

19th MHD days  
2.-4. December 2024  
Leibniz Institute for  
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# Sunspot simulations with potential field initial conditions



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GAČR-DFG Project Unveiling the principles of solar magneto-convection  
computations using SOLARNET Trans-national Access Program, funded by the EU under grant number 824135

# Overview

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- Introduction & Motivation
- Methods & boundary conditions
- Initial conditions
- Parameter study
  - what can go wrong
  - what differences in good simulations
- Example simulation
  - Velocities
  - Flux emergence
- Conclusion

Unit conversion to SI:

$$10\text{kG} = 1\text{Tesla}$$

$$10^{22}\text{Mx} = 10^{14}\text{Weber}$$

# Introduction

- Many high-resolution observations of sunspots exist, particularly of the stable and decaying phase
- Only a few groups attempted radiative magneto-hydrodynamics simulations of sunspots
- Rempel (2009, *Science*, 325, 171) presented a simulation, that looks like 2 sunspots and has flow directions consistent with observations
- Rempel (2012, *ApJ*, 750, 62) showed an improved version, standard until today
- Jurčák+ (2020, *A&A* 638, A28) showed, that the magnetic field distribution of simulations and observations are different, particularly at the umbral boundary  $B_{\text{ver}}$  and inclinations

# Motivation: $B_{\text{ver}}$ @ umbral boundary const.

- Jurčák+ (2018, A&A 611, L4) showed that  $B_{\text{ver}}$  at the umbral boundary is independent of sunspot size and traced the umbral boundaries
- Schmassmann+ (2018, A&A 620, A104) showed that  $B_{\text{ver}}$  at the umbral boundary is constant in time

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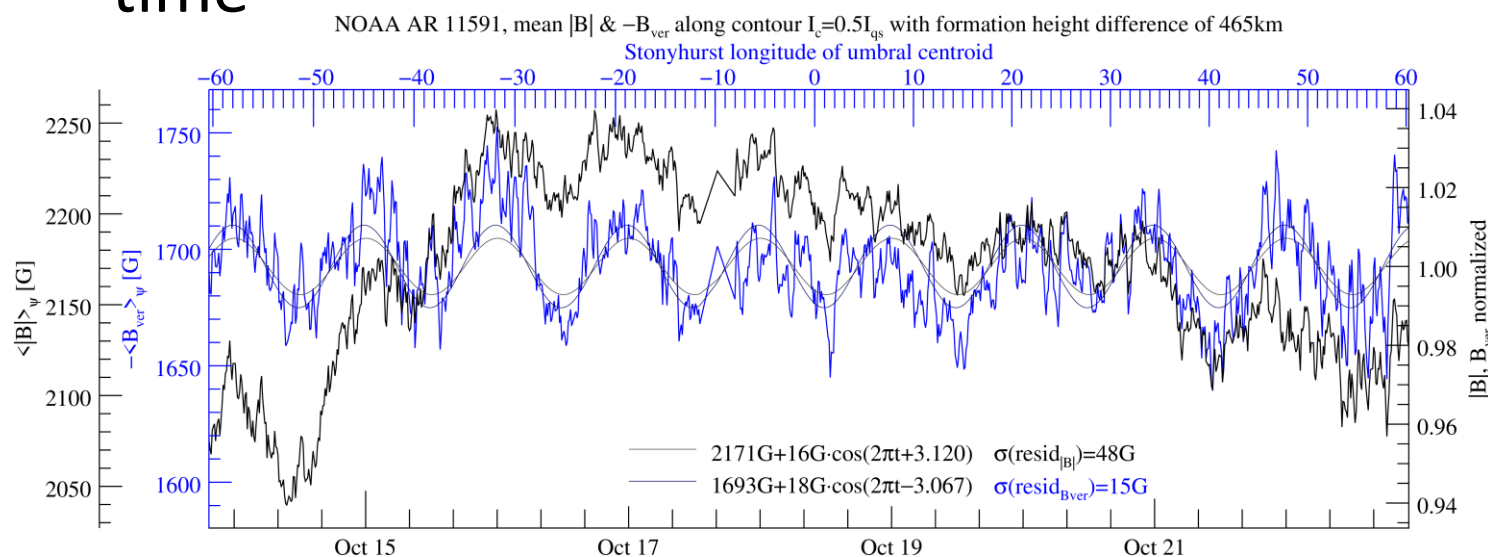
[Jurčák et al, 2018, A&A 611, L4](#)

Figure 2, bottom panel

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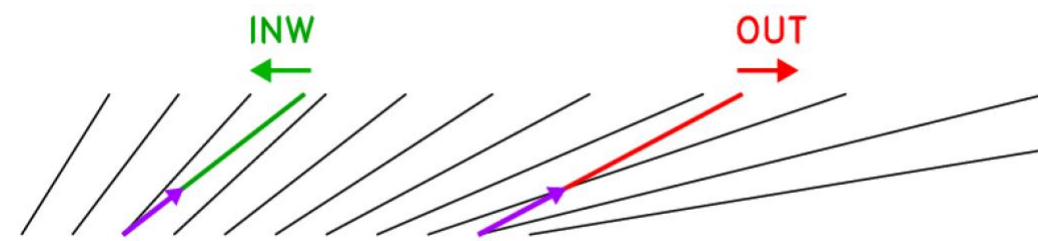
[Jurčák et al, 2018, A&A 611, L4](#)

Figure 1



# Motivation 2: Importance of inclination in the penumbra

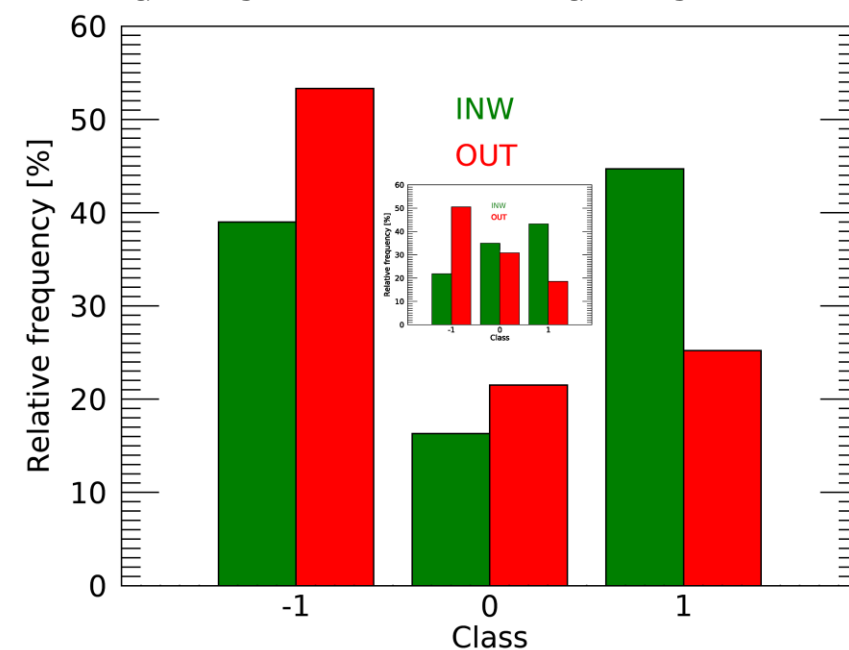
- Sobotka+ (2024, A&A 682, A65) showed that the inclination difference between penumbral grains (PGs) and their surrounding is correlated with their movement direction
- Therefore, if little penumbral-type convection occurs at inclinations typical for the inner penumbra, few PGs have inclinations larger than their surroundings (class 1), and we miss inward-moving PGs. Analysis performed on the continuation of Rempel2012,  $\alpha = 2$ . The inset shows results from observation for comparison. Sobotka+ (2024, A&A awaiting reviewer response)



Surrounding penumbral magnetic field

Class 1:  $\gamma_{PG} > \gamma_s$

Class -1:  $\gamma_{PG} < \gamma_s$



# Motivation 3: box height

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- Forcing the field to be more horizontal than natural at the top boundary ( $\alpha = 2$ ) only influences the surface and below, if the box ends close to the surface
- Simulations creating flares & CMEs require higher boxes
- Potential or other force-free field top boundary conditions required

# Methods & boundary conditions

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Simulation using MURaM radiative MHD code with default settings, in particular:

- Bottom boundary condition: open boundary, symmetric field, called *OSb* in Rempel 2014, ApJ 789, 132, Sec. 2.2
- Potential magnetic field top boundary condition, see Rempel, 2012, ApJ, 750, 62 or Cheung, 2006, PhD thesis

Non-standard MURaM, fixing internal energy per mass in regions with high Alfvén velocity, as used in type I sunspot sim Jurčák+ 2020, A&A, 638, A28

# Initial conditions

- Initial conditions, potential field, based on an idea by Nordlund 2015, Nordita imposed on small-scale dynamo simulation:

$$B_{z,0}(r) = B_0 \exp\left(-\frac{r^2 B_0 \pi}{F_{\text{Gauss}}}\right) - B_{\text{opp}}$$

$$F_{\text{tot}} = \int B_{z,0} \left(\sqrt{x^2 + y^2}\right) dx dy = F_{\text{Gauss}} - B_{\text{opp}} w^2$$

$$B_z = \mathcal{F}^{-1} \left( \mathcal{F}(B_{z,0}) e^{-z|k|} \right)$$

$$B_x = \mathcal{F}^{-1} \left( \mathcal{F}(B_{z,0}) \frac{-ik_x}{|k|} e^{-z|k|} \right)$$

- Varying from  $B_0 = 160 \text{ kG}$ ,  $B_{\text{opp}} = 0 \text{ G}$ ,  $F_{\text{Gauss}} = F_{\text{tot}} = 10^{22} \text{ Mx}$ ,  $w = 49 \text{ 152 km}$



# Parameter study

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Reducing initial field strength

$$B_0 = 20\text{kG}, 40\text{kG}, 80\text{kG}, 160\text{kG}$$

Subtracting constant vertical offset

$$B_{\text{opp}} = 0, 50, 100, 150, 200, 300 \text{ G}$$

Increasing width of the box

$$w = 49 \ 152 \text{ km}, 98 \ 304 \text{ km}$$

Fixing  $F_{\text{Gauss}}$  or  $F_{\text{tot}} = 10^{22} \text{ Mx}$

# Parameter study, $B_0$

Reducing initial field strength

$B_0 = 20\text{kG}, 40\text{kG}, 80\text{kG}, 160\text{kG}$

Subtracting constant vertical offset

$B_{\text{opp}} = 0, 50, 100, 150, 200, 300 \text{ G}$

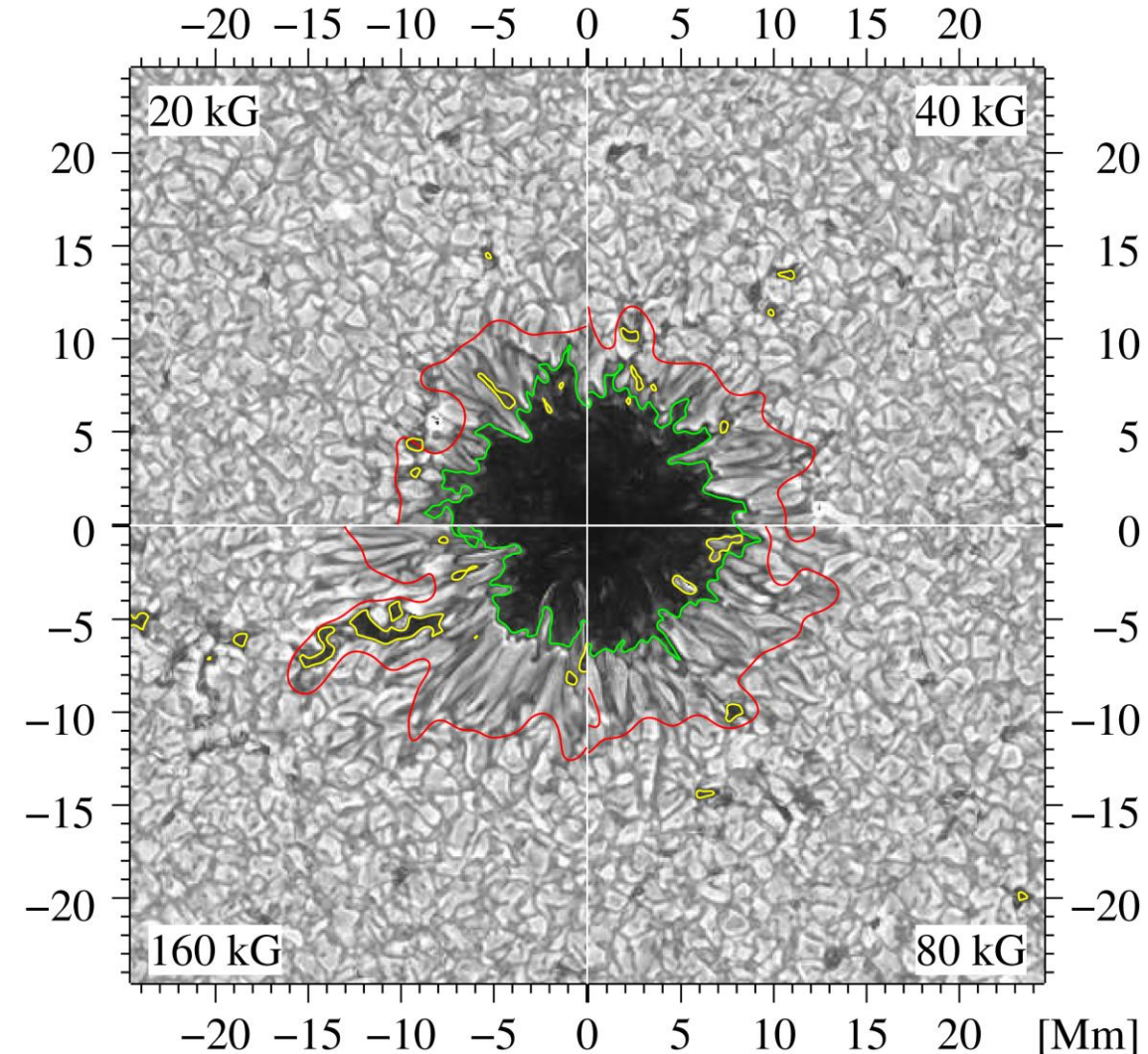
Increasing width of the box

$w = 49 \text{ km}, 152 \text{ km}, 98 \text{ km}, 304 \text{ km}$

Fixing  $F_{\text{Gauss}}$  or  $F_{\text{tot}} = 10^{22} \text{ Mx}$

$B_0 < 160 \text{ kG}$

results in too narrow a penumbra



# Parameter study, increasing $F_{\text{Gauss}}$

Reducing initial field strength

$$B_0 = 20\text{kG}, 40\text{kG}, 80\text{kG}, 160\text{kG}$$

Subtracting constant vertical offset

$$B_{\text{opp}} = 0, 50, 100, 150, 200, 300 \text{ G}$$

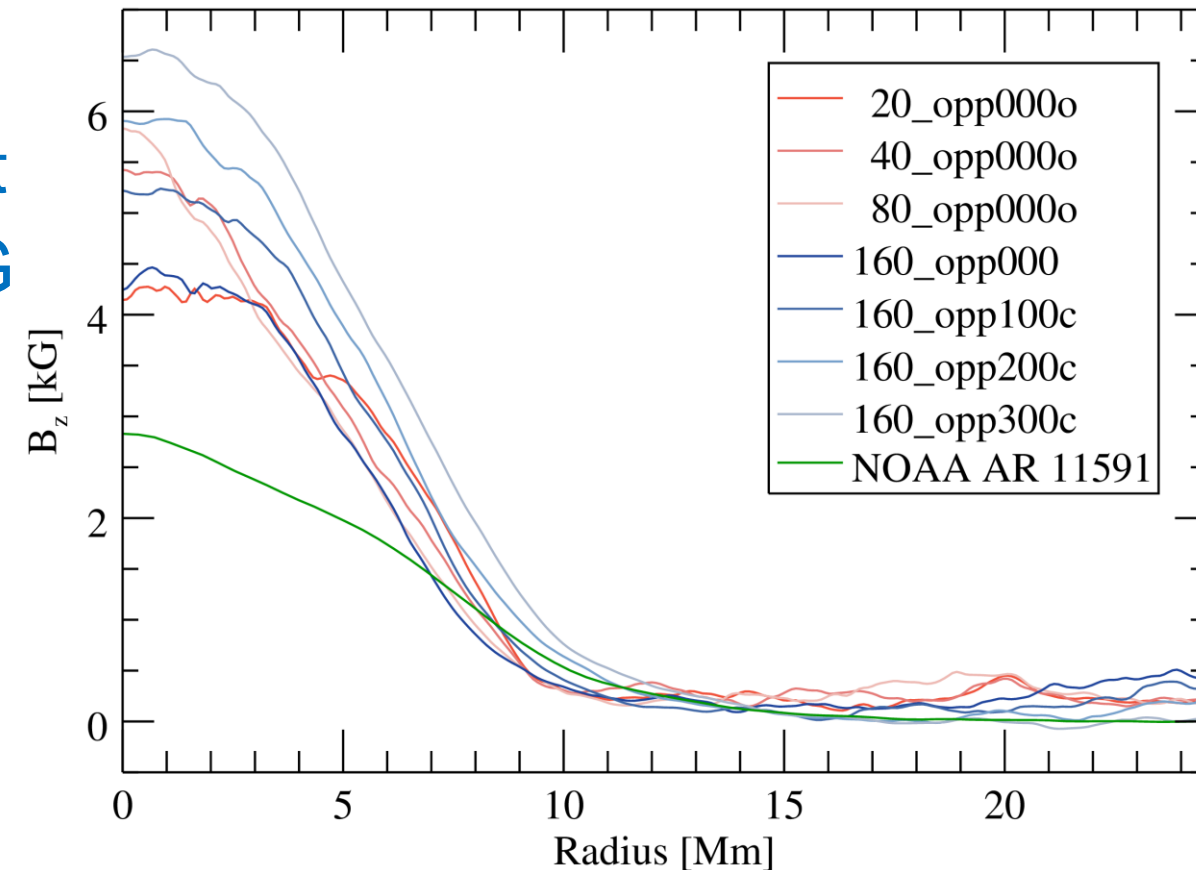
Increasing width of the box

$$w = 49 \text{ km}, 152 \text{ km}, 98 \text{ km}, 304 \text{ km}$$

Fixing  $F_{\text{Gauss}}$  or  $F_{\text{tot}} = 10^{22} \text{ Mx}$

$$F_{\text{Gauss}} > 10^{22} \text{ Mx}$$

results in too strong fields in the umbra



# Parameter study, decreasing $F_{\text{tot}}$

Reducing initial field strength

$$B_0 = 20\text{kG}, 40\text{kG}, 80\text{kG}, 160\text{kG}$$

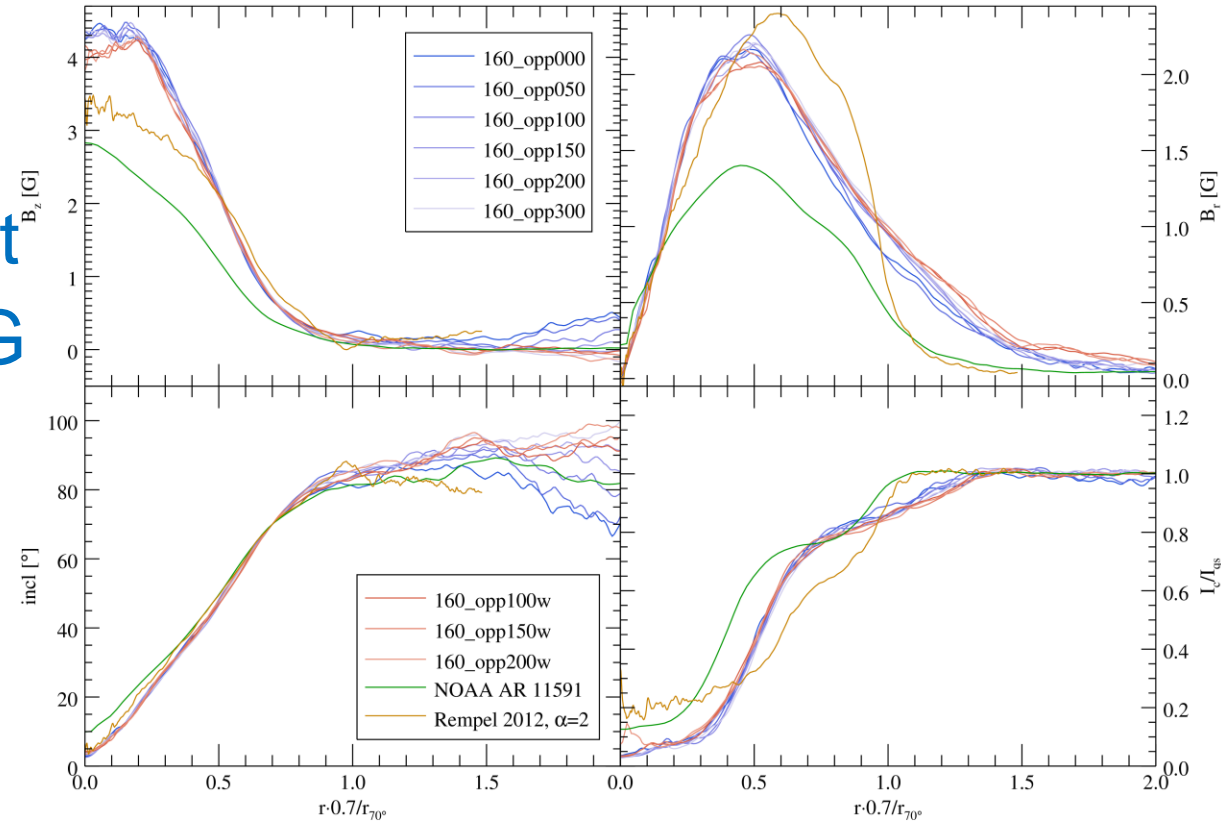
Subtracting constant vertical offset

$$B_{\text{opp}} = 0, 50, 100, 150, 200, 300 \text{ G}$$

Increasing width of the box

$$w = 49 \text{ km}, 152 \text{ km}, 98 \text{ km}, 304 \text{ km}$$

Fixing  $F_{\text{Gauss}}$  or  $F_{\text{tot}} = 10^{22} \text{ Mx}$



Changing  $B_{\text{opp}}$  with  $F_{\text{Gauss}} = 10^{22} \text{ Mx}$   
changes little within the spot, but  
dominates outside

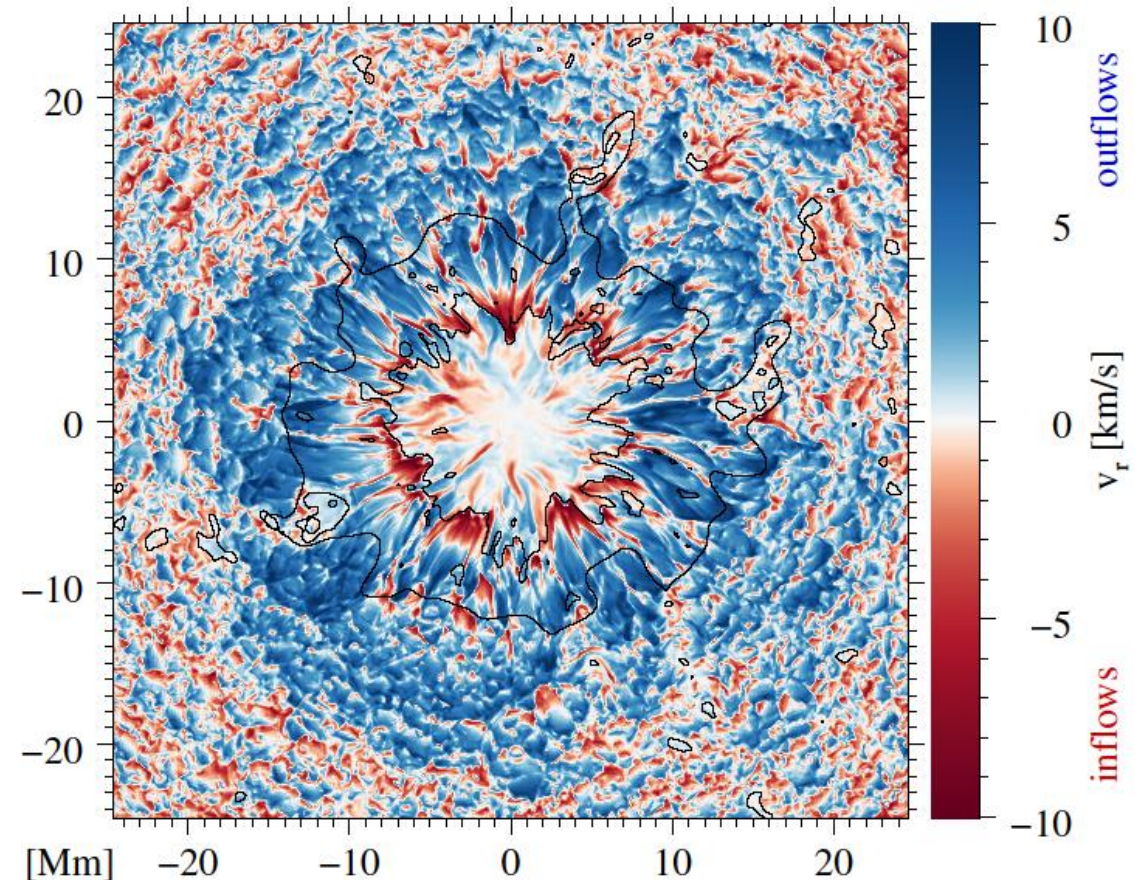
# Radial velocities

simulation:  $B_0 = 160 \text{ kG}$ ,  $B_{\text{opp}} = 0 \text{ G}$ ,  $F_{\text{Gauss}} = F_{\text{tot}} = 10^{22} \text{ Mx}$ ,  $w = 49\,152 \text{ km}$

- Inside the umbra, flows are slow and often associated with waves
- The penumbral filament heads at the umbral boundary show in- and down-flows
- This is more consistent with observations of penumbra formation than with stable sunspots

García-Rivas+ (2024, A&A, 686, A112)

- Also, flux within the spot increases  $0.59 \rightarrow 0.65 \cdot 10^{22} \text{ Mx}$  in  $3\text{h} \rightarrow 4\text{h}$



# Ongoing flux emergence

Simulation:

$$B_0 = 160\text{kG}, B_{\text{opp}} = 0\text{G}, F_{\text{Gauss}} = F_{\text{tot}} = 10^{22}\text{Mx}, w = 49\ 152\ \text{km}$$

Open video: [lout\\_vel2\\_flux\\_1432x1080\\_h265\\_crf29.mp4](#)



- very dynamic initial phase
- ongoing flux emergence afterward
- When flux emergence stops, the penumbra gets narrower.
- supporting relation to forming penumbrae

# Conclusions

- Using the potential field approach,  $B_0 = 160\text{kG}$  and  $F_{\text{Gauss}} = 10^{22}\text{Mx}$ , it is possible to create sunspot simulations
- Subtracting a uniform vertical field  $B_{\text{opp}}$  has little influence on the spot itself, but allows to control  $B_{\text{ver}}$  outside the spot
- The gas flows in the penumbral filaments of such simulations are more consistent with a forming penumbra, than with a stable sunspot
- Such simulations show ongoing flux emergence

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# Thank you for your attention

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- Questions?
- Anyone interested in sunspot simulation data?

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And thanks for the funding and access to computing time to

- GAČR-DFG Project Unveiling the principles of solar magneto-convection
- SOLARNET Trans-national Access Program, funded by the EU under grant number 824135



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- \*.mov for QuickTime and other dumb players