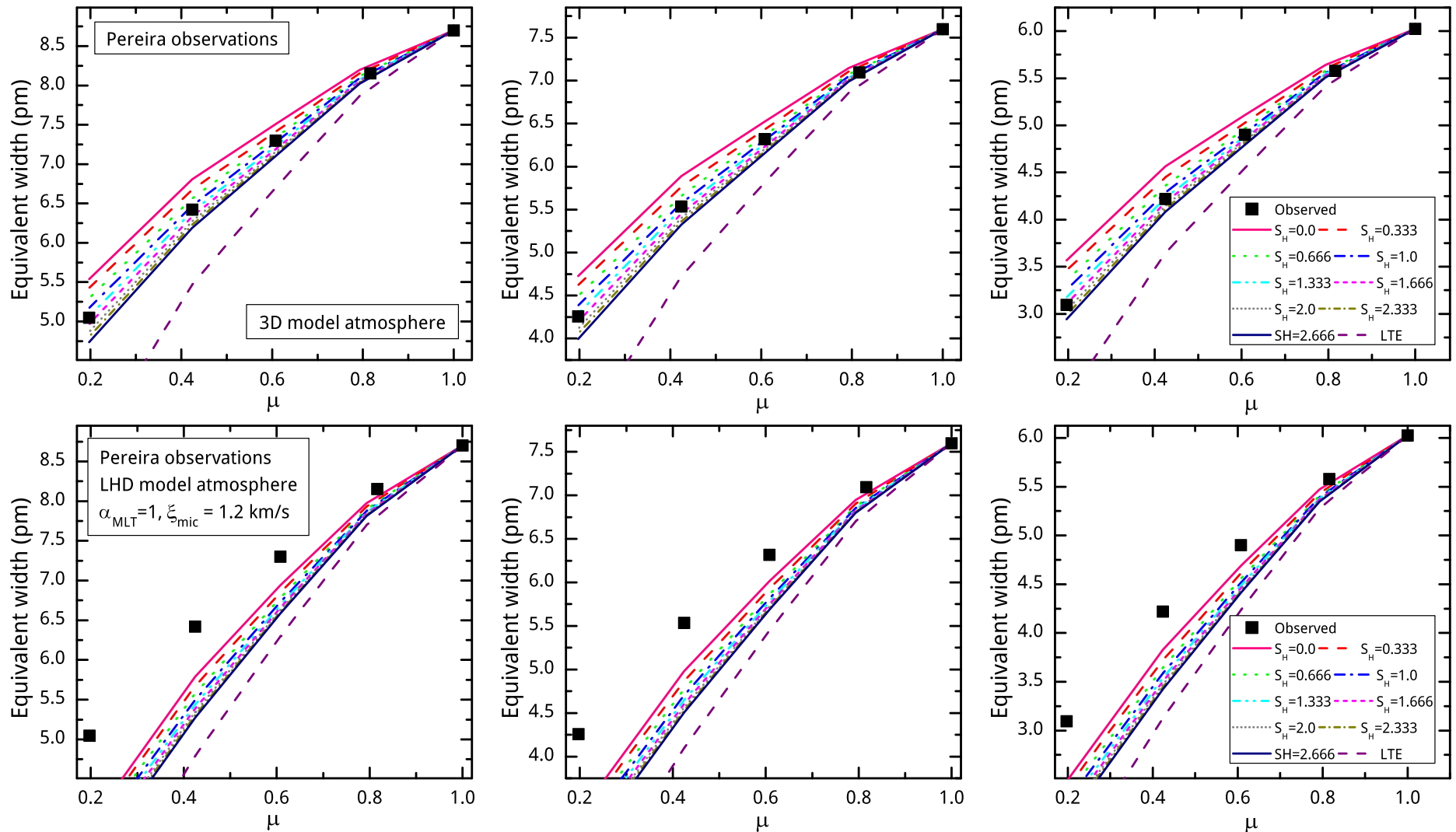
Microturbulence ξ_{micro}

- In **1D abundance analyses** ξ_{micro} is usually considered a “nuisance” parameter
 - influences the strength of strong, saturated lines
 - interpreted as effect of unknown (in 1D!), small-scale atmospheric velocity field
 - also **compensates offsets in thermal structure** between model and observation
 - usually modelled by a depth-independent Gaussian of fixed width ξ_{micro}
 - adjusted to make weak and strong lines provide the same abundance
- **Spectroscopic determination of T_{eff} , $\log g$, abundances, and ξ_{micro} interrelated**
- At low spectral resolution or S/N abundance analysis relies on strong lines → survey work
- No determination of ξ_{micro} possible, in need of calibration
- 3D models predict atmospheric velocity field → can provide theoretical guidance
 - longish story in itself, exploitation of this feature is worked on
 - **observational picture rather messy** (line parameters? activity? rotation?)

Another exercise in caution: ξ_{micro} and S_{H}

- Departures from local thermodynamic equilibrium (LTE) limits accuracy of spectroscopic abundance determinations – also in cool stars
- Collisions with neutral H-atoms important for establishing of LTE
- Few accurate laboratory measurements or quantum-mechanical calculations available
 - standard recipe: approximate **Drawin formula times a global scaling factor S_{H}**
 - empirical calibration of S_{H} necessary
- Wording: *global* means here for all transitions in a particular model atom in the same way
- Here: 1D and 3D calibration of S_{H} for oxygen infrared triplet lines in the Sun
 - observation of lines at various limb-angles $\mu = \cos \theta$
 - unique abundance of oxygen assumed
 - **ξ_{micro} in 1D model: Gaussian, depth-independent, μ -independent**

Center-to-limb variation of O-triplet in 3D-NLTE and 1D-NLTE



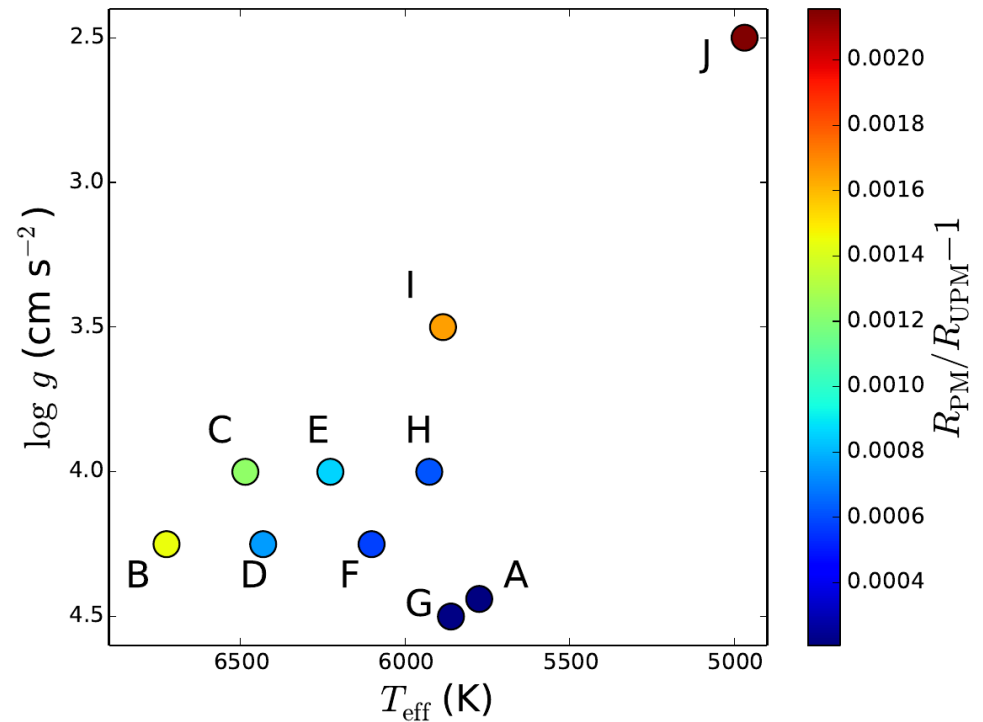
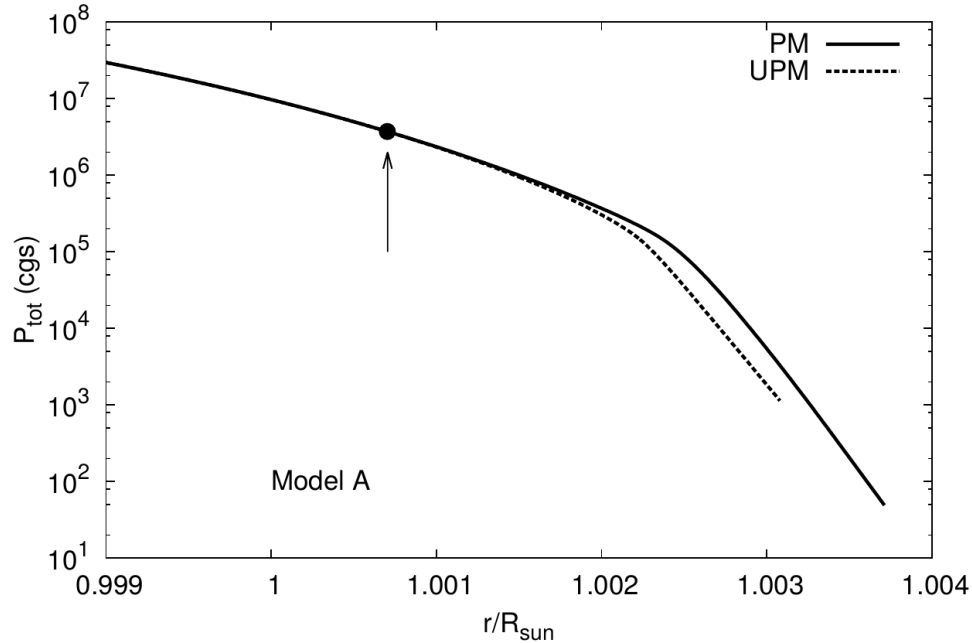
● 3D: $S_H = 1.2 \dots 1.8$, oxygen abundance $\log \epsilon_O = 8.76 \pm 0.02$

● 1D: no reasonable fit possible ($S_H < 0$)! \rightarrow μ -independent ξ_{micro} problematic

Stellar models and turbulent pressure

- In standard 1D stellar models convective transport is described by **mixing-length theory** (MLT)
 - approximate treatment of energy transport by gas flows
- Momentum transport, in particular **turbulent pressure** is usually ignored
 - in fact local nature of MLT make it difficult to include turbulent pressure
 - naturally included in multi-D hydrodynamical approach
- Effects limited to regions of significant flow speed (Mach numbers)
→ stellar surface
- Idea ...
 - combine interior 1D model with horizontally averaged 3D structure in the outer layers → combined or patched model
 - compare combined with standard model to derive changes in mode frequencies
- Correct for “surface effect”

3D model atmospheres and surface effects on mode frequencies

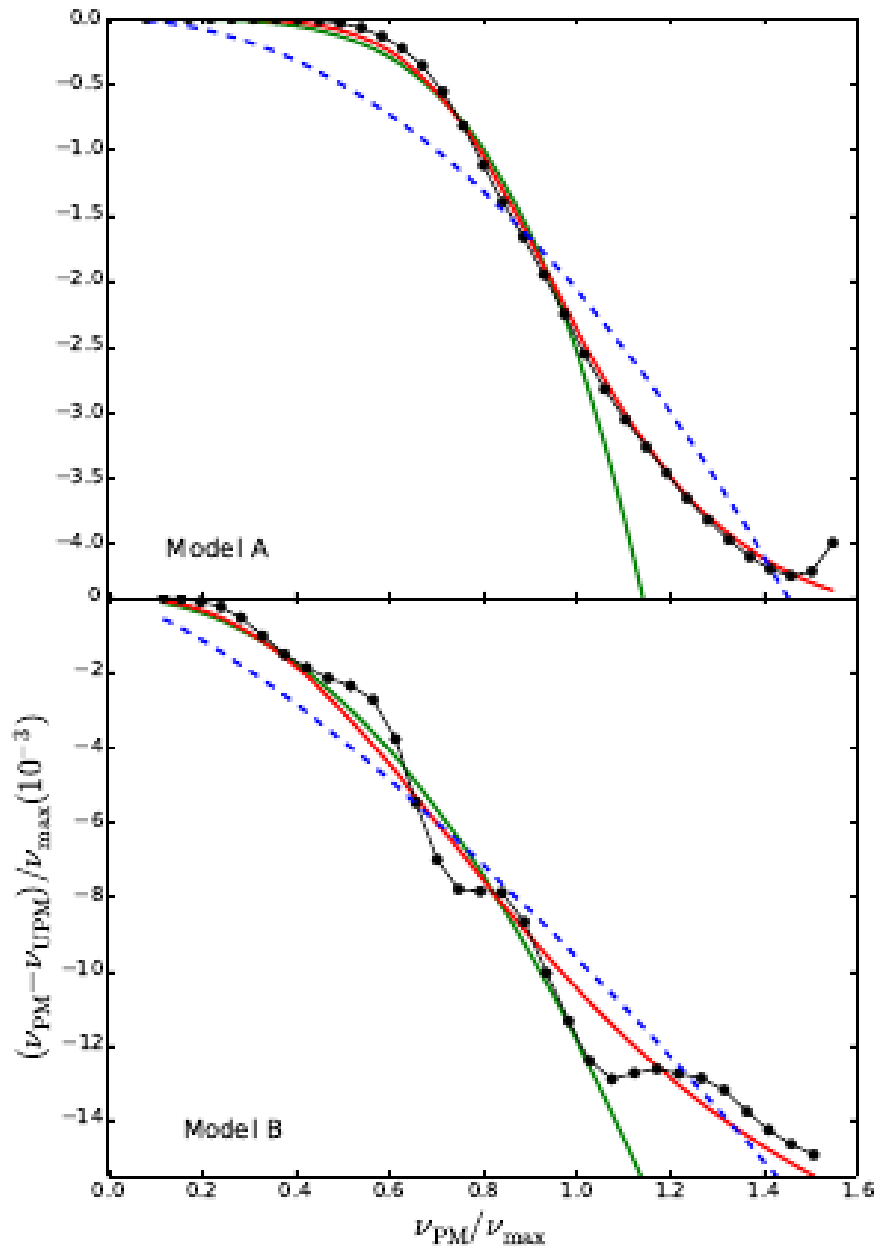


standard (UPM) & combined model (PM)

radius increase

- In 3D, turbulent pressure “lifts” outer layers wrt 1D standard model
- Increase of size of resonant cavity, effect pronounced in red giants ($\Delta R/R \approx 10^{-3}$)
- Systematic lowering of mode frequencies
 - frequency change dependent on upper turning point of waves

Examples: frequency changes of radial modes



- Green and dashed blue lines: power law fits to frequency differences as suggested by Kjeldsen et al. (2008)
- Red line: Lorentzian gives better fit
- Hot F-dwarf model B shows effects of acoustic glitch (H-ionization)
- → wiggly shape makes analytical fit difficult
- Here 10 models across HRD

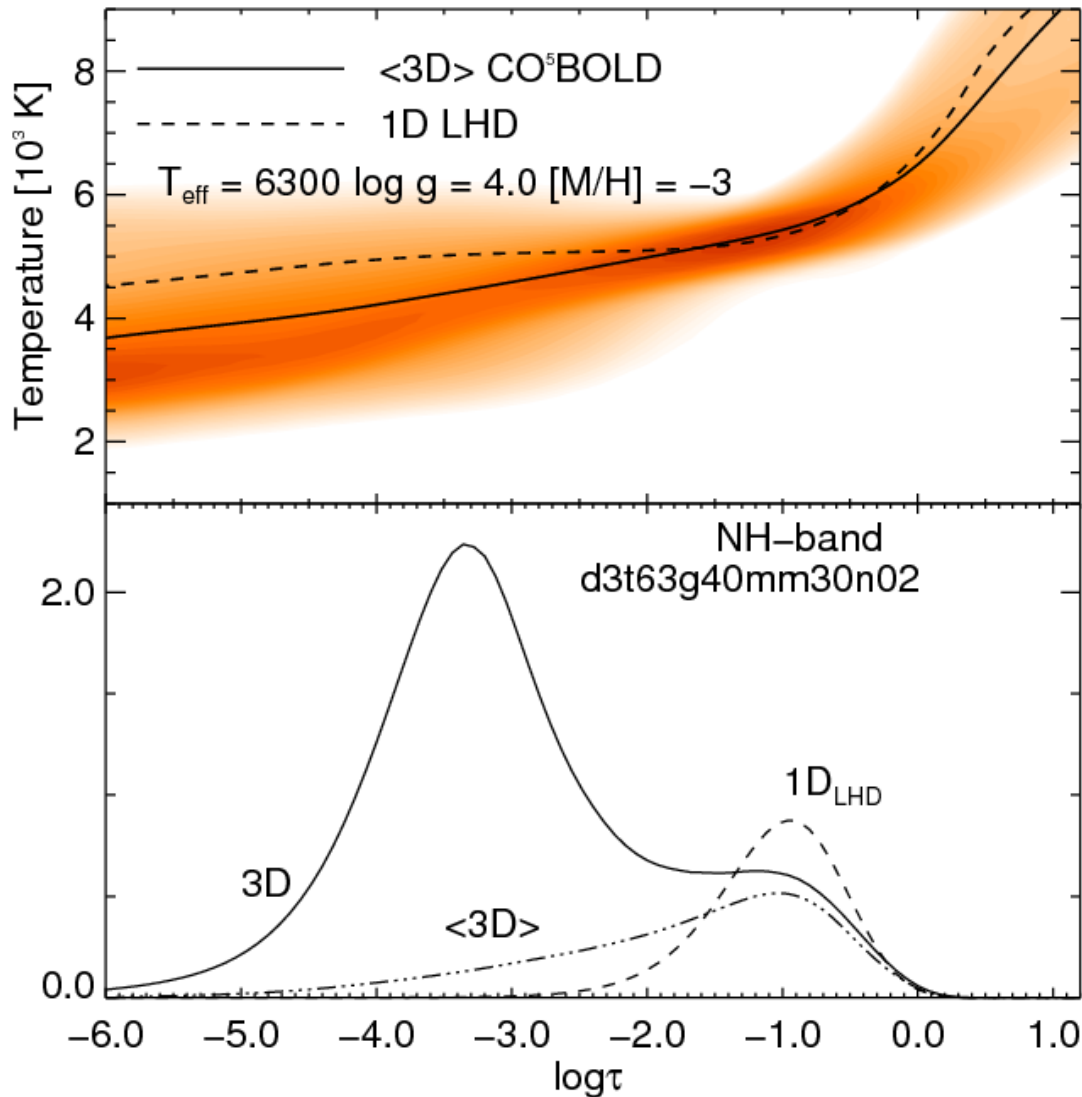
Final remarks

- 3D model atmospheres provide ...
 - a natural path to achieve higher accuracy in studies of stellar surface structure
 - the possibility to quantify the impact of approximations in 1D
- Exploitation of existing model grids to support survey work ongoing
 - systematic investigation of larger model basis
 - transfer of obtained information into analyses
- Observational tests?
- Where is this needed?

Talking of molecules ...



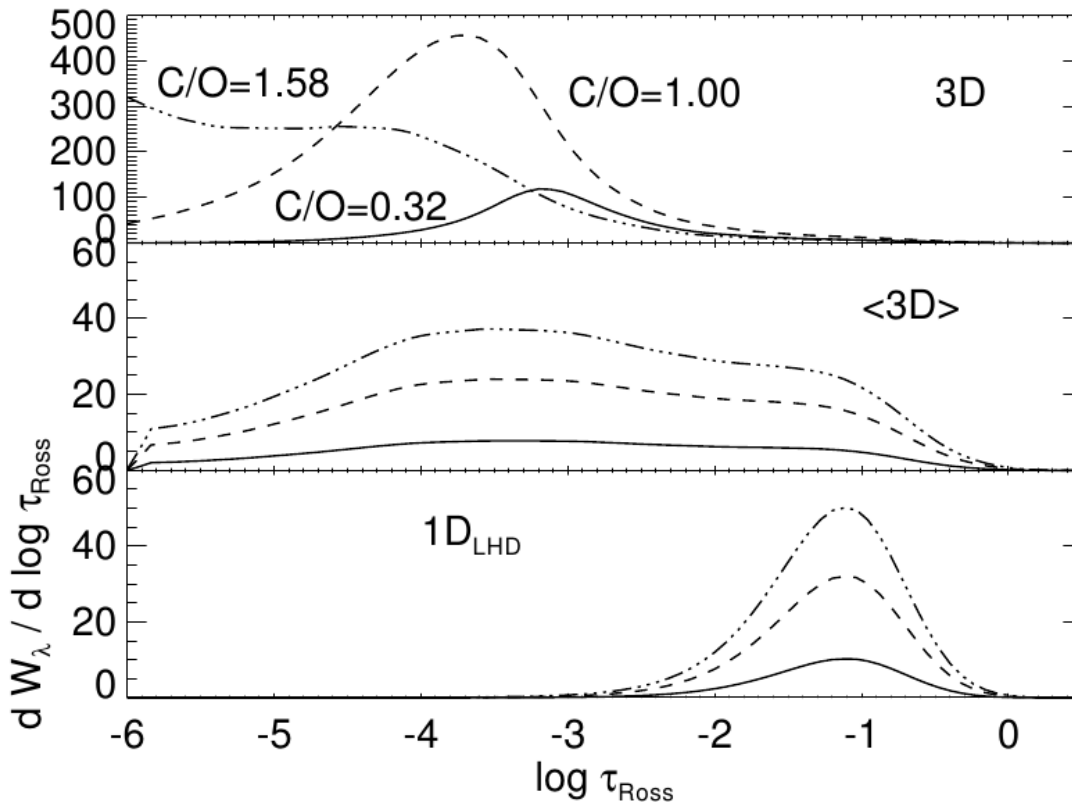
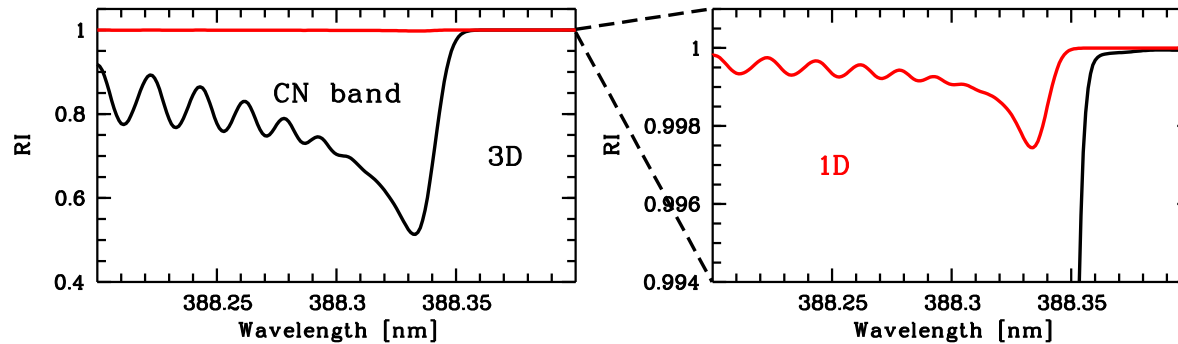
Molecular line formation and temperature fluctuations



(Bonifacio et al. 2013)

- Binary molecules
CH, NH, OH, C₂, CN, CO
important abundance indicators
- Dissociation equilibria rather
T-sensitive
- Example: **contribution function**
to equivalent width of NH band
- 3D vs. $\langle 3D \rangle$ emphasizes role of
T-fluctuations
- Coupled via reaction network

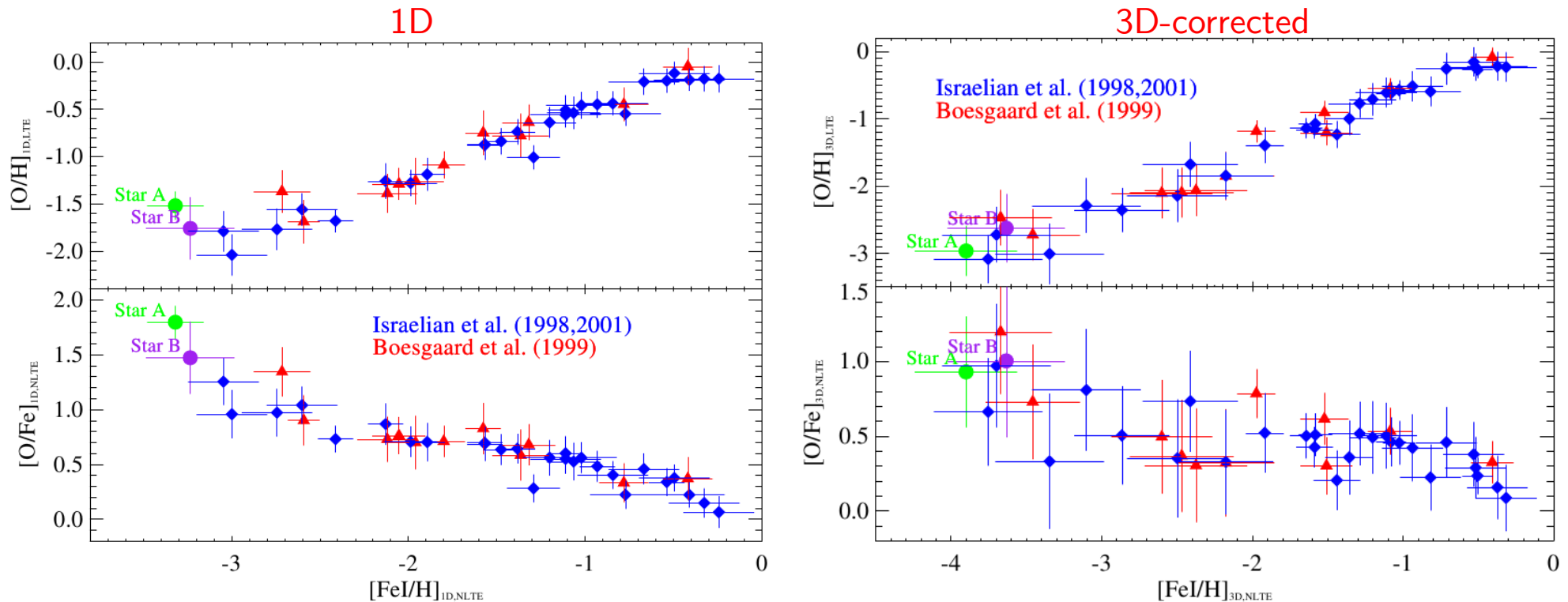
Molecular line formation and C/O ratio



(all figures from Bonifacio et al. 2013)

- CN 388.3 nm band
- ≈ 2 dex difference in EW
- Extreme sensitivity to carbon-to-oxygen ratio
- CO formation (most stable molecule) controls available C for other molecules
- Pure 3D effect!
- Frequency of CEMP stars? (from CH-band)

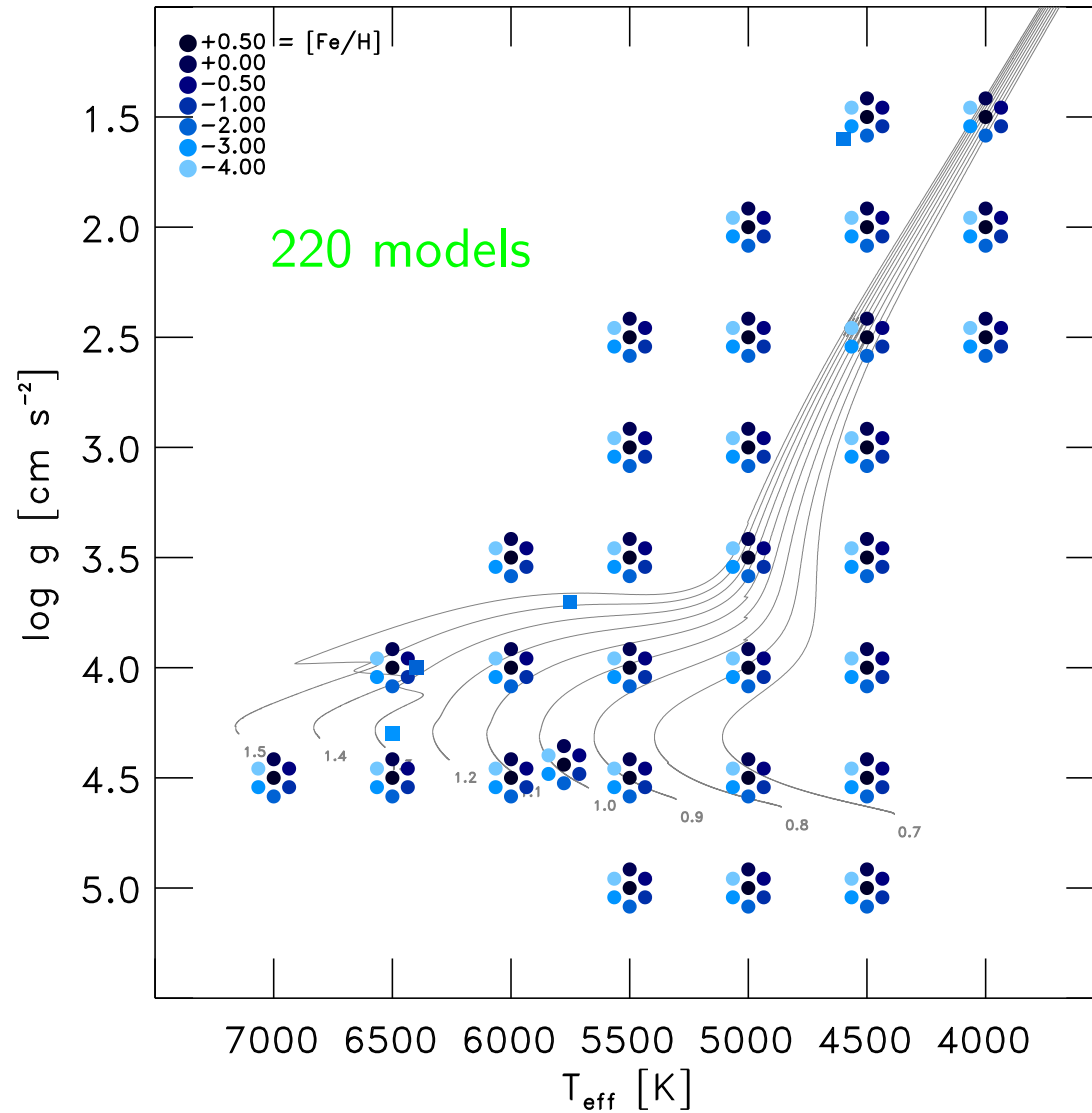
Galactic evolution of oxygen from OH lines in dwarfs



(González Hernández et al. 2010)

- UV-lines of OH in metal-poor dwarf stars last available abundance indicator of O
- Above example record work using 52 3D models to derive abundance corrections
- Downward revision by factor 10 at low metallicity, better consistency with giants
- Fine print: in 3D departures from LTE for Fe and molecules largely unexplored
→talk of Lyudmila Machonkina

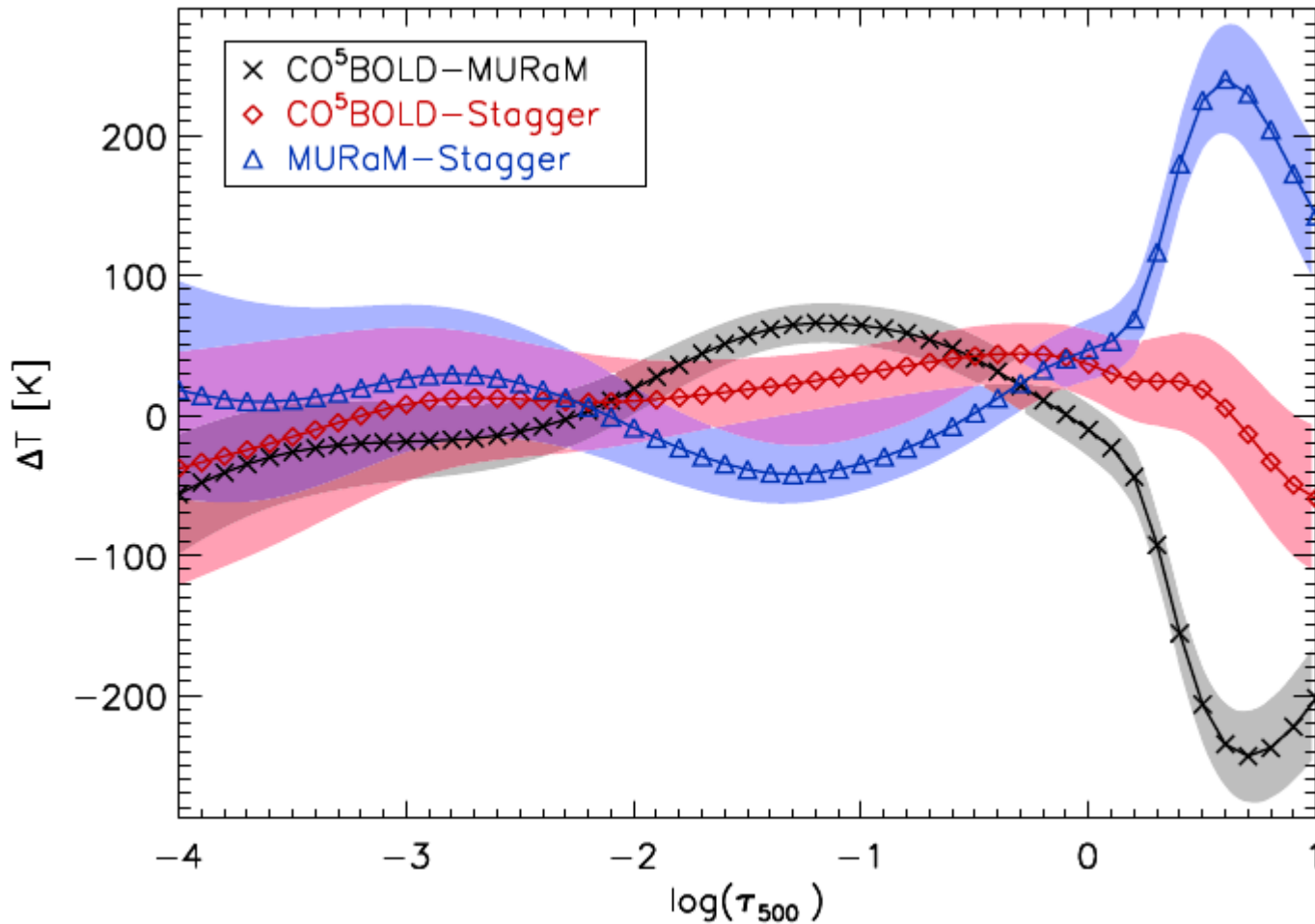
STAGGER 3D model atmosphere grid



(Magic et al. 2013)

🔴 More metallicities, typically higher resolution → talk by Remo Collet

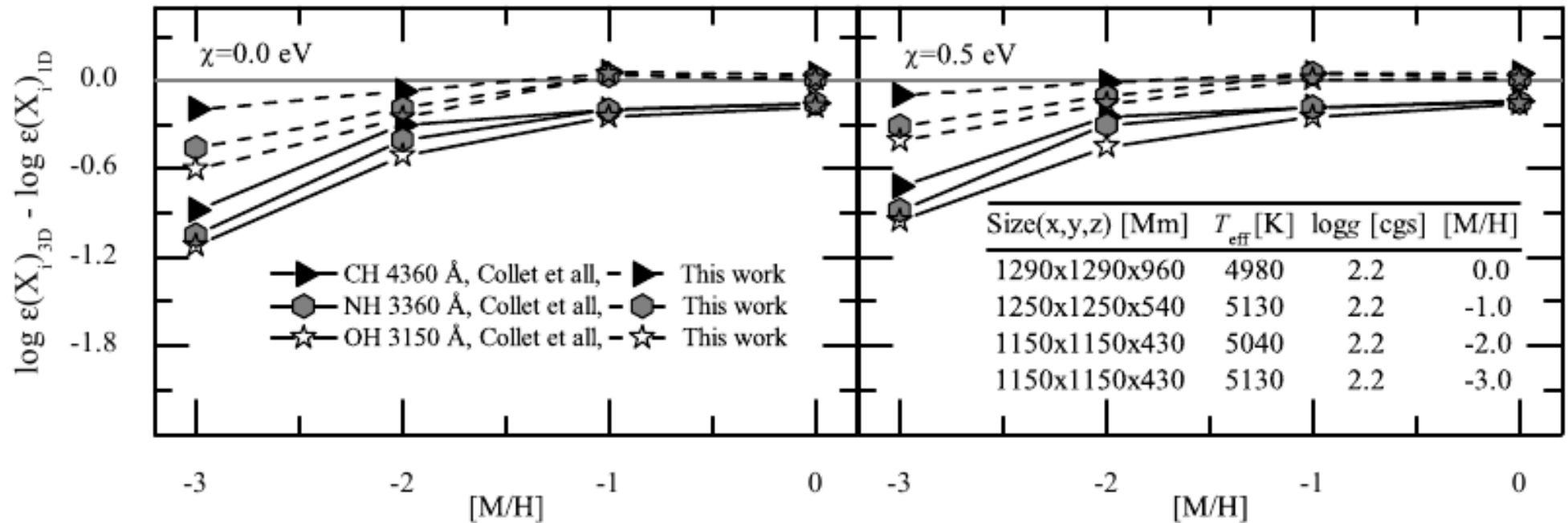
3D model systematics: getting closer – for the Sun



(Beeck et al. 2012)

- CO⁵BOLD and STAGGER (Collet et al. 2011) agree within 50 K for $\tau_{500} < 1$
- Discrepancies reduced by about factor 2 over recent years

Situation for giants less favorable



(Ivanauskas et al. 2010, Collet et al. 2007)

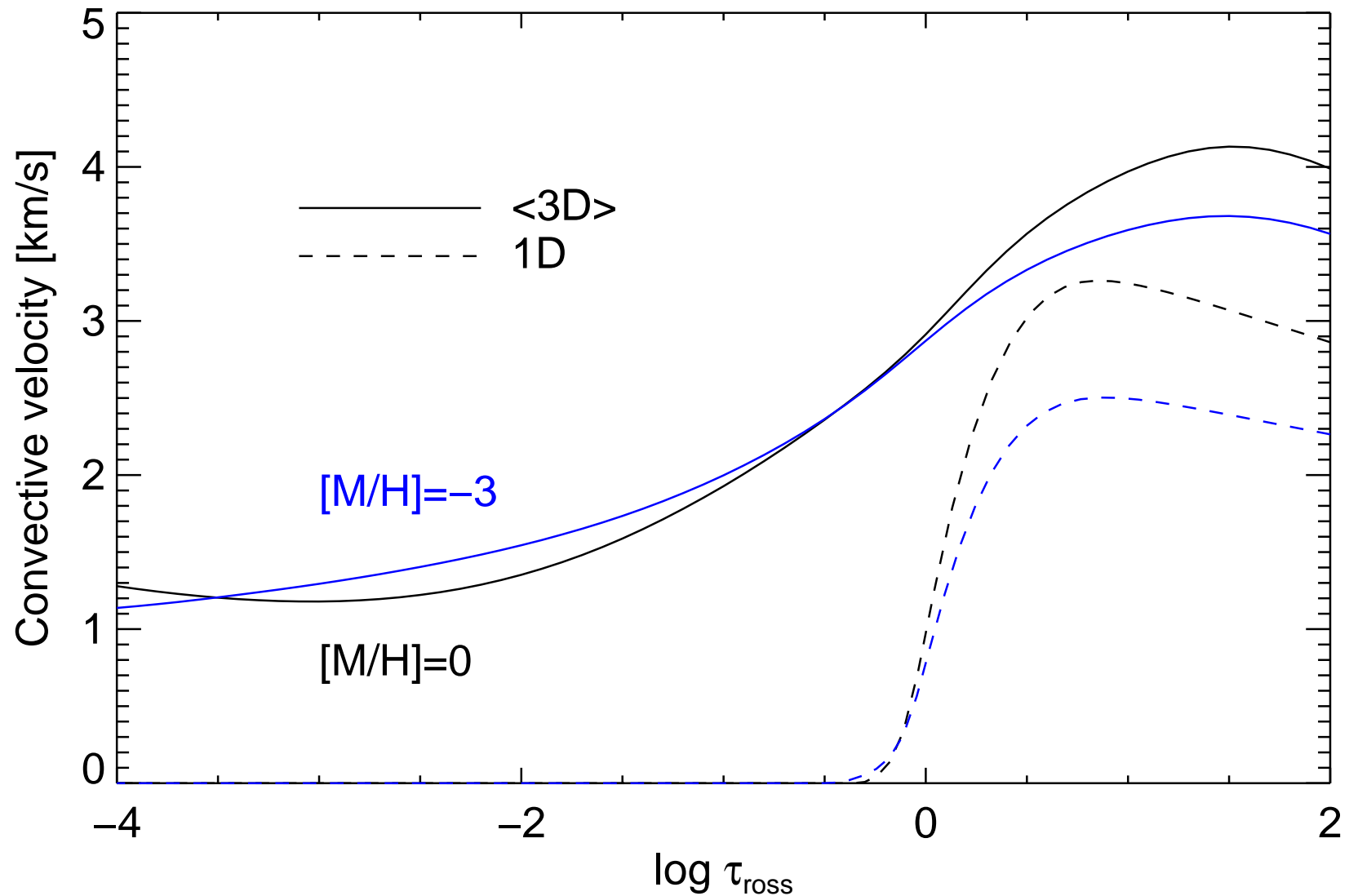
- Abundance corrections of molecules in CO⁵BOLD models smaller in magnitude than in Nordlund-Stein/STAGGER models
- Indicative of different T-structure
- Likely related to different approaches in opacity binning scheme

Comparison between 1D and 3D models

3D abundance corrections

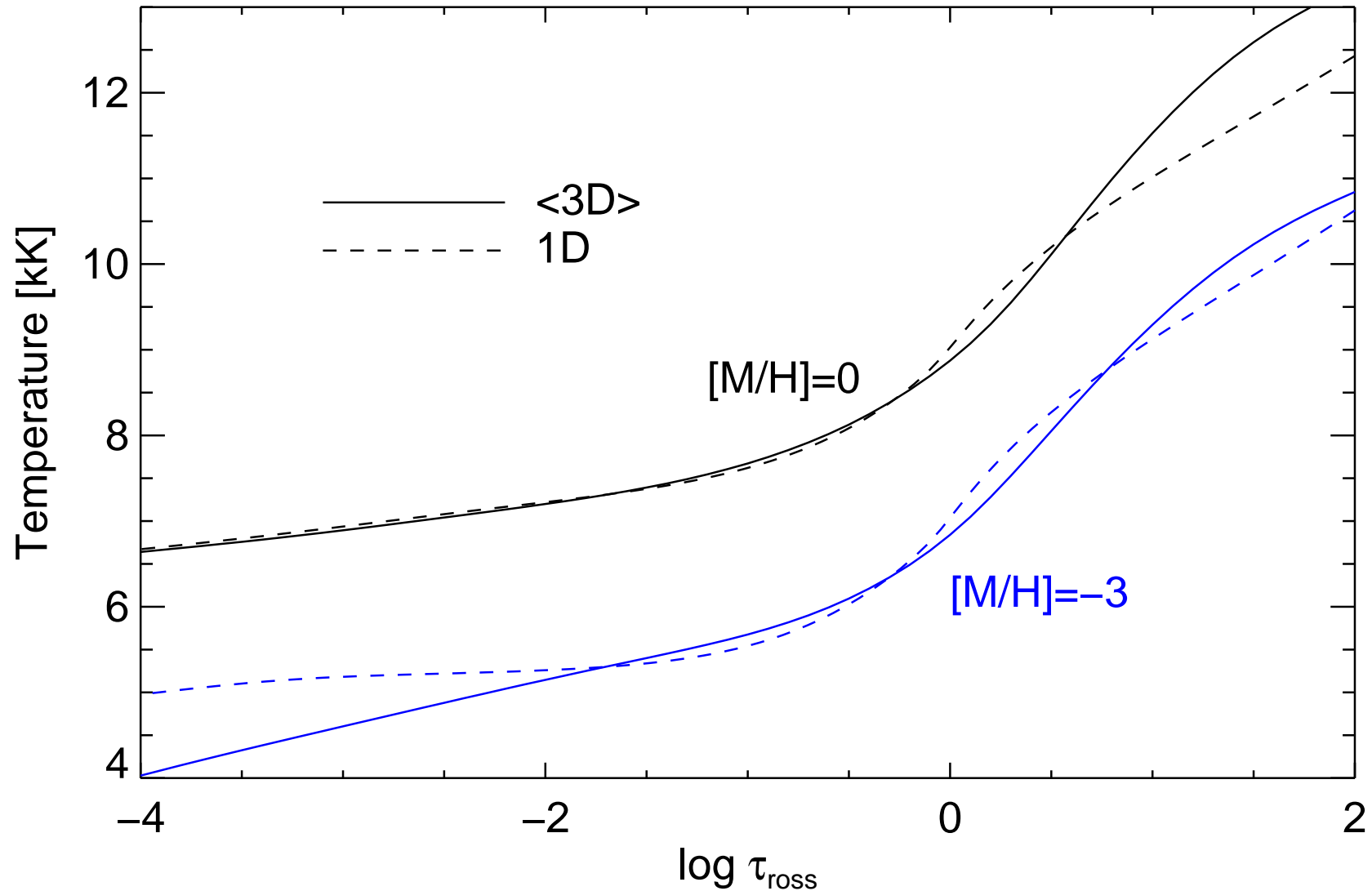
- Comparison between 1D and 3D model of the **same atmospheric parameters** effective temperature, surface gravity, overall metallicity
- 1D model has further free parameters, **mixing-length parameter, microturbulence ξ_{micro}** for spectroscopic applications
- Further diagnostics: **$\langle 3D \rangle$ model** obtained by horizontal and temporal averaging
- **3D abundance corrections ...**
 - spectral synthesis of spectral lines of interests in 1D and 3D
 - space-time averaging of 3D spectra
- **3D-1D** (total) correction: difference between 3D and 1D abundance for given line strength
 - **3D- $\langle 3D \rangle$** : effects due to horizontal inhomogeneities only
 - **$\langle 3D \rangle$ -1D**: effects due to differences in mean structure only

Overshooting beyond Schwarzschild boundary at all metallicities



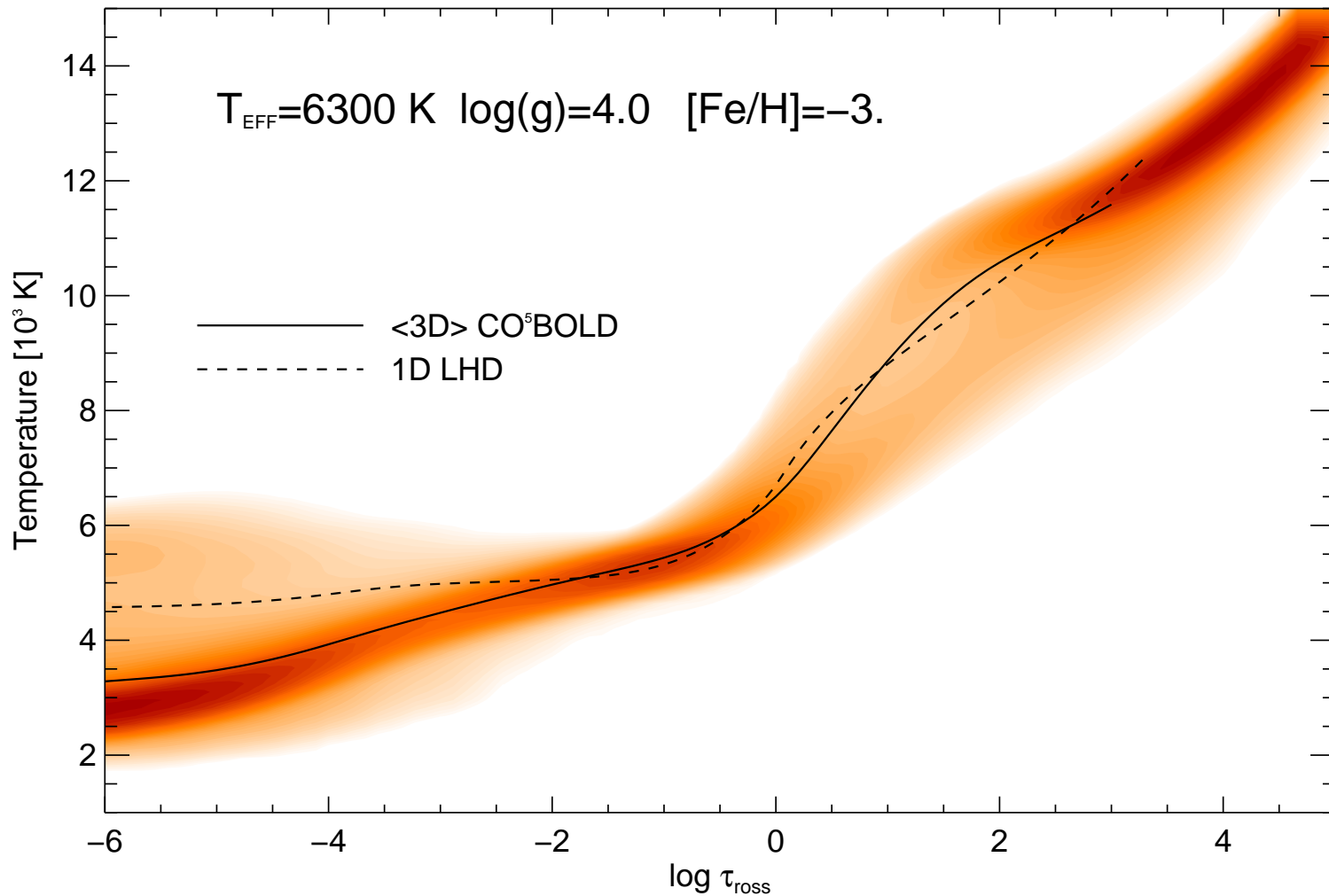
- 3D models predict strong overshooting (v_z^{rms}) \rightarrow micro/macro-turbulence

T-response to convective overshooting depends on metallicity



- In 3D balance between convective cooling and radiative heating
- Dependent on atmospheric parameters, in particular metallicity

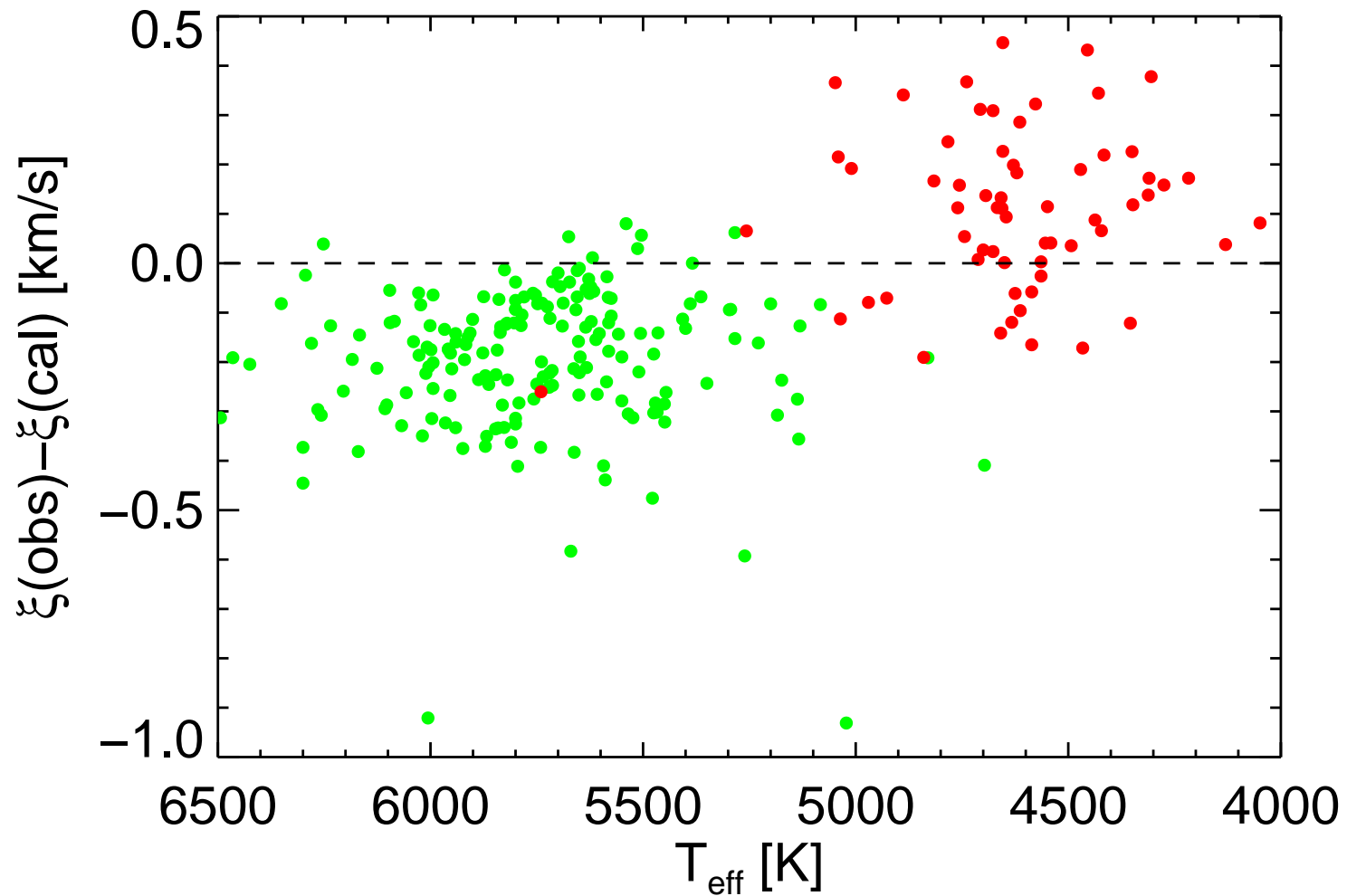
Temperature fluctuations



(González Hernández et al. 2010)

- Flow dynamics induces temperature fluctuations

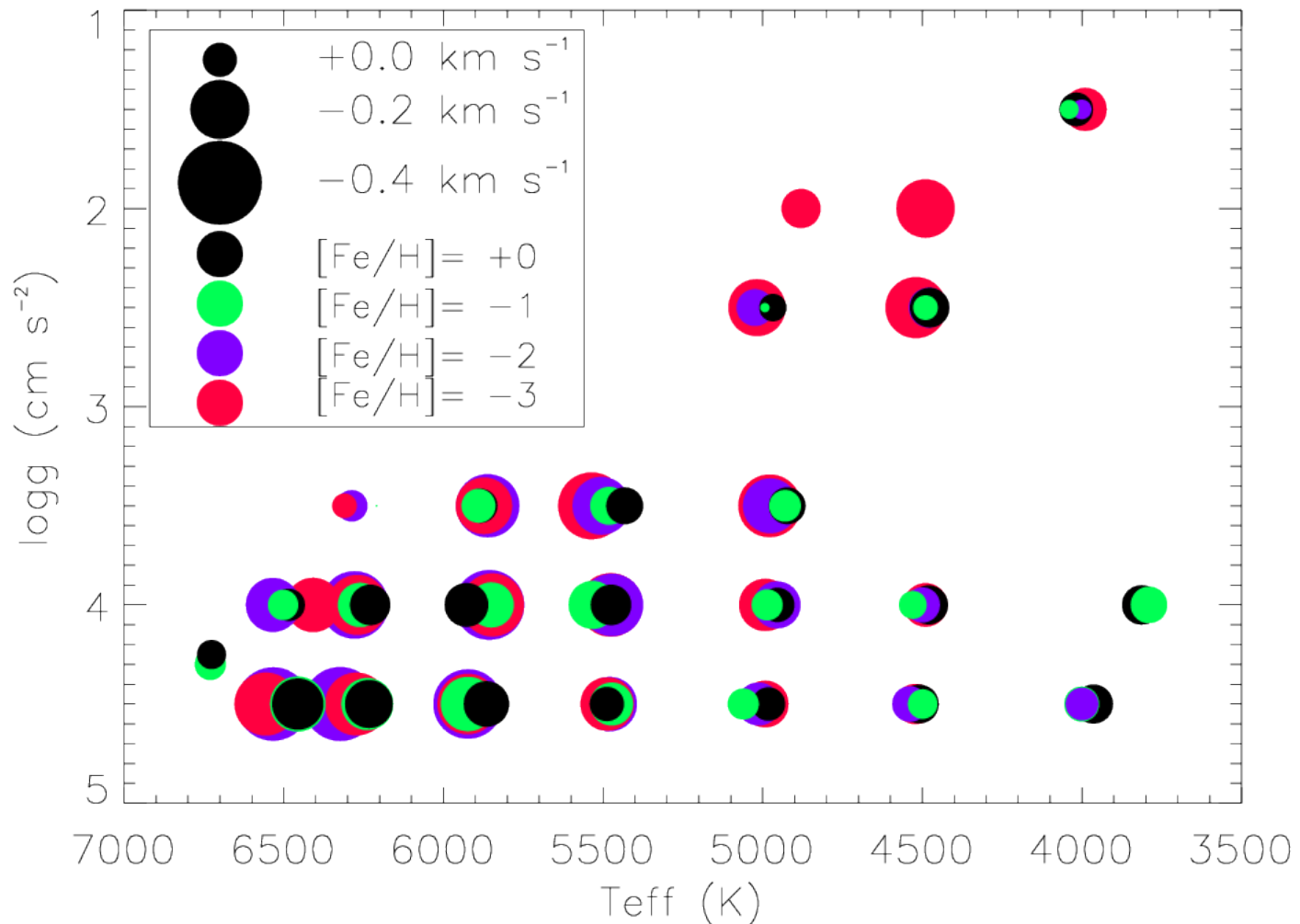
GES UVES stars: measured ξ_{micro} vs. recommended calibration



(red points: giants $\log g < 3.5$)

- Dispersion does not show obvious correlation with atmospheric parameters??

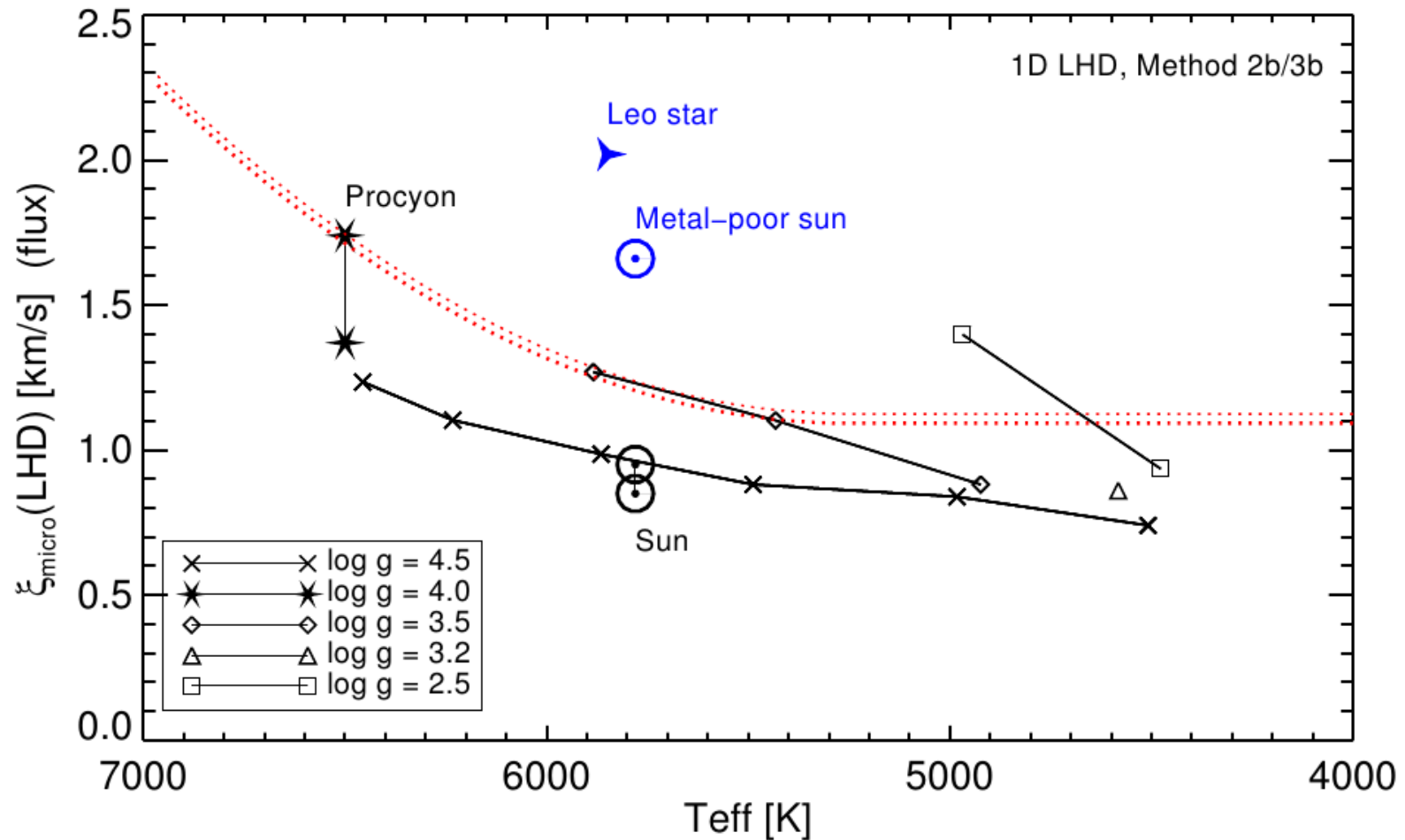
Predicted line shifts for Gaia's Radial Velocity Spectrometer



(Allende Prieto et al. 2013)

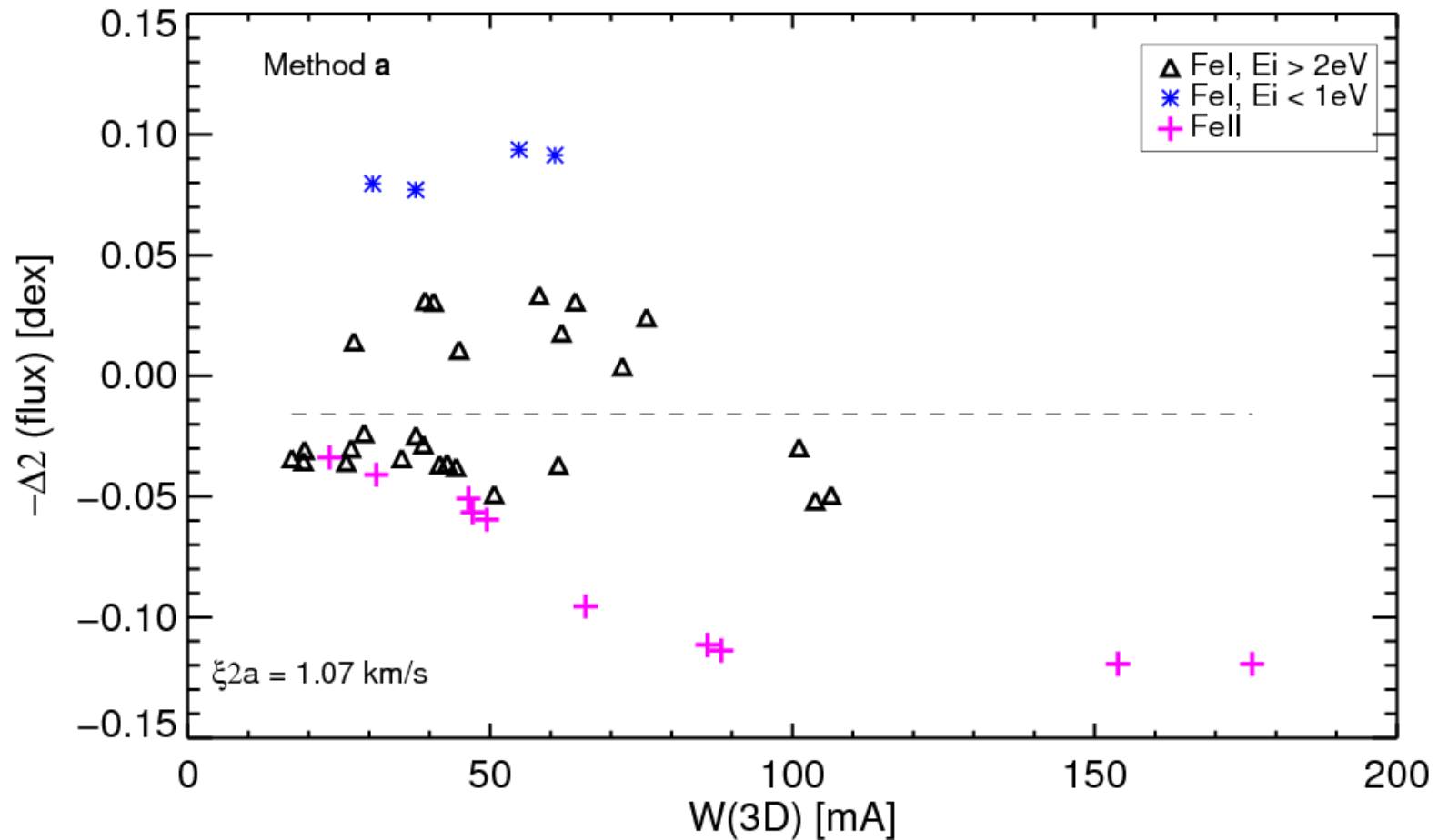
- Correcting spectroscopic radial velocities to actual stellar space motion
- 3D synthesis of RVS spectral range **serious computational effort** → Ranger@TACC

Microturbulence from 3D models (Steffen et al. 2013)



- CO⁵BOLD 3D model to provide “observation”, here mostly $[M/H] = 0$
- Interpret 3D line strength with help of 1D model
 - resolution of 3D models?
 - mismatch between 1D and 3D model in thermal structure?

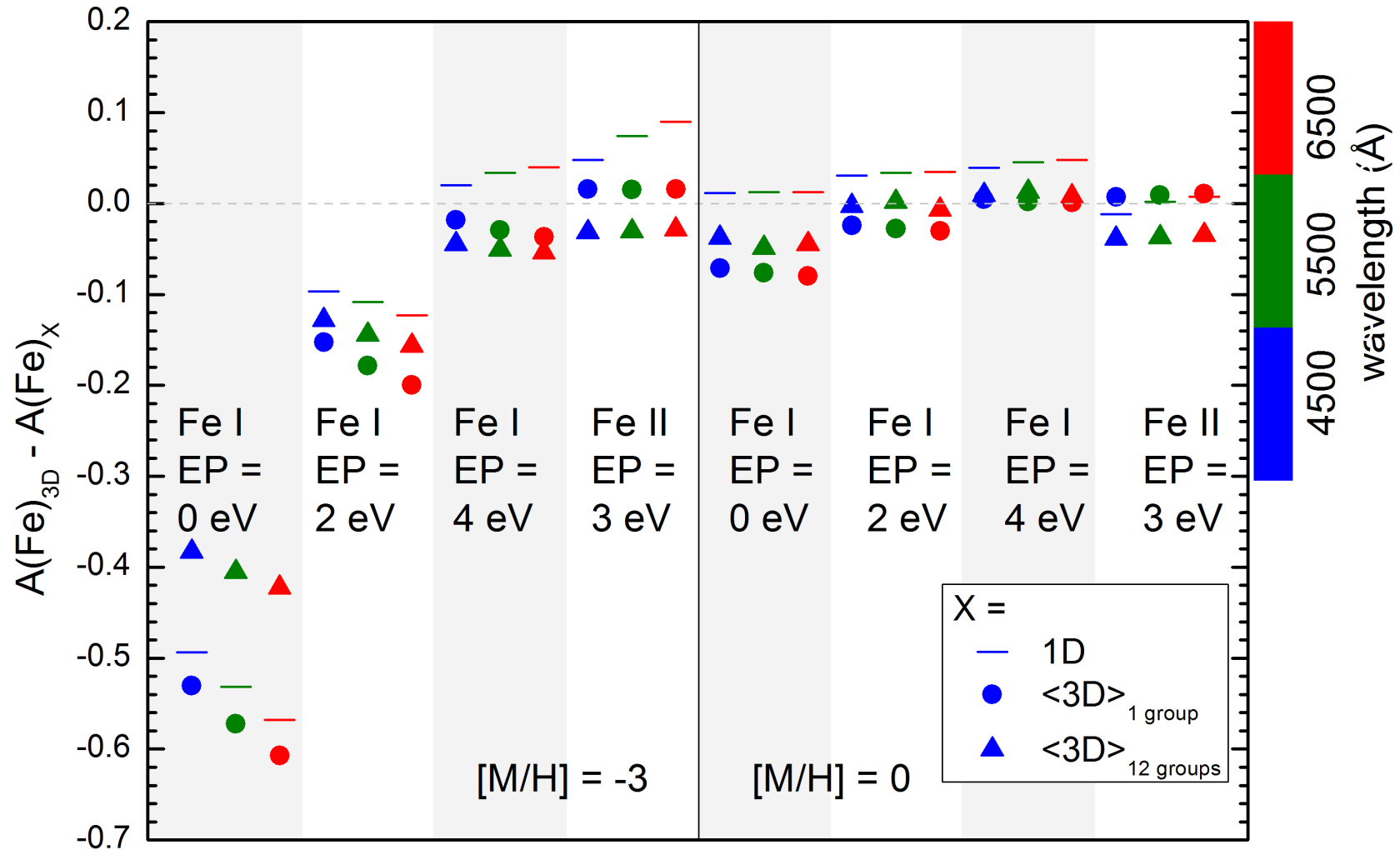
Precision limits to 1D analysis: e.g. solar-metallicity F-dwarf



- **Ideal situation:** perfect LTE, line strengths and parameters exactly known
- Model of solar metallicity: 1D and $\langle 3D \rangle$ model very similar
→ T-fluctuations drive differences and **significant dispersion**

Best 1D representation of 3D model? (intensity)

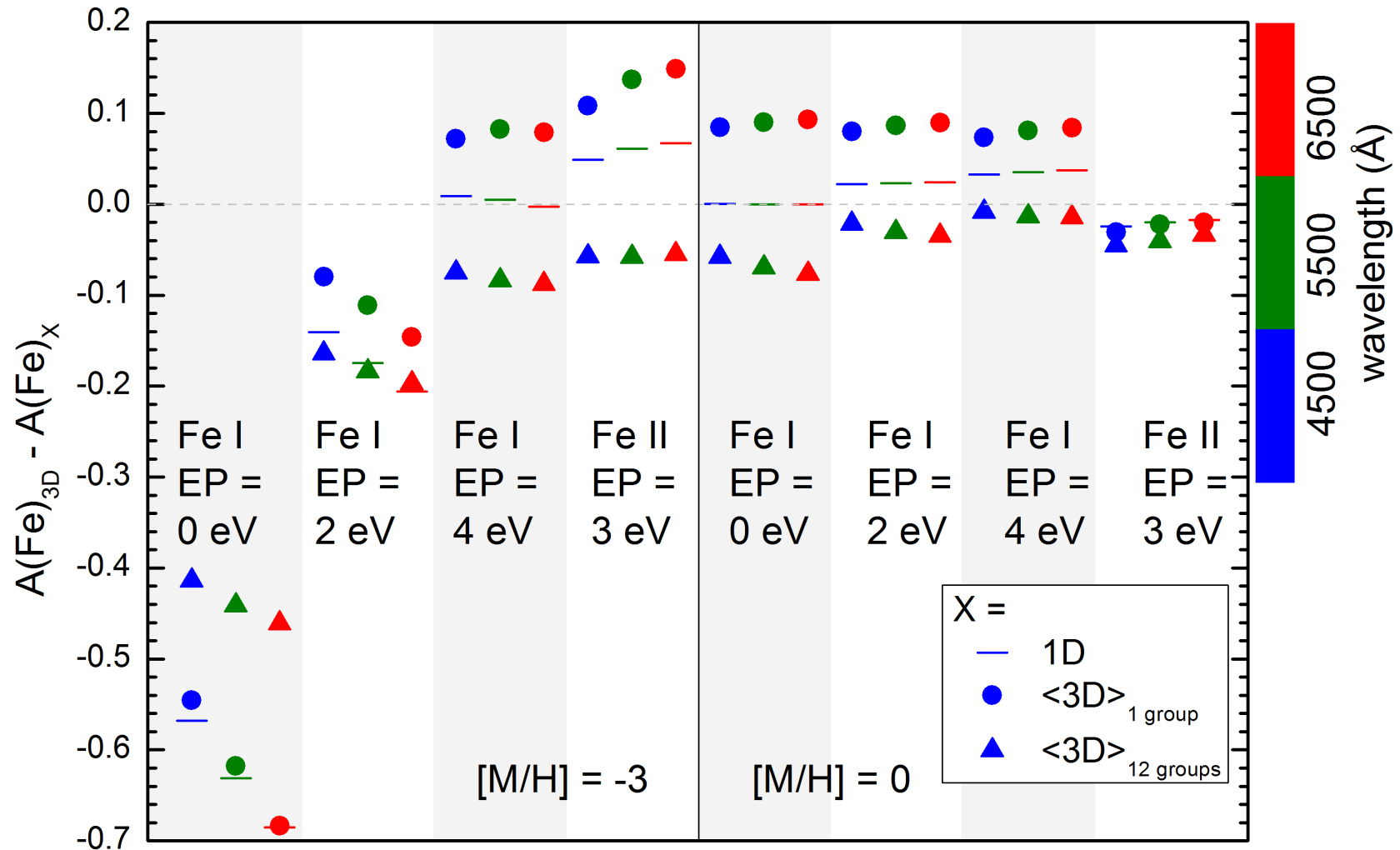
CO⁵BOLD $T_{\text{eff}} = 5000$ K, $\log g = 2.5$ [cgs], for lines with $\text{EW} < 1$ mÅ
disk center



(Klevas 2013, priv. comm.)

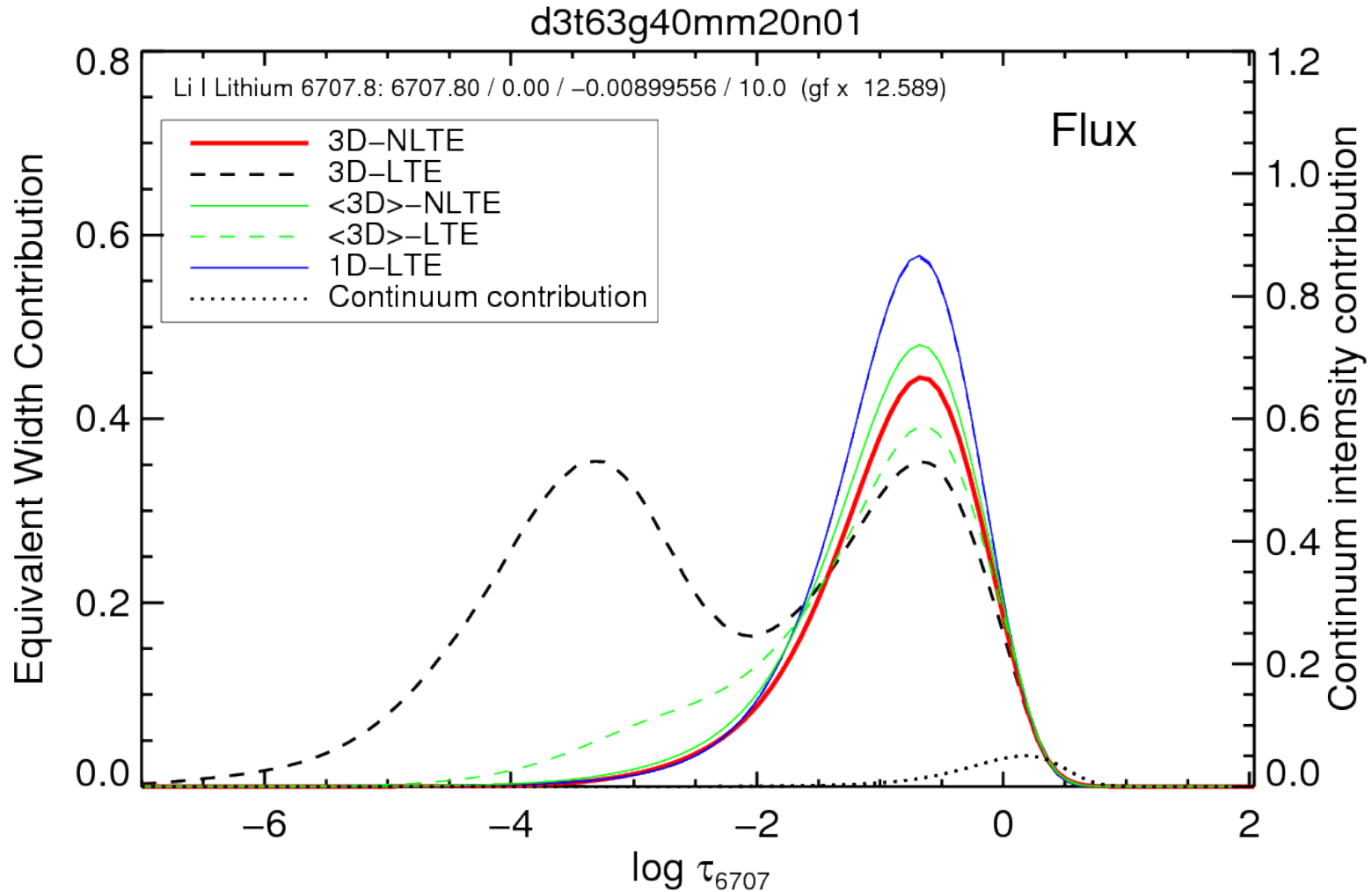
Best 1D representation of 3D model? (flux)

CO⁵BOLD $T_{\text{eff}} = 5000$ K, $\log g = 2.5$ [cgs], for lines with $\text{EW} < 1$ mÅ
disk-integrated



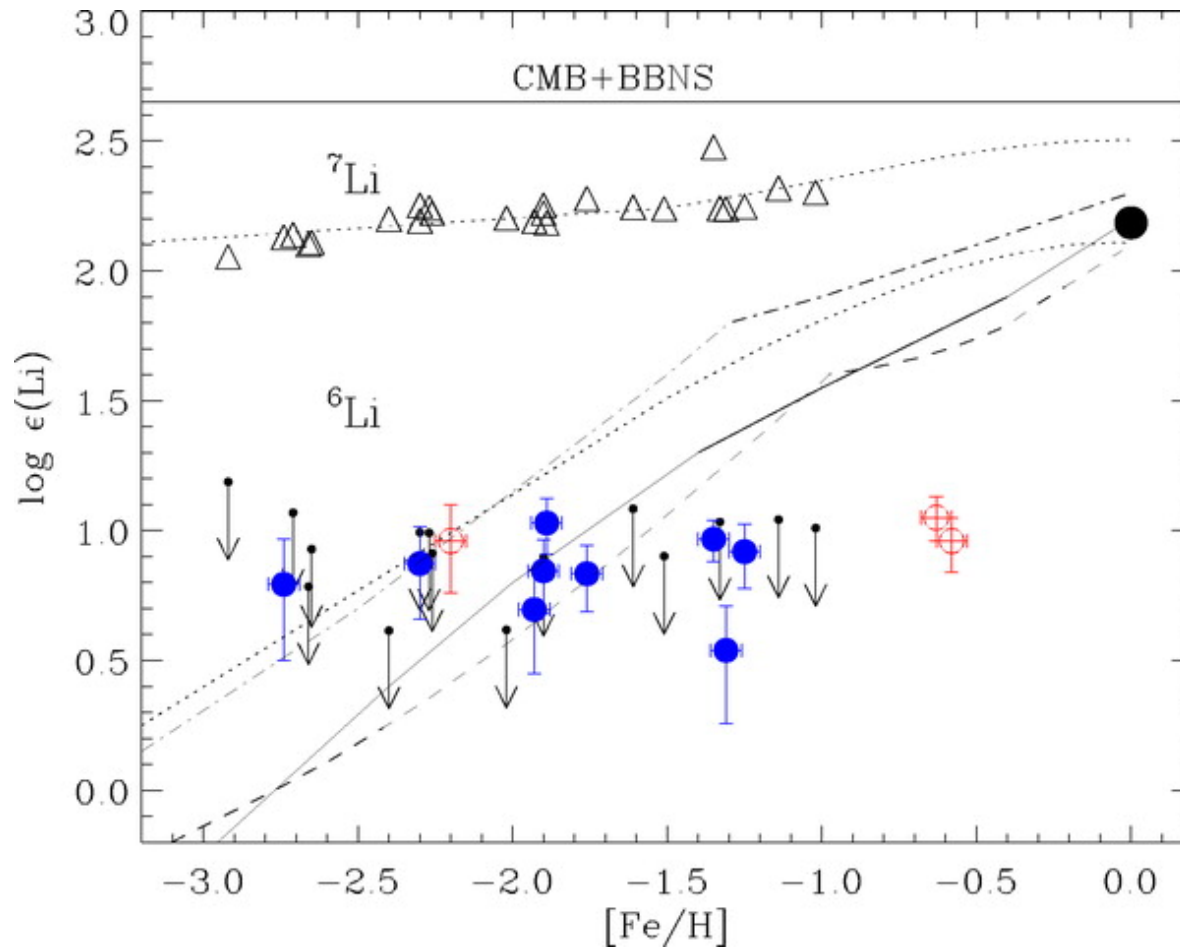
(Klevas 2013, priv. comm.)

Departures from LTE 3D, $\langle 3D \rangle$, and 1D



(Steffen 2013, priv. comm.)

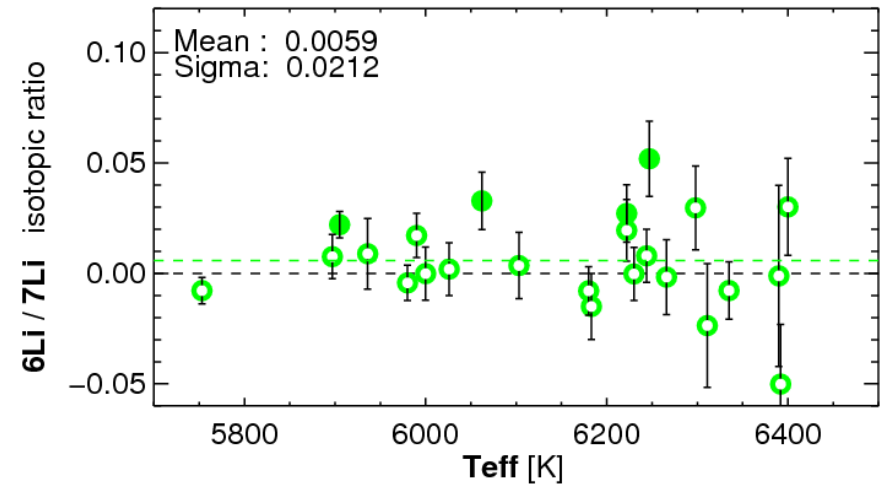
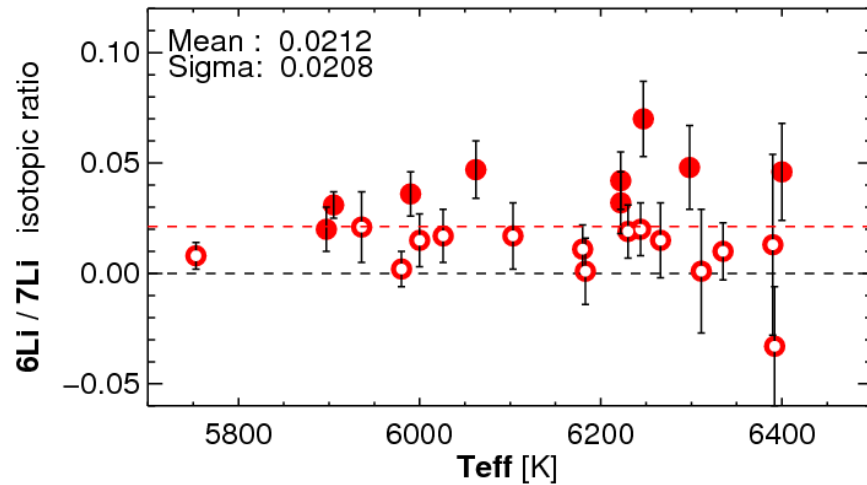
^6Li and ^7Li in metal-poor halo stars



(Asplund et al. 2006; Smith et al. 1993, 1998; Cayrel et al. 1999; Nissen et al. 1999; chemical evolution models: Prantzos 2006; Ramaty et al. 2000; Fields & Olive 1999; Vangioni-Flam et al. 2000)

- Not corrected for stellar endogenic depletion; arrows indicate 3σ upper limits
- Essentially no ^6Li production during Big Bang; but measured isotopic ratio ≈ 0.05

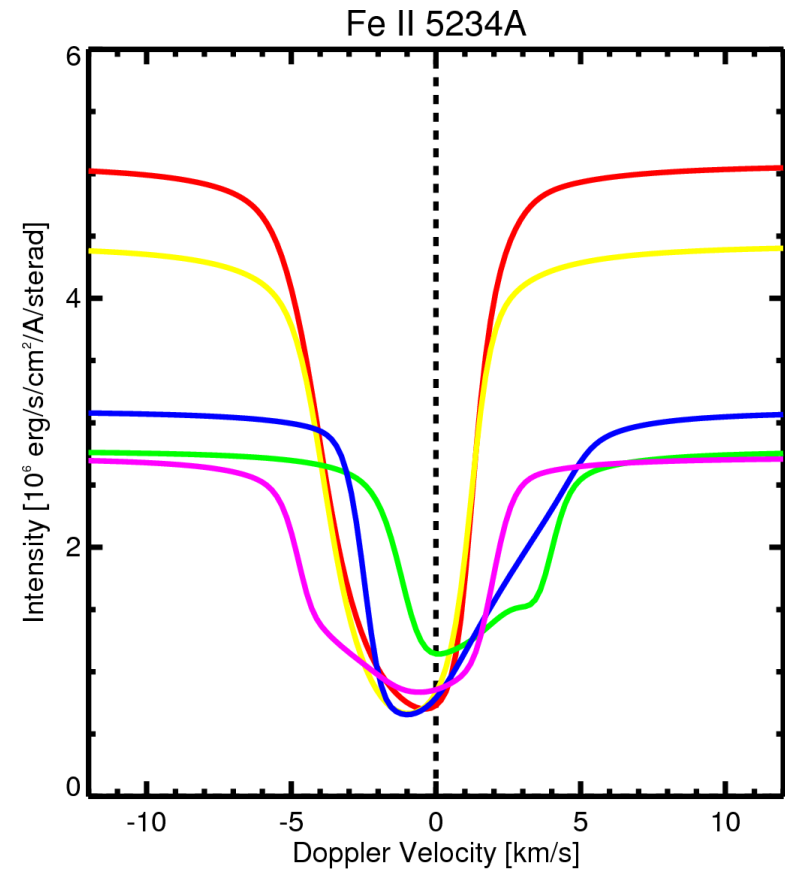
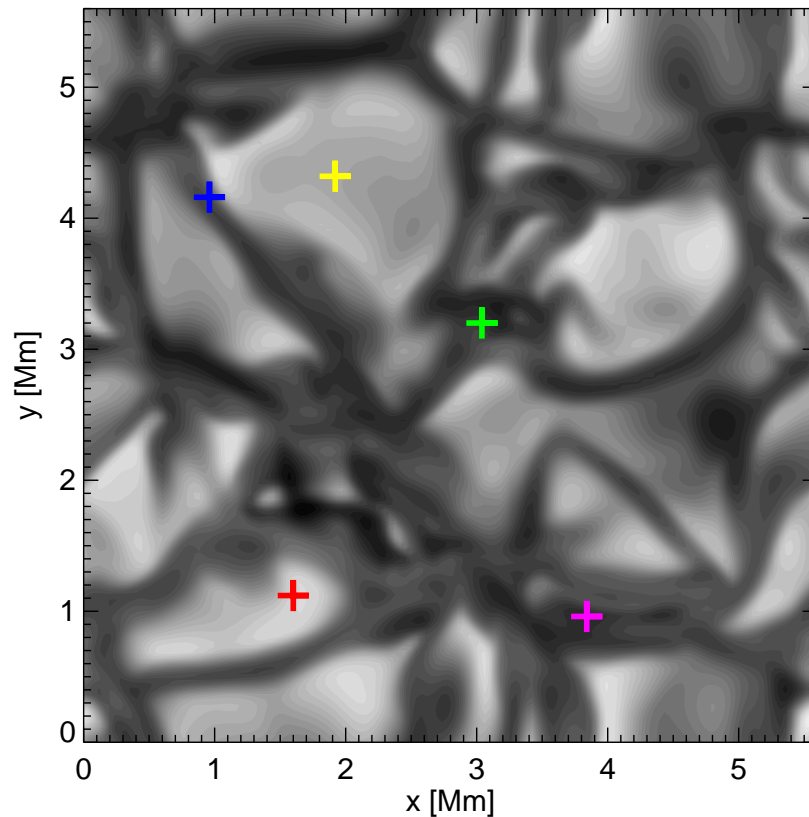
Detections when accounting for 3D and NLTE effects



solid: detections / open: non-detections / left: Asplund et al. 2006 / right: corrected

- Reduction from 9 to 2-4 detections out of 24 2σ observations
- ^6Li in metal-poor halo stars rather the exception than the rule

3D spectral line formation with the Linfor3D package



- Variations in line strength, width, shift, asymmetry across granulation pattern
- Non-linearities cause net effects in disk-integrated light
- Knowledge of detailed line shapes \rightarrow no micro/macro-turbulence